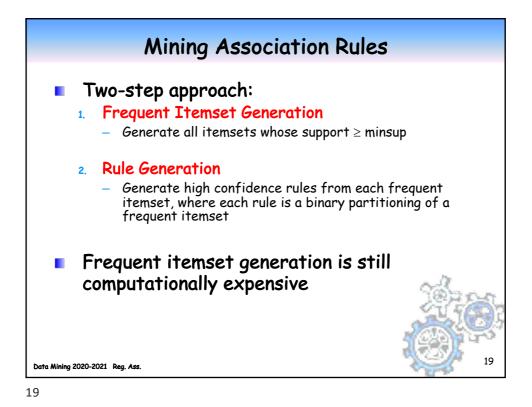




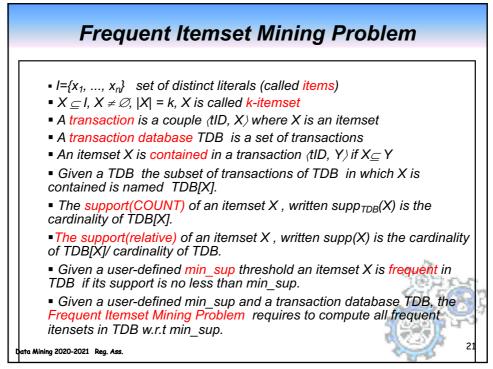
	Mining Association Rules				
TID 1 2 3 4 5	ItemsBread, MilkBread, Diaper, Beer, EggsMilk, Diaper, Beer, CokeBread, Milk, Diaper, BeerBread, Milk, Diaper, Coke	Example of Rules: {Milk,Diaper} \rightarrow {Beer} (s=0.4, c=0.67) {Milk,Beer} \rightarrow {Diaper} (s=0.4, c=1.0) {Diaper,Beer} \rightarrow {Milk} (s=0.4, c=0.67) {Beer} \rightarrow {Milk,Diaper} (s=0.4, c=0.67) {Diaper} \rightarrow {Milk,Beer} (s=0.4, c=0.5) {Milk} \rightarrow {Diaper,Beer} (s=0.4, c=0.5)			
Obs	ervations:				
• All t	the above rules are binary p {Milk, Diaper, Beer}	partitions of the same itemset:			
	Rules originating from the same itemset have identical support but can have different confidence				
• Thu	is, we may decouple the su	pport and confidence requirements			
ta Mining 20	a Mining 2020-2021 Reg. Ass. 18				

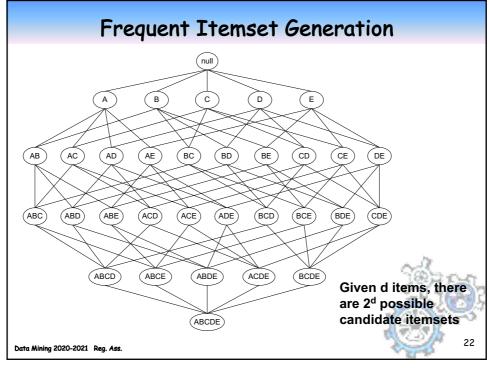


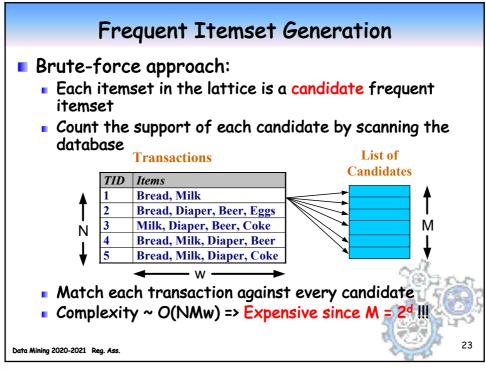
Basic Apriori Algorithm
Problem Decomposition

Find the *frequent itemsets*: the sets of items that satisfy the support constraint
A subset of a frequent itemset is also a frequent itemset, i.e., if {A,B} is a frequent itemset, both {A} and {B} should be a frequent itemset
Iteratively find frequent itemsets with cardinality from 1 to k (k-itemset)

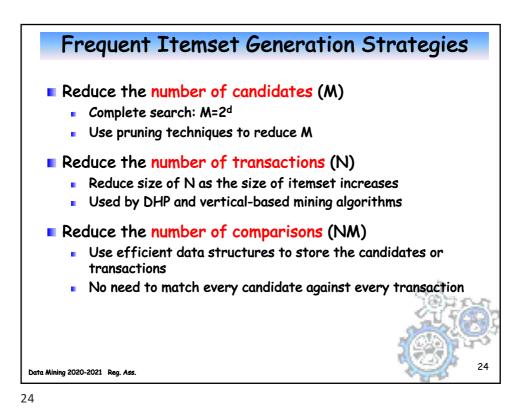
Use the frequent itemsets to generate association rules.

