

Data Preparation

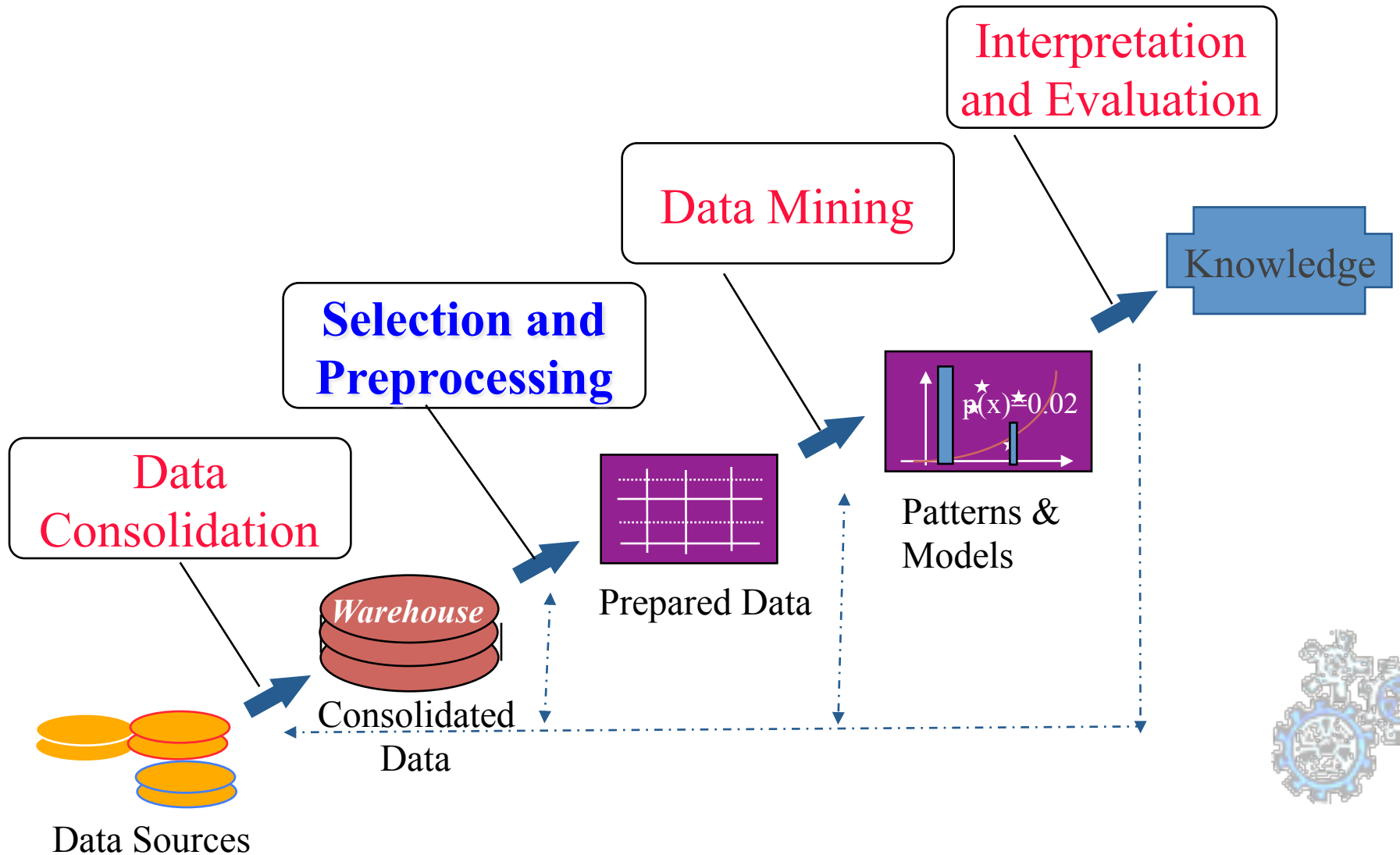
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KDD Process



Data understanding vs Data preparation

Data understanding provides general information about the data like

- The existence of **missing values**
- The existence of **outliers**
- the character of attributes
- **dependencies** between attributes.