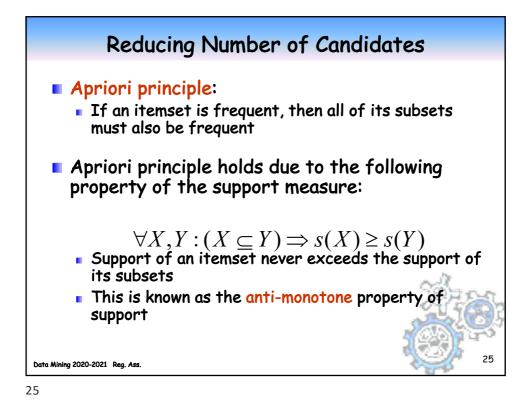


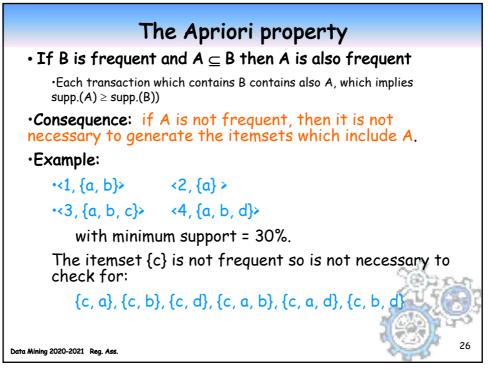


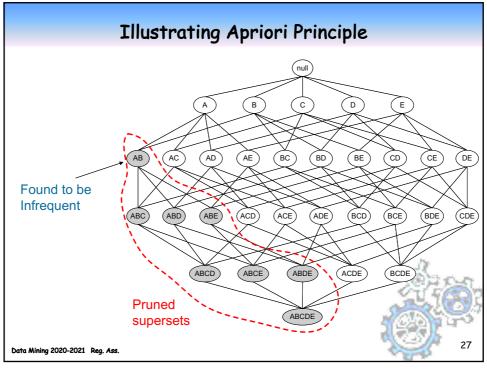


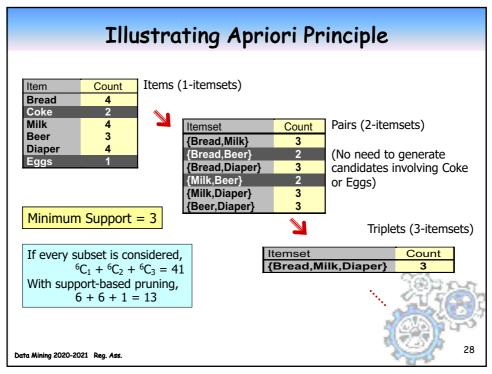


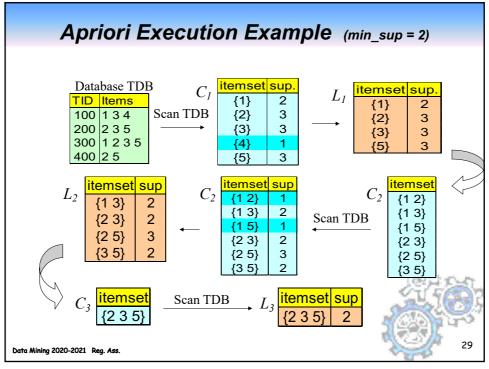




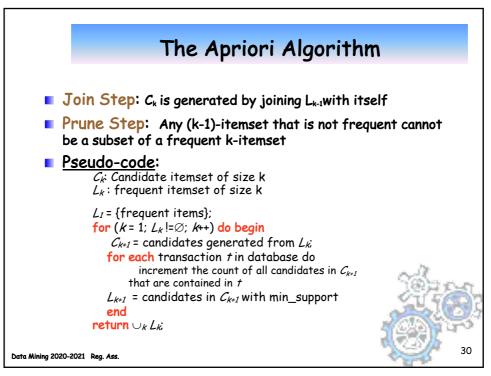


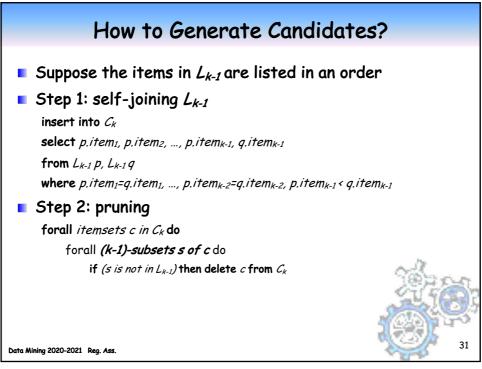




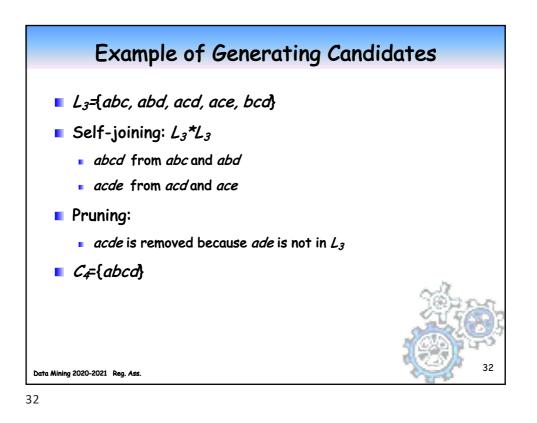


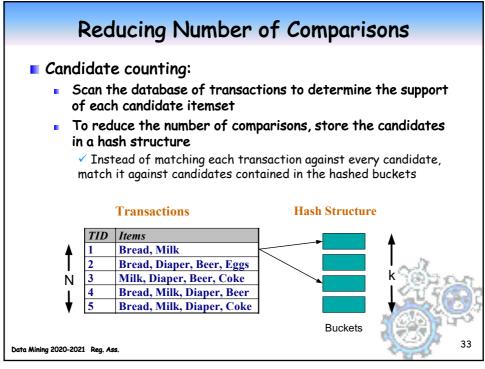




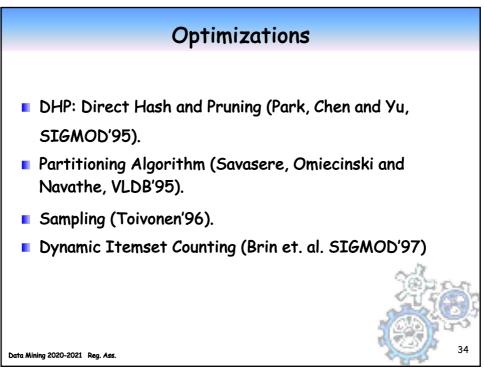


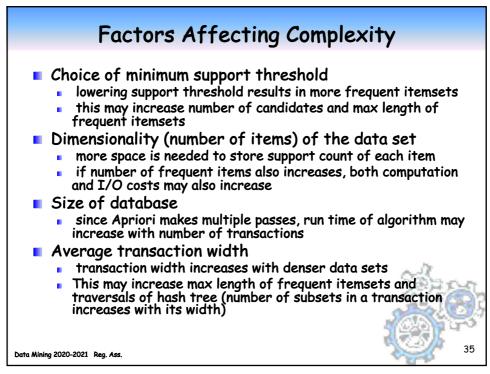


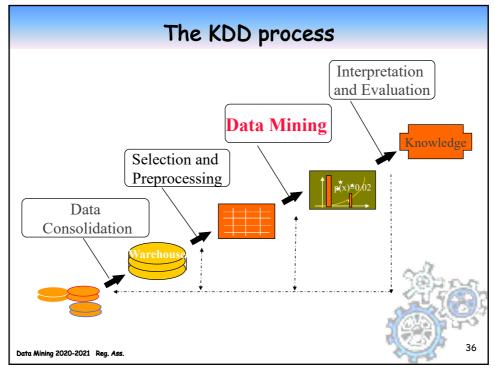


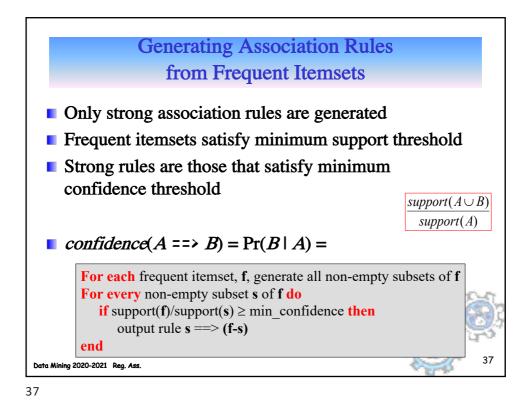


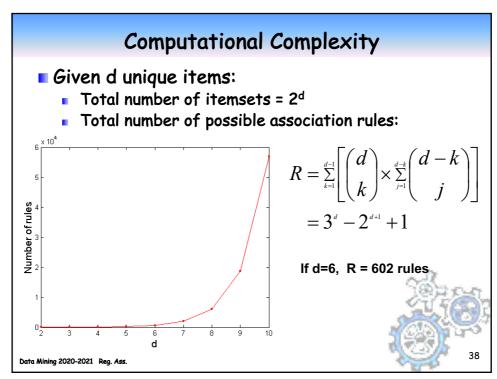


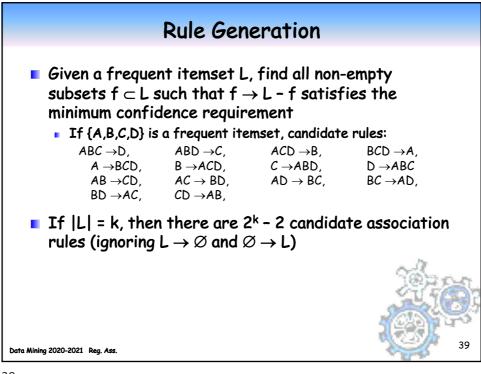


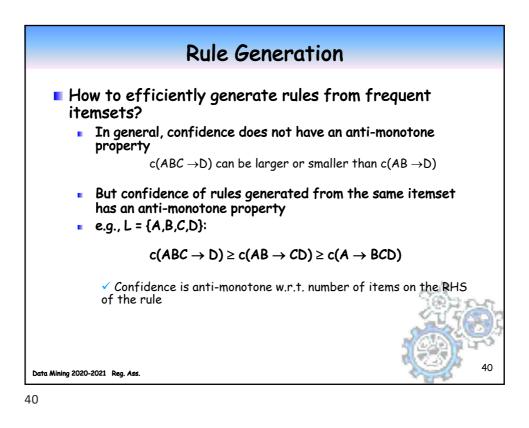


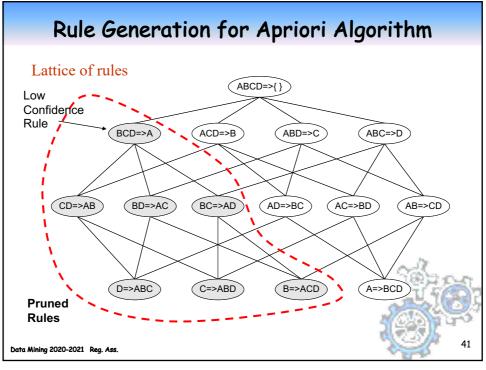




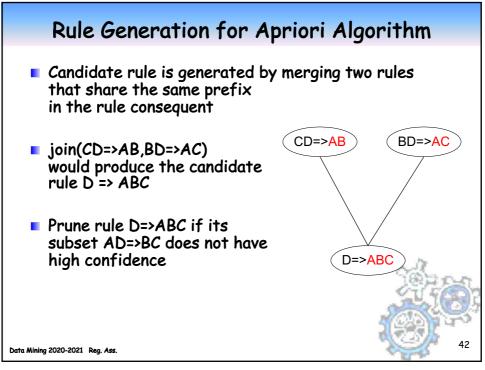


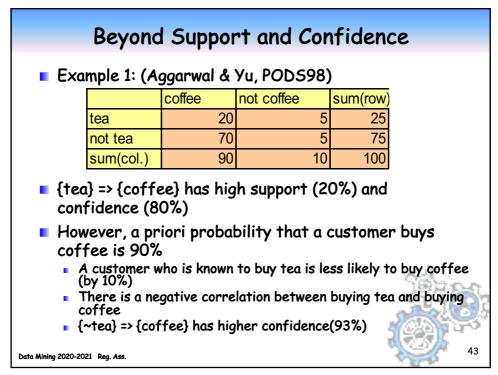


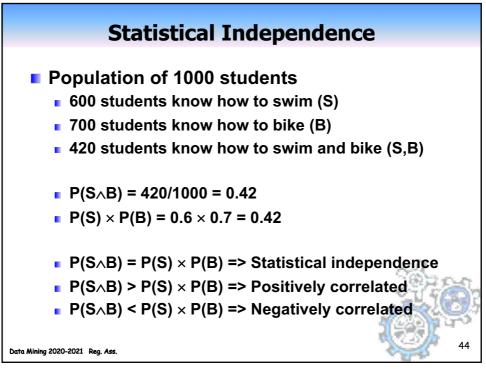


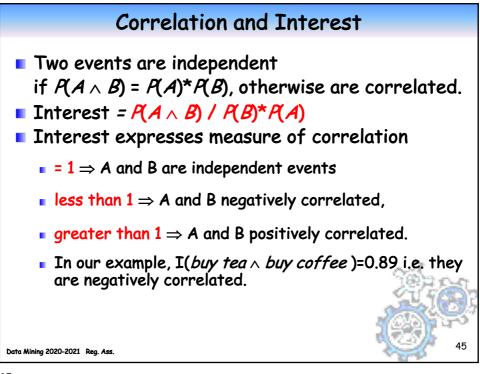


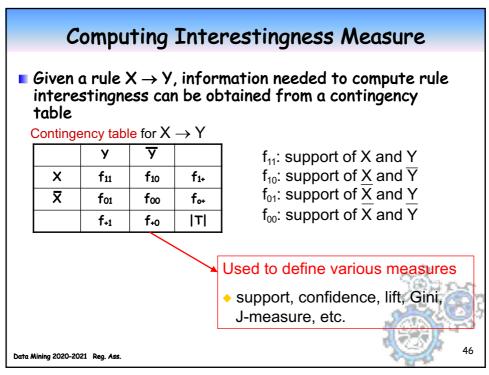


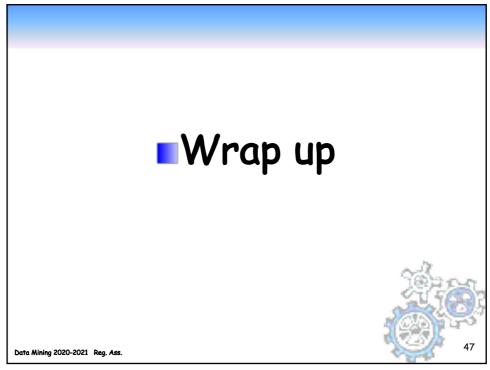


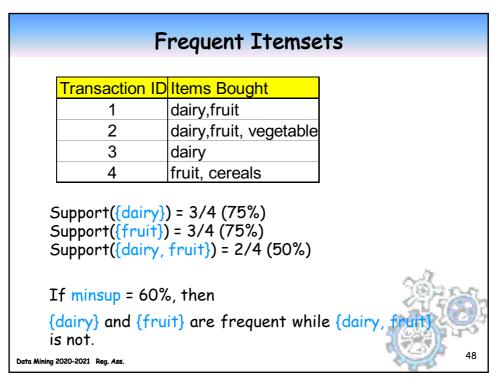


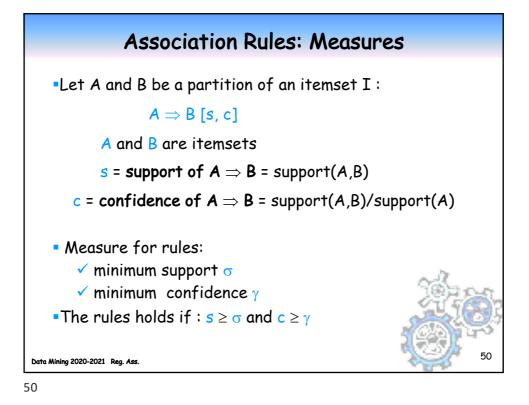


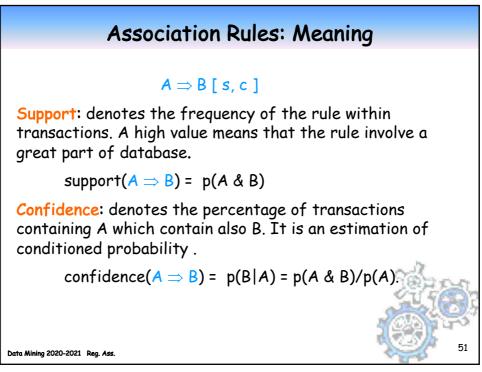


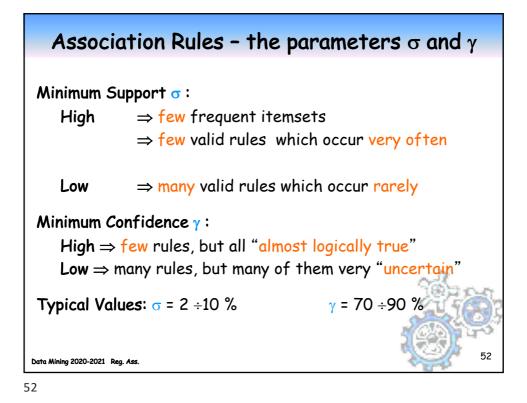


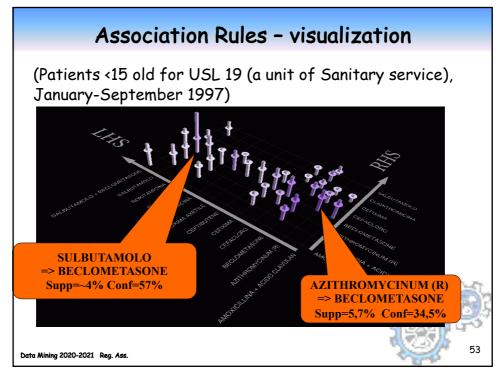


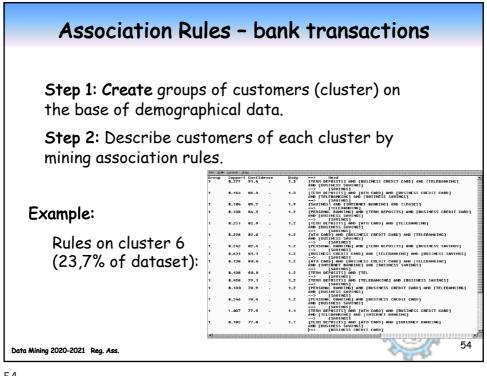








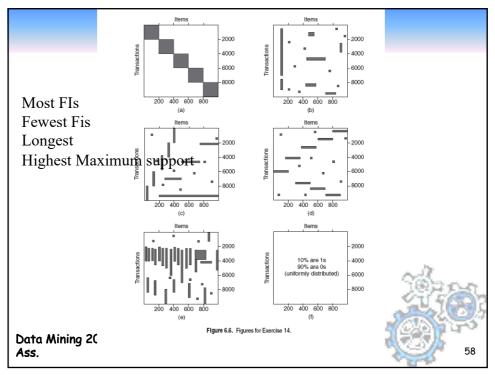


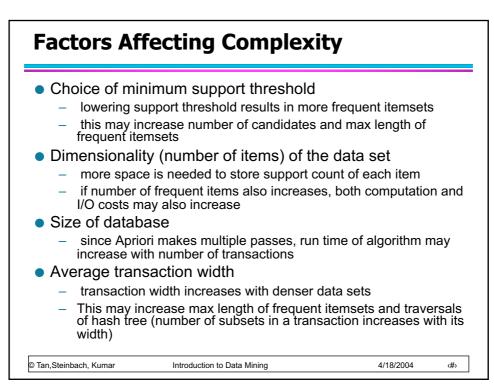


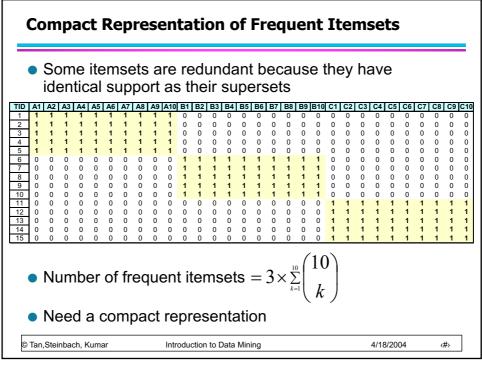
File Erfi	i each s	elp.			
Group 1	Support 0.277	t Confid 91.4	ence	Body 1.3	> Head [TERH DEPOSITS] AND [BUSINESS CREDIT CARD] AND [TELEBANKING] AND [DUSINESS SAVINGS]
1	8.164	86.4	-	1.3	> [SAUINGS] [TERH DEFOSITS] AND [ATH CARD] AND [DUSINESS CREDIT CARD] AND [TELEBANKING] AND [BUSINESS SAVINGS] > [SAUINGS]
1	0.104	85.7	-	1.9	[SAVINGS] AND [INTERNET BANKING] AND [LEASES] > [TELEDANKING]
1	0.138	84.2	-	1.2	[PERSONAL BANKING] AND [TERM DEPOSITS] AND [BUSINESS CREDIT CARD] AND [DUSINESS SAUINGS] =-> [SAUINGS]
1	8.251	82.9	-	1.2	[TERI DEPOSITS] AND [ATH CARD] AND [TELEBANKING] AND [BUSINESS SAUINGS] > [SAUINGS]
1	0.328	82.6	-	1.2	[ATH CARD] AND [BUSINESS CREDIT CARD] AND [TELEBANKING] AND [DUSINESS SAUINGS] =-> [SAUINGS]
1	8.242	82.4		1.2	[PERSONAL DANKING] AND [TERM DEPOSITS] AND [DUSINESS SAVINGS] ==> [SAVINGS]
1	8.631	81.1	-	1.2	[BUSINESS CREDIT CARD] AND [TELEBANKING] AND [BUSINESS SAVINGS] ==> [SAVINGS]
1	8.138	89.6	-	1.2	[ATH CARD] AND [BUSINESS CREDIT CARD] AND [TELEBANKING] AND [INTERNET BANKING] AND [BUSINESS SAUINGS] > [Sauing]
1	0.138	80.0	-	1.2	TERH DEPOSITS] AND [TEL > [SAVINGS]
1	0.458	79.1	-	1.2	[TERH DEPOSITS] AND [TELEBANKING] AND [BUSINESS SAVINGS] > [SAVINGS]
1	0.130	78.9	-	1.2	[PERSONAL BANKING] AND [BUSINESS CREDIT CARD] AND [TELEBANKING] AND [DUSINESS SAUINGS] > [SAUINGS]