Data preparation uses this information to

- select attributes,
- reduce the dimension of the data set,
- select records,
- treat missing values,
- treat outliers,
- integrate, unify and transform data
- improve data quality



Data Reduction

Reducing the amount of data

- Reduce the number of **records**
 - Data Sampling
 - Clustering
- Reduce the number of **columns** (attributes)
 - Select a subset of attributes
 - Generate a new (a smaller) set of attributes



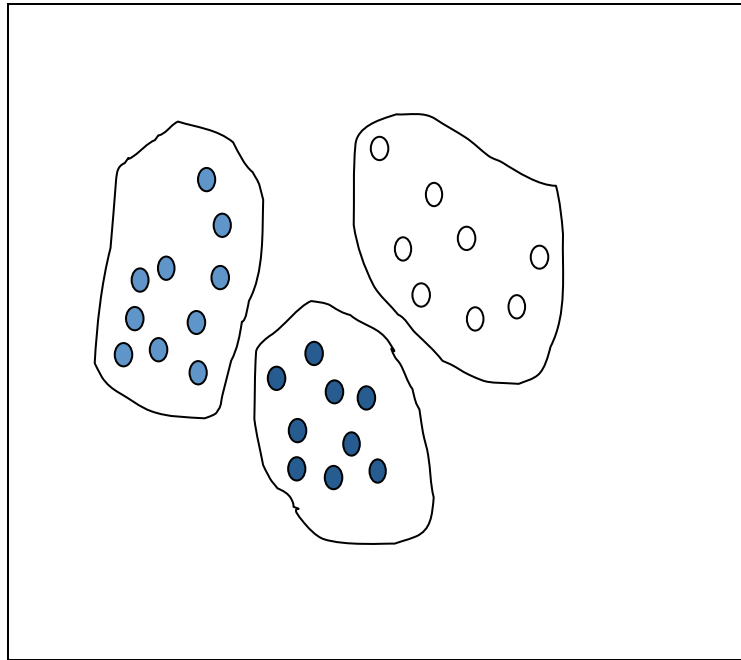
Sampling

- Improve the execution time of data mining algorithms
- **Problem:** how to select a subset of **representative** data?
 - **Random sampling:** it can generate problems due to the possible peaks in the data
 - **Stratified sampling:**
 - Approximation of the percentage of each class
 - Suitable for distribution with peaks: each peak is a **layer**

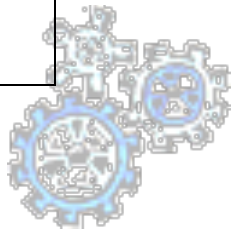
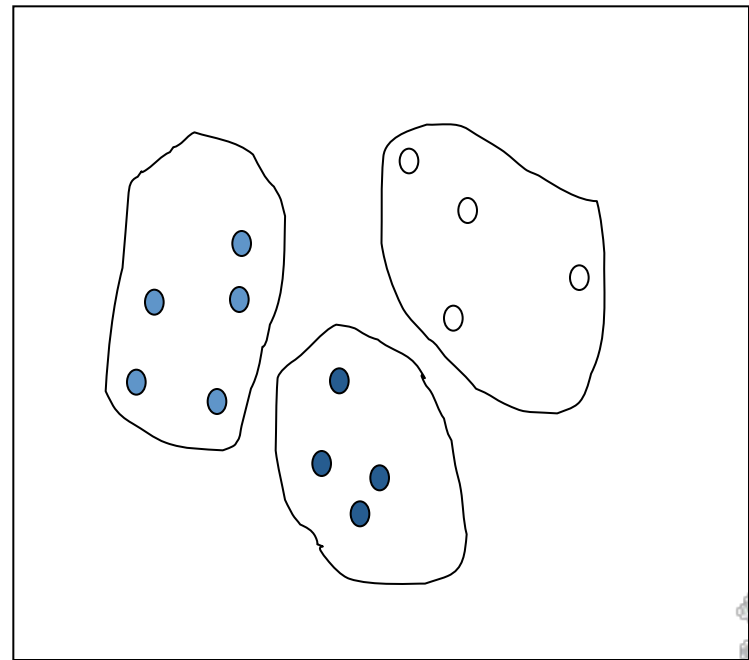