1	8.346	78.4	-	1.2	[PERSONAL BANKING] AND [OUSINESS CREDIT CARD] AND [BUSINESS SAUINGS] > [SAUINGS]
1	1.037	77.9	-	1.1	TERH DEPOSITS] AND [ATH CARD] AND [BUSINESS CREDIT CARD] AND [TELEDANKING] AND [INTERNET BANKING] > [SAUING]
1	8.182	77.8	-	1.7	TERH DEPOSITS] AND [ATH CARD] AND [INTERNET DANKING] AND [BUSINESS SAUINGS] -> [DUSINESS CREDIT CARD]

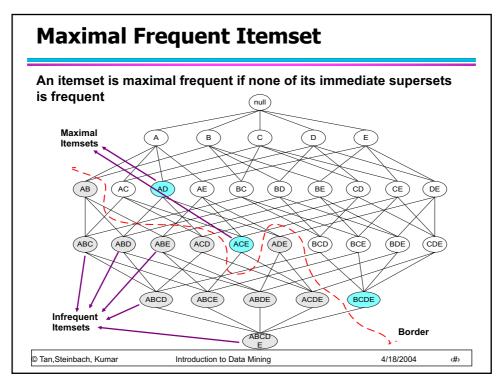
Table (6.1)				
	Table 6.1. Ex	ample of market bask	et transactions.	
	Customer ID	Transaction ID	Items Bought	
	1	0001	$\{a, d, e\}$	
	1	0024	$\substack{\{a,b,c,e\}\\\{a,b,d,e\}}$	
	2	0012	$\{a, b, d, e\}$	
	2	0031	$\{a,c,d,e\}$	
	3	0015	$\{b, c, e\}$	
	3	0022	$\{b, d, e\}$	
	4	0029	$\{c, d\}$	
	4	0040	$\{a, b, c\}$	
	5	0033	$\{a, d, e\}$	
	5	0038	$\{a, b, e\}$	
				Same -
				CT CON
C				
	upport?: e, (b,	,,		10201000
	2020-2021 Reg] .		
Ass.	56			

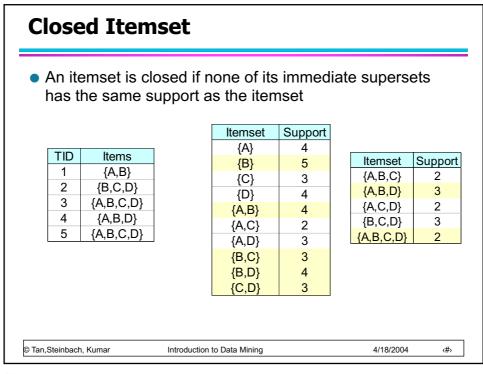
Table 6.2. Market basket transactions.					
Tra	nsaction ID	Items Bought			
	1	{Milk, Beer, Diapers}			
	2	{Bread, Butter, Milk}			
	3	{Milk, Diapers, Cookies}			
	4	{Bread, Butter, Cookies}			
	5	{Beer, Cookies, Diapers}			
	6	{Milk, Diapers, Bread, Butter}			
	7	{Bread, Butter, Diapers}			
	8	{Beer, Diapers}			
	9	{Milk, Diapers, Bread, Butter}			
	10	{Beer, Cookies}			
247 L.1 (M.1998-111)					
Max size of itemset, 2-itemsets with larger support					
Data Mining 2020-2	2021 Reg.	5 (SA2)	10-0		
Ass.	-		57		

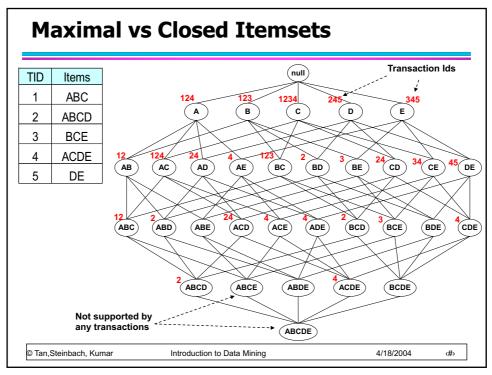


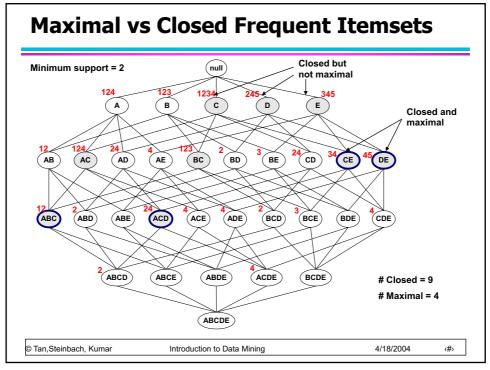


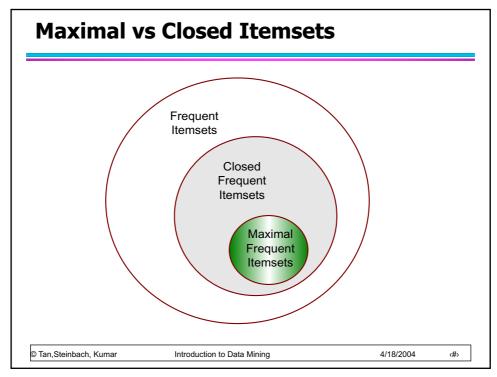


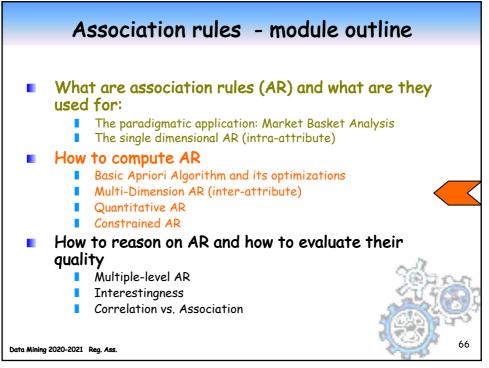




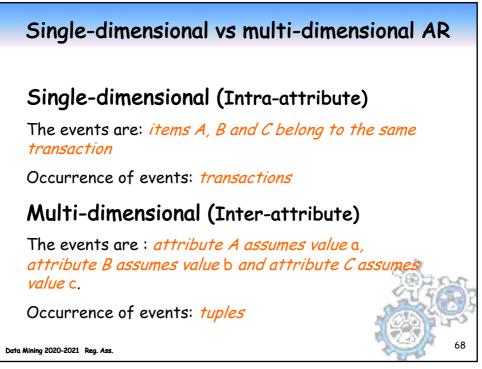


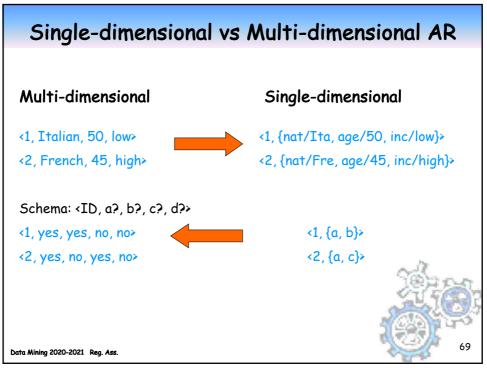


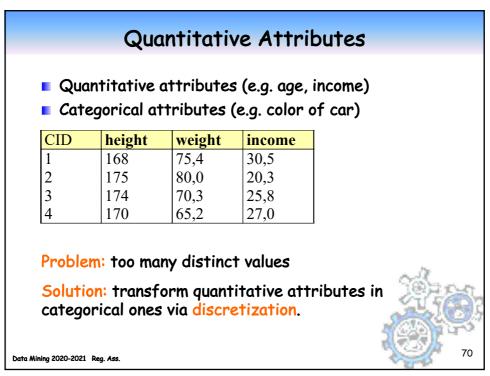


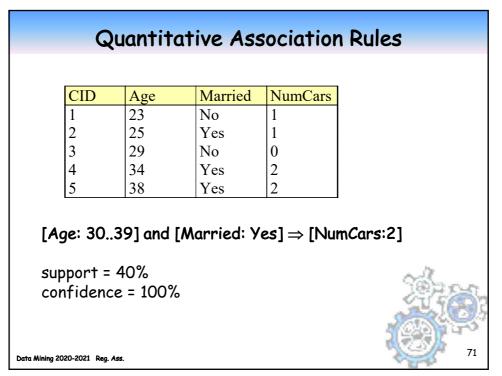


	Multidi	mens	ional AR	
Associations	s between valu	les of (different att	tributes :
CID	nationality	age	income]
1	Italian	50	low	1
2	French	40	high	
3	French	30	high	
4	Italian	50	medium	
5	Italian	45	high	
6	French	35	high	
RULES	•		•	-
	French ⇒ i nc	ome =	high [50% 1	00%1
•			J	The CONTRACT AND AND
-	n ⇒ nati	•		Tang Mar T Provide St
age = 50	\Rightarrow natio	onality	= Italian [33	%, 100%]
Data Mining 2020-2021 Reg. As	S.			67









Discretization of quantitative attributes

Solution: each value is replaced by the interval to which it belongs. height: 0-150cm, 151-170cm, 171-180cm, >180cm

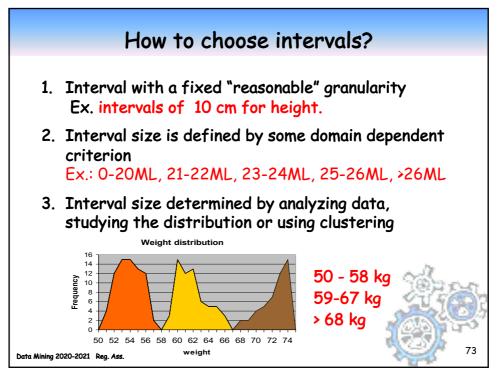
weight: 0-40kg, 41-60kg, 60-80kg, >80kg income: 0-10ML, 11-20ML, 20-25ML, 25-30ML, >30ML

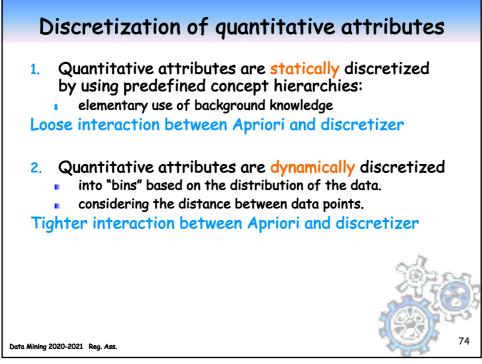
CID	height	weight	income
1	151-171	60-80	>30
2	171-180	60-80	20-25
3	171-180	60-80	25-30
4	151-170	60-80	25-30

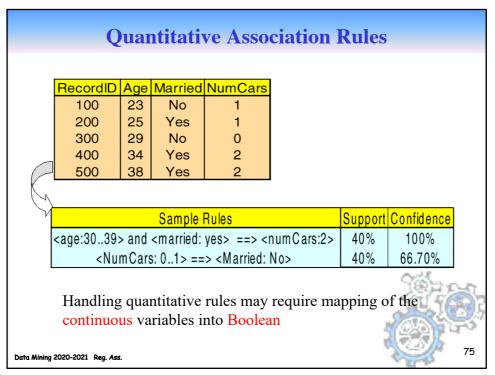
Problem: the discretization may be useless (see weight

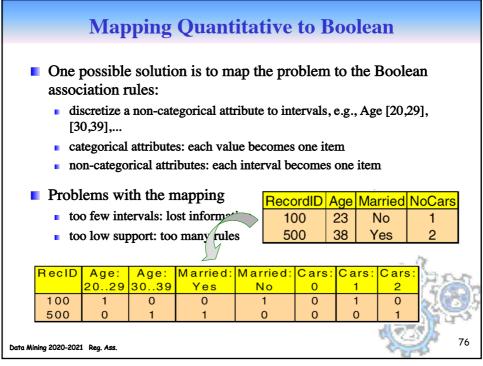
Data Mining 2020-2021 Reg. Ass.

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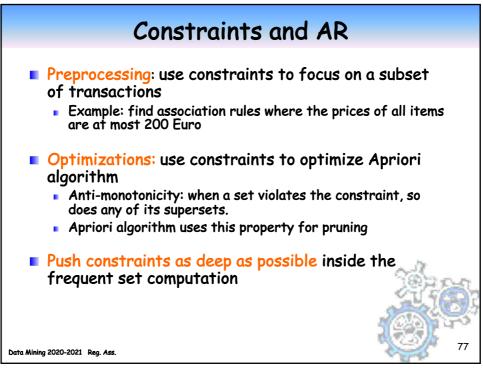