Stratified Sampling

Raw Data



Cluster/Stratified Sample



Reduction of Dimensionality

- **Selection of a subset of attributes** that is as small as possible and sufficient for the data analysis.
 - removing (more or less) **irrelevant** features
 - removing **redundant** features.



Removing irrelevant/redundant features

- For **removing irrelevant features**, a **performance measure** is needed that indicates how well a feature or subset of features performs w.r.t. the considered data analysis task
- For removing **redundant features**, either a **performance measure** for subsets of features or a **correlation measure** is needed.



Reduction of Dimensionality

Manual

- After analyzing the **significance** and/or **correlation** with other attributes

Automatic: Selecting the top-ranked features

- Incremental Selection of the “best” attributes
- “Best” = with respect to a specific measure of statistical significance (e.g.: information gain).



Data Cleaning

- How to handle anomalous values
- How to handle outliers
- Data Transformations



Anomalous Values

- **Missing values**
 - NULL, ?
- **Unknown Values**
 - Values without a real meaning
- **Not Valid Values**
 - Values not significant



Manage Missing Values

1. Elimination of records
2. Substitution of values

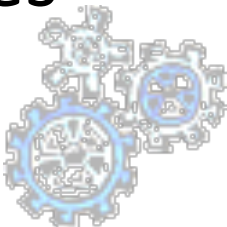
Note: it can influence the original distribution of numerical values

- Use mean/median/mode
- Estimate missing values **using the probability distribution** of existing values
- Data Segmentation and using mean/mode/median of each **segment**
- Data Segmentation and using **the probability distribution within the segment**
- Build a model of **classification/regression** for computing missing values



Data Transformation: Motivations

- Data with errors and incomplete
- Data not adequately distributed
 - Strong asymmetry in the data
 - Many peaks
- Data transformation can reduce these issues



Goals

- Define a transformation T on the attribute X :

$$Y = T(X)$$

such that :

- Y preserve the **relevant** information of X
- Y eliminates at least one of the problems of X
- Y is more **useful** of X



Goals

- **Main goals:**
 - stabilize the variances
 - normalize the distributions
 - Make linear relationships among variables
- **Secondary goals:**
 - simplify the elaboration of data containing features you do not like
 - represent data in a scale considered more suitable



Why linear correlation, normal distributions, etc?

- Many statistical methods require linear correlations, normal distributions, the absence of outliers
- Many data mining algorithms have the ability to automatically treat **non-linearity** and **non-normality**
 - The algorithms work still better if such problems are treated



Normalizations

- min-max normalization

$$v' = \frac{v - \mathit{min}_A}{\mathit{max}_A - \mathit{min}_A} (\mathit{new_max}_A - \mathit{new_min}_A) + \mathit{new_min}_A$$

- z-score normalization

$$v' = \frac{v - \mathit{mean}_A}{\mathit{stand_dev}_A}$$

- normalization by decimal scaling

$$v' = \frac{v}{10^j} \quad \text{Where } j \text{ is the smallest integer such that } \text{Max}(|v'|) < 1$$



Methods

- Exponential transformation

$$T_p(x) = \begin{cases} ax^p + b & (p \neq 0) \\ c \log x + d & (p = 0) \end{cases}$$

- with a, b, c, d and p real values
 - Preserve the order
 - Preserve some basic statistics
 - They are continuous functions
 - They are derivable
 - They are specified by simple functions