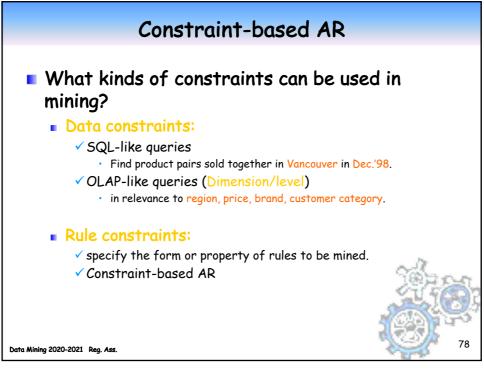




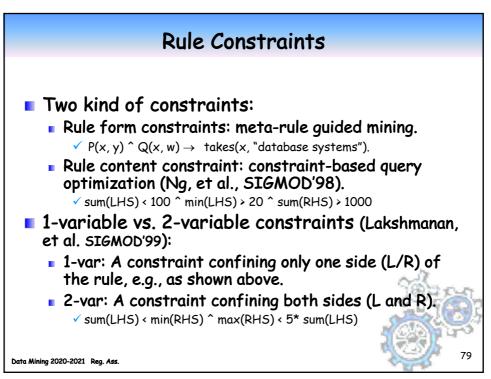


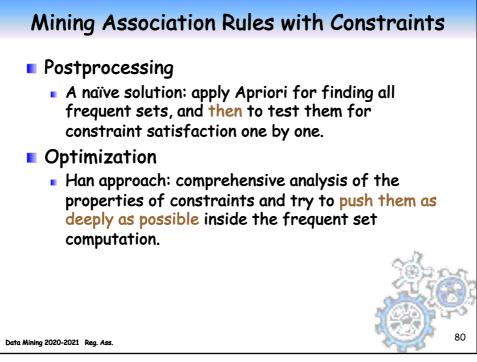




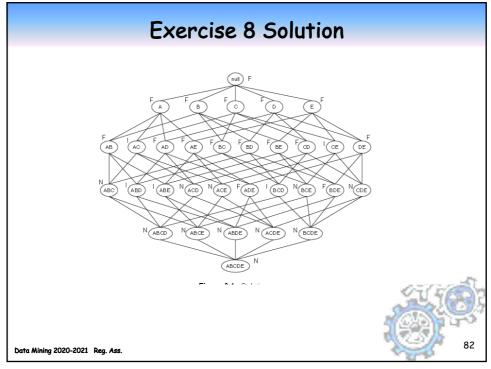


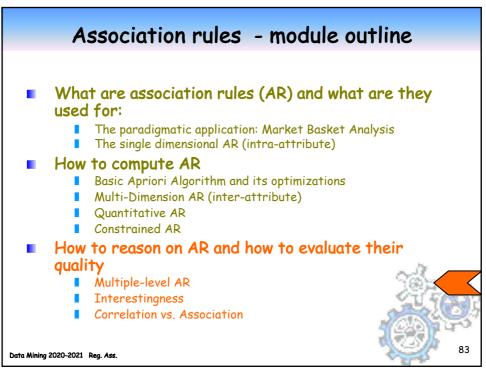


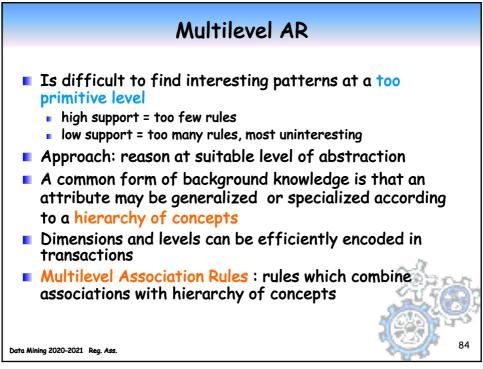


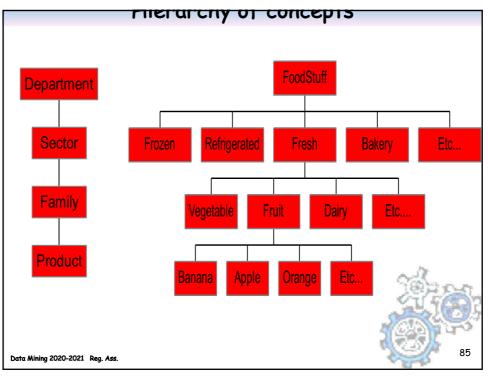


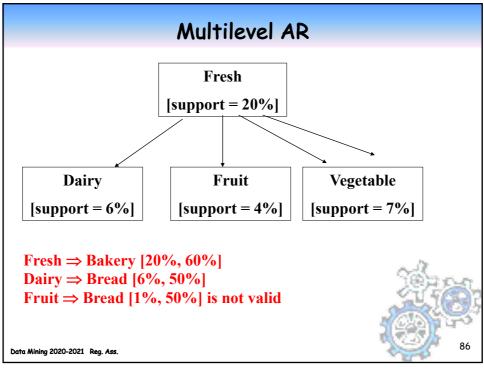
		rcise 6	
ТИК	Ne v.v. Example of the	anorpashormansaonor	10.
	Transaction ID	Items Bought	
	1	$\{a, b, d, e\}$	
	2	$\{b, c, d\}$	
	3	$\{a, b, d, e\}$	
	4	$\{a, c, d, e\}$	
	5	$\{b, c, d, e\}$	
	6	$\{b, d, e\}$	
	7	$\{c,d\}$	
	8	$\{a, b, c\}$	
	9	$ \{c, d\} \{a, b, c\} \{a, d, e\} $	
	10	$\{b,d\}$	
		·	A BOARD



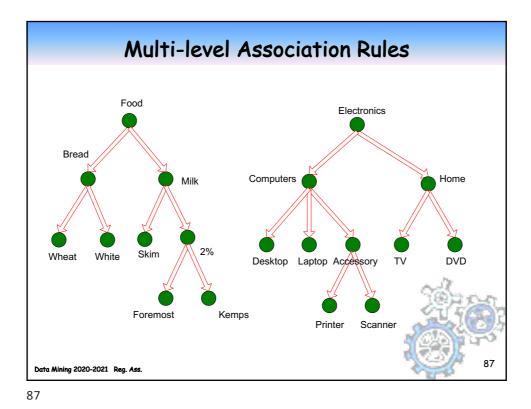


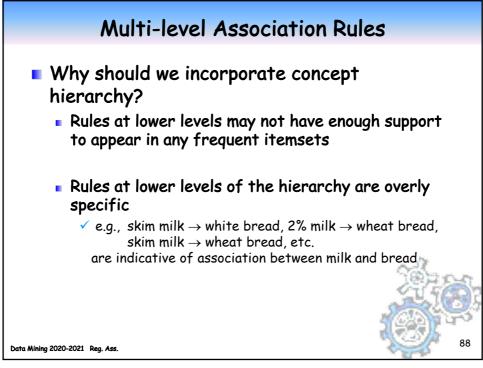




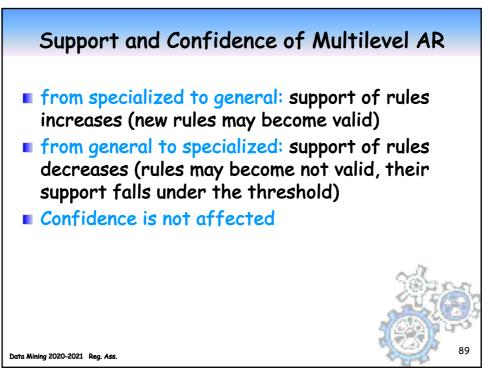


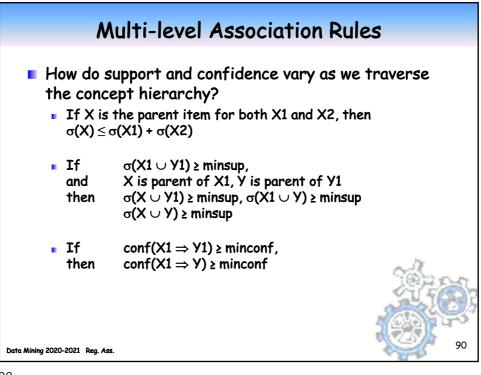


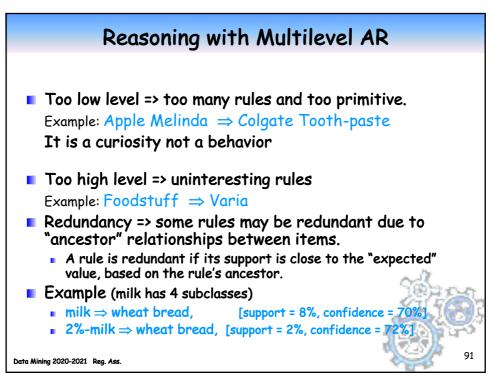


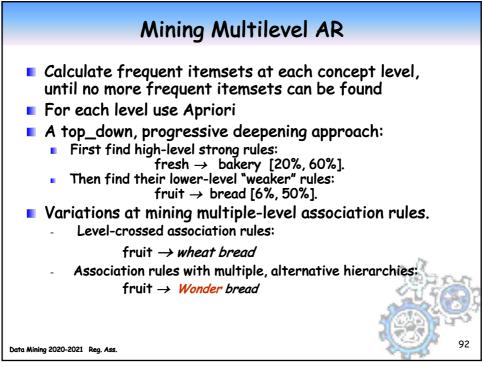


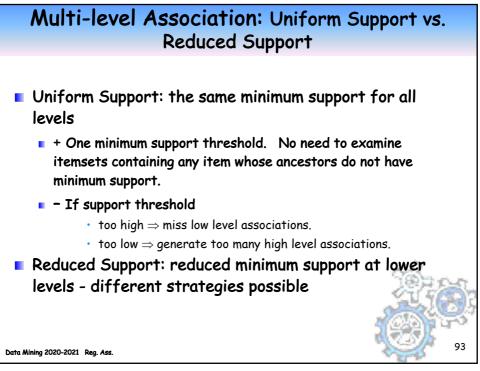


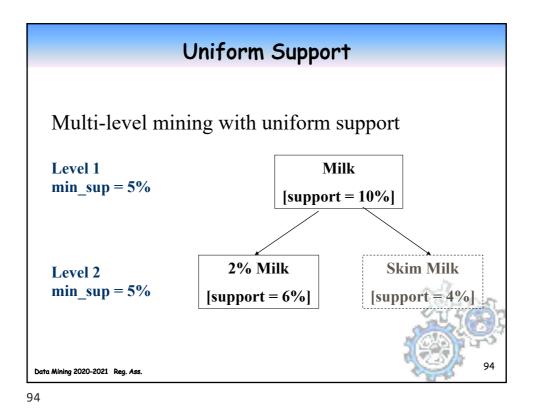


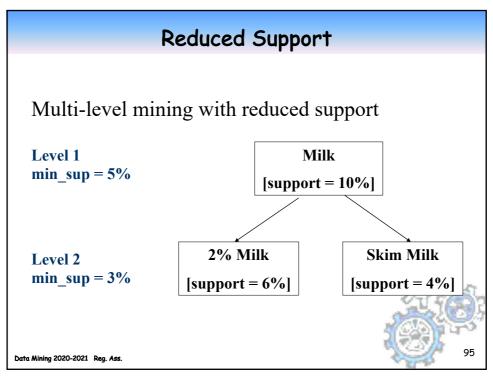


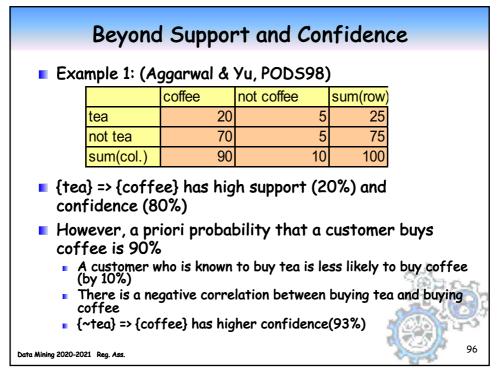


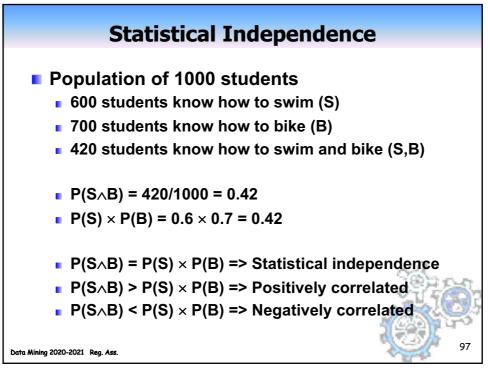


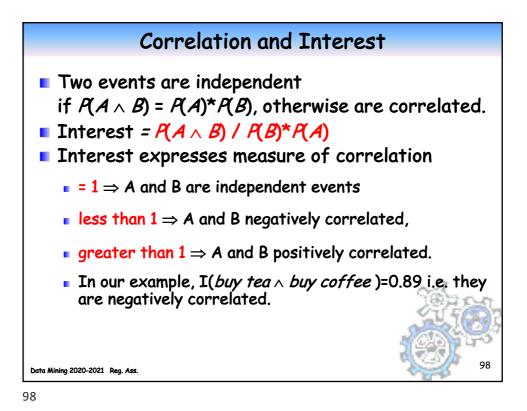


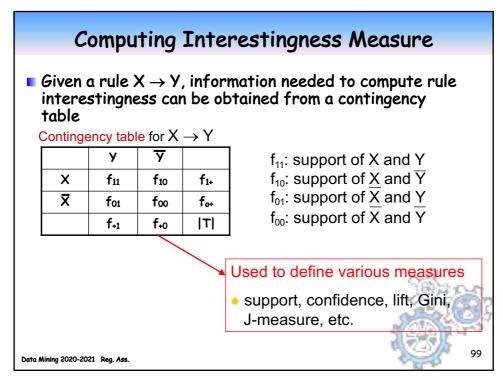


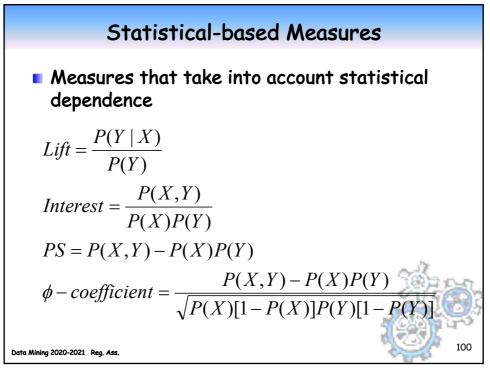


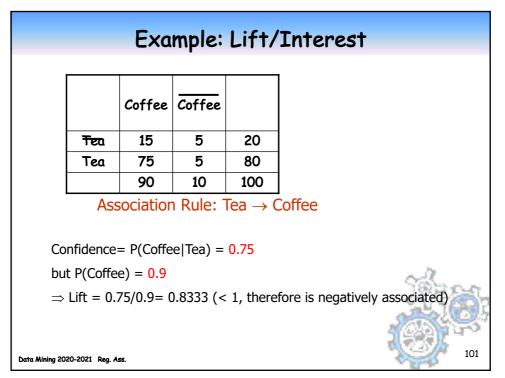


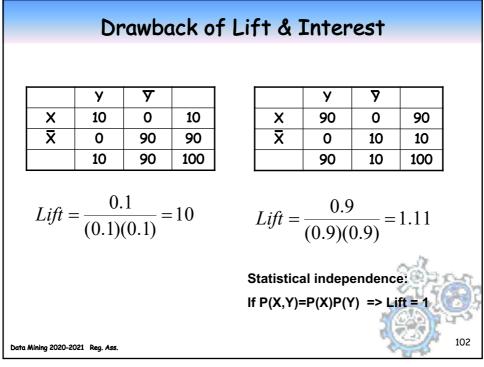




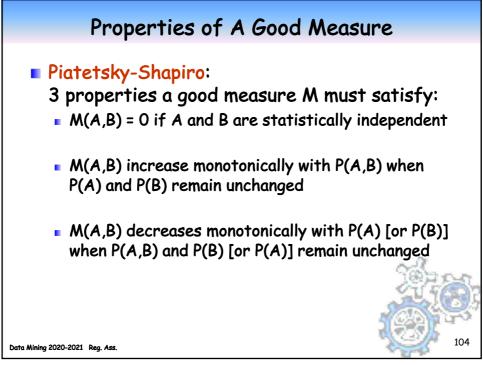




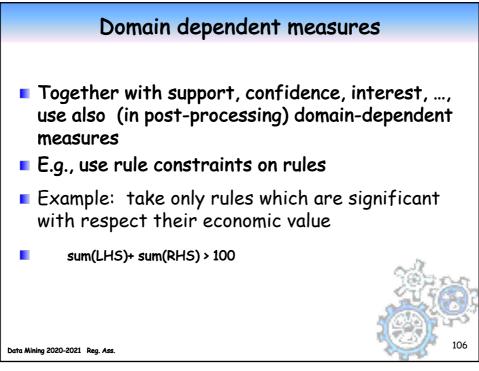


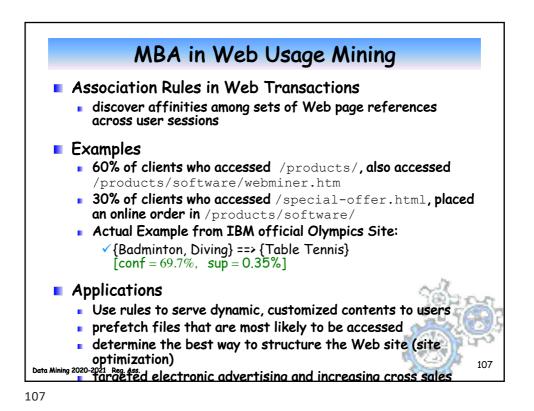


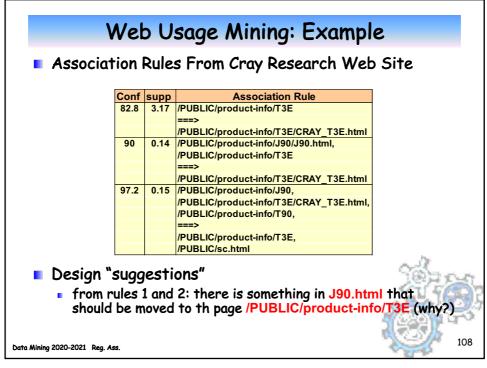
	#	Measure	Formula
	#		$\frac{P(A,B)-P(A)P(B)}{P(A,B)-P(A)P(B)}$
There are lots of	1	ϕ -coefficient	$\sqrt{P(A)P(B)(1-P(A))(1-P(B))}$
measures proposed	2	Goodman-Kruskal's (λ)	$\frac{\sum_{j=1}^{j} \max_{k} P(A_{j}, B_{k}) + \sum_{k=1}^{j} \max_{j=1} P(A_{j}, B_{k}) - \max_{j=1} P(A_{j}) - \max_{k} P(B_{k})}{2 - \max_{i} P(A_{i}) - \max_{k} P(B_{k})}$
in the literature	3	Odds ratio (α)	$\frac{P(A,B)P(\overline{A},\overline{B})}{P(A,\overline{B})P(\overline{A},B)}$
	4	Yule's Q	$\frac{P(A,B)P(\overline{AB}) - P(A,\overline{B})P(\overline{A},B)}{P(A,B)P(\overline{AB}) + P(A,\overline{B})P(\overline{A},B)} = \frac{\alpha - 1}{\alpha + 1}$
	5	Yule's Y	$\frac{\sqrt{P(A,B)P(AB)} - \sqrt{P(A,B)P(\overline{A}B)}}{\sqrt{P(A,B)P(\overline{A}B)} + \sqrt{P(A,\overline{B})P(\overline{A},B)}} = \frac{\sqrt{\alpha} - 1}{\sqrt{\alpha} + 1}$
Some measures are good for certain	6	Kappa (ĸ)	$\frac{\nabla P(A,B)P(AB) + \nabla P(A,B)P(A,B)}{1 - P(A)P(B) - P(A)P(B)} = \frac{\nabla P(A,B)}{1 - P(A)P(B) - P(A)P(B)}$ $\frac{\sum_{i} \sum_{j} P(A_{i},B_{j}) \log \frac{P(A_{i},B_{j})}{P(A_{i})P(B_{j})}$
applications, but not	7	Mutual Information (M)	$\min(-\sum_{i} P(A_i) \log P(A_i), -\sum_{j} P(B_j) \log P(B_j))$
for others	8	J-Measure (J)	$\max\Big(P(A,B)\log(\frac{P(B A)}{P(B)}) + P(A\overline{B})\log(\frac{P(\overline{B} A)}{P(\overline{B})}),$
			$P(A, B) \log(\frac{P(A B)}{P(A)}) + P(\overline{A}B) \log(\frac{P(\overline{A} B)}{P(A)})$
	9	Gini index (G)	$\max \left(P(A)[P(B A)^3 + P(\overline{B} A)^2] + P(\overline{A})[P(B \overline{A})^3 + P(\overline{B} \overline{A})^2] \right)$
What criteria should			$-P(B)^2 - P(\overline{B})^2$,
we use to determine			$P(B)[P(A B)^{2} + P(\overline{A} B)^{2}] + P(\overline{B})[P(A \overline{B})^{2} + P(\overline{A} \overline{B})^{2}]$
whether a measure			$-P(A)^3 - P(\overline{A})^3$
is good or bad?	10	Support (s)	P(A,B)
-	11	Confidence (c)	$\max(P(B A), P(A B))$
	12	Laplace (L)	$\max\left(\frac{NP(A,B)+1}{NP(A)+2},\frac{NP(A,B)+1}{NP(B)+2}\right)$