Better Interpretation

- Linear Transformation

$$1\text{€} = 1936.27 \text{ Lit.}$$

$$- p=1, a= 1936.27, b =0$$

$$^{\circ}\text{C} = 5/9(^{\circ}\text{F} - 32)$$

$$- p = 1, a = 5/9, b = -160/9$$

$$T_p(x) = \begin{cases} ax^p + b & (p \neq 0) \\ c \log x + d & (p = 0) \end{cases}$$



Stabilizing the Variance

- **Logarithmic Transformation**

$$T(x) = c \log x + d$$

- Applicable to positive values
- Makes homogenous the variance in log-normal distributions
 - E.g.: normalize seasonal peaks



Logarithmic Transformation: Example

<i>Bar</i>	<i>Birra</i>	<i>Ricavo</i>
A	Bud	20
A	Becks	10000
C	Bud	300
D	Bud	400
D	Becks	5
E	Becks	120
E	Bud	120
F	Bud	11000
G	Bud	1300
H	Bud	3200
H	Becks	1000
I	Bud	135

2300 Mean
2883,3333 Scarto medio assoluto
3939,8598 Standard Deviation
5 Min
120 1° Quartile
350 Median
1775 2° Quartile
11000 Max

Data are sparse!!!



Logarithmic Transformation: Example

<i>Bar</i>	<i>Birra</i>	<i>Ricavo (log)</i>
A	Bud	1,301029996
A	Becks	4
C	Bud	2,477121255
D	Bud	2,602059991
D	Becks	0,698970004
E	Becks	2,079181246
E	Bud	2,079181246
F	Bud	4,041392685
G	Bud	3,113943352
H	Bud	3,505149978
H	Becks	3
I	Bud	2,130333768

Media	2,585697
Scarto medio assoluto	0,791394
Deviazione standard	1,016144
Min	0,69897
Primo Quartile	2,079181
Mediana	2,539591
Secondo Quartile	3,211745
Max	4,041393



Stabilizing the Variance

$$T(x) = ax^p + b$$

- **Square-root Transformation**
- $p = 1/c$, c integer number
 - To make homogenous the variance of particular distributions e.g., Poisson Distribution
- **Reciprocal Transformation**
 - $p < 0$
 - Suitable for analyzing time series, when the variance increases too much wrt the mean



Discretization: Advantages

- Hard to understand the optimal discretization
 - We should need the real data distribution
- Original values can be **continuous** and **sparse**
- Discretized data can be **simple** to be interpreted
- Data distribution after discretization can have a **Normal shape**
- Discretized data can be too much **sparse yet**
 - Elimination of the attribute



Unsupervised Discretization

- Characteristics:
 - No label for the instances
 - The number of classes is unknown
- Techniques of *binning*:
 - **Natural binning** → Intervals with the same width
 - **Equal Frequency binning** → Intervals with the same frequency
 - **Statistical binning** → Use statistical information (Mean, variance, Quartile)



Discretization of quantitative attributes

- **Solution:** each value is replaced by the interval to which it belongs.
 - **height:** 0-150cm, 151-170cm, 171-180cm, >180c
 - **weight:** 0-40kg, 41-60kg, 60-80kg, >80kg
 - **income:** 0-10ML, 11-20ML, 20-25ML, 25-30ML, >30ML

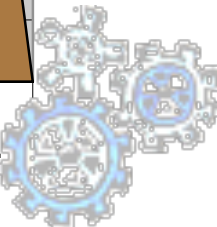
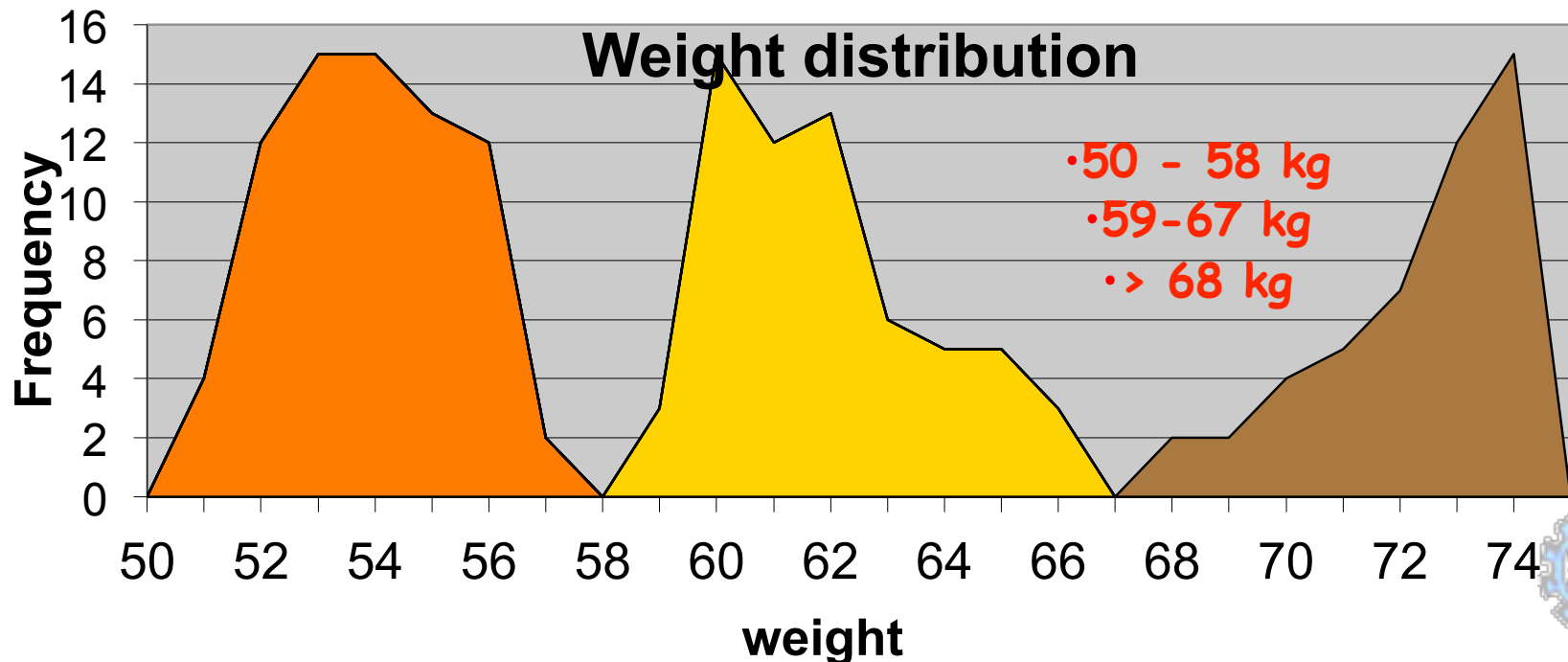
CID	height	weight	income
1	151-171	60-80	>30
2	171-180	60-80	20-25
3	171-180	60-80	25-30
4	151-170	60-80	25-30

- **Problem:** the discretization may be useless (see **weight**).



How to choose intervals?

1. Interval with a fixed “reasonable” granularity
Ex. **intervals of 10 cm for height.**
2. Interval size is defined by some domain dependent criterion
Ex.: **0-20ML, 21-22ML, 23-24ML, 25-26ML, >26ML**
3. Interval size determined by analyzing data, studying the distribution or using clustering