What about Apriori-	13	Conviction (V)	$\max\left(\frac{P(A)P(\overline{B})}{P(A\overline{B})}, \frac{P(B)P(\overline{A})}{P(B\overline{A})}\right)$
style support based	14	Interest (I)	$\frac{P(A,B)}{P(A)P(B)}$
pruning? How does	15	cosine (IS)	$\frac{\mathbf{\hat{P}}(\mathbf{A},\mathbf{B})}{\sqrt{P(\mathbf{A})P(\mathbf{B})}}$
it affect these	16	Piatetsky-Shapiro's (PS)	P(A,B) - P(A)P(B)
measures?	17	Certainty factor (F)	$\max\left(rac{P(B A)-P(B)}{1-P(B)},rac{P(A B)-P(A)}{1-P(A)} ight)$
	18	Added Value (AV)	$\max(P(B A) - P(B), P(A B) - P(A))$
	19	Collective strength (S)	$\frac{\underline{P(A,B)} + \underline{P(\overline{AB})}}{\underline{P(A)P(B)} + \underline{P(\overline{A})P(\overline{B})}} \times \frac{1 - \underline{P(A)P(B)} - \underline{P(\overline{A})P(\overline{B})}}{1 - \underline{P(A,B)} - \underline{P(\overline{AB})}}$
	20	Jaccard (ζ)	$\frac{P(A,B)}{P(A)+P(B)-P(A,B)}$ 103
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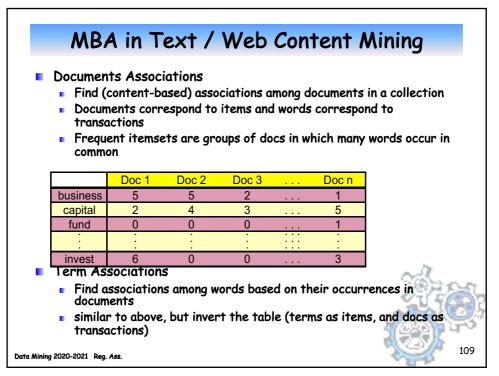


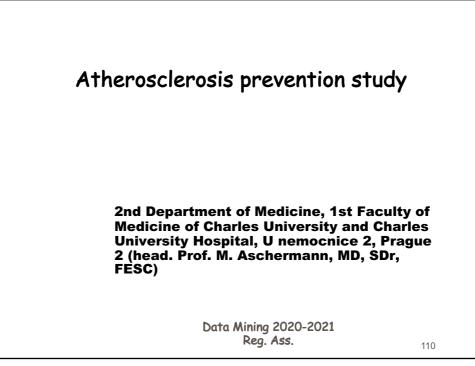
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#	φ	λ	α	Q	Y	ĸ	M	J	G	8	с	L	V	I	IS	PS	F	AV	S	ς	K
E1	1	1	3	3	3	1	2	2	1	3	5	5	4	6	2	2	4	6	1	2	5
$\mathbf{E2}$	2	2	1	1	1	2	1	3	2	2	1	1	1	8	3	5	1	8	2	3	6
E3	3	3	4	4	4	3	3	8	7	1	4	4	6	10	1	8	6	10	3	1	10
E4	4	7	2	2	2	5	4	1	3	6	2	2	2	4	4	1	2	3	4	5	1
E5 Ee	5	4	8	8	8 7	4 7	7	5	4	7	9 8	9	9 7	3 2	6 8	3	9	4	5	6 8	3 2
E6 E7	5	5	7 9	9	7 9	7 6	6 8	4	5	9 4	8 7	8	7 8	25	8 5	4	8	2 5	6	8	2
E4 E8	8	9	10	10	9 10	0 8	10	10	8	4	10	10	0 10	9 9	5 7	7		9 9	8	4	4 9
E9	9	9	5	5	5	9	9	7	9	8	3	3	3	7	9	9	3	7	9	9	8
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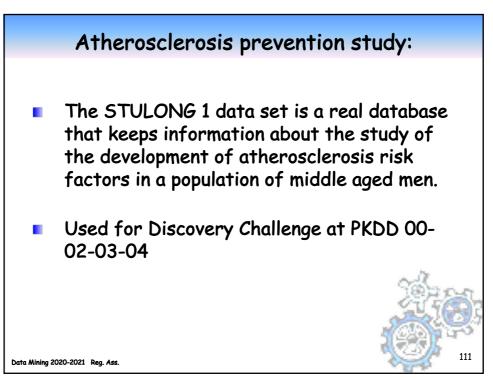


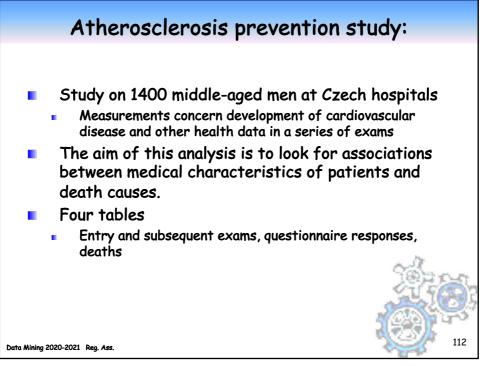






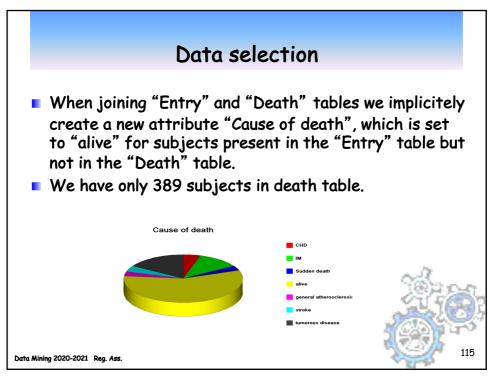






Data	from Entry and E	xams
General characteristics	Examinations	habits
Marital status	Chest pain	Alcohol
Transport to a job	Breathlesness	Liquors
Physical activity in a job	Cholesterol	Beer 10
Activity after a job	Urine	Beer 12
Education	Subscapular	Wine
Responsibility	Triceps	Smoking
Age		Former smoker
Weight		Duration of smoking
Height		Tea
-		Sugar
		Coffee Coffee

Inei	input data	
DEATH CAUSE	PATIENTS	%
myocardial infarction	80	20.6
coronary heart disease	33	8.5
stroke	30	7.7
other causes	79	20.3
sudden death	23	5.9
unknown	8	2.0
tumorous disease	114	29.3
general atherosclerosis	22	5.7
TOTAL	389	100.0
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	General Examinations Habits								
Patient		Examinati	0115	nabits	Cause of				
	Activity after work	Education	Chest pain		Alcohol		death		
1	moderate activity	university	not present		no		Stroke		
2	great activity		not ischaemic		occasionally		myocardi infarction		
3	he mainly sits		other pains		regularly		tumorous disease		
							alive		
389	he mainly sits		other pains		regularly		tumorous disease		