Natural Binning

- Simple
- Sort of values, subdivision of the range of values in k parts with the same size

$$\delta = \frac{x_{\max} - x_{\min}}{k}$$

- Element x_j belongs to the class i if

$$x_j \in [x_{\min} + i\delta, x_{\min} + (i+1)\delta)$$

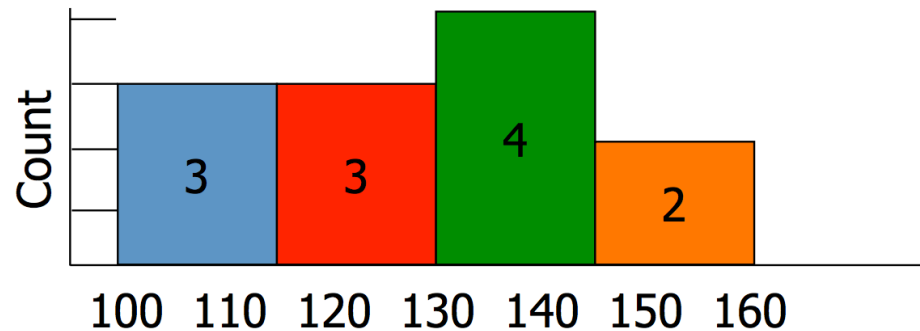
- It can generate distribution very unbalanced



Example

Bar	Beer	Price
A	Bud	100
A	Becks	120
C	Bud	110
D	Bud	130
D	Becks	150
E	Becks	140
E	Bud	120
F	Bud	110
G	Bud	130
H	Bud	125
H	Becks	160
I	Bud	135

- $\delta = (160 - 100) / 4 = 15$
- class 1: [100, 115)
- class 2: [115, 130)
- class 3: [130, 145)
- class 4: [145, 160]



Equal Frequency Binning

- Sort and count the elements, definition of k intervals of f , where:

$$f = \frac{N}{k}$$

(N = number of elements of the sample)

- The element x_i belongs to the class j if

$$j \times f \leq i < (j+1) \times f$$

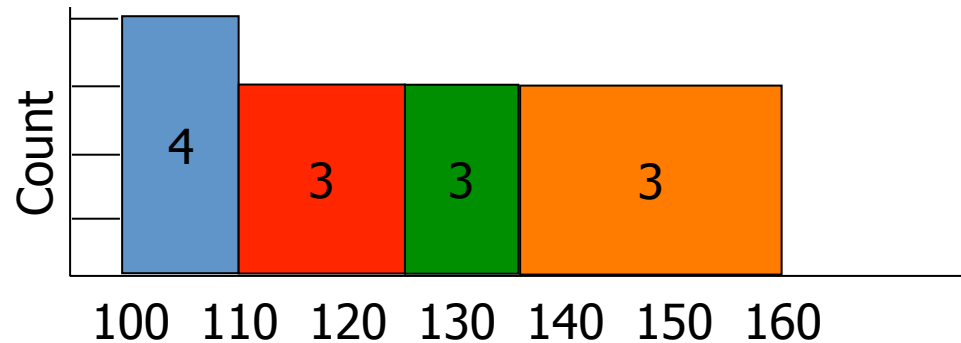
- It is not always suitable for highlighting interesting correlations



Example

Bar	Beer	Price
A	Bud	100
A	Becks	120
C	Bud	110
D	Bud	130
D	Becks	150
E	Becks	140
E	Bud	120
F	Bud	110
G	Bud	130
H	Bud	125
H	Becks	160
I	Bud	135

- $f = 12/4 = 3$
- class 1: {100,110,110}
- class 2: {120,120,125}
- class 3: {130,130,135}
- class 4: {140,150,160}



How many classes?

- If too few
⇒ Loss of information on the distribution
- If too many
⇒ Dispersion of values and does not show the form of distribution
- The optimal number of classes is function of N elements (Sturges, 1929)

$$C = 1 + \frac{10}{3} \log_{10}(N)$$

- The optimal width of the classes depends on the variance and the number of data (Scott, 1979)

$$h = \frac{3,5 \cdot s}{\sqrt{N}}$$



Supervised Discretization

- **Characteristics:**
 - The discretization has a quantifiable goal
 - The number of classes is known
- **Techniques:**
 - ChiMerge
 - discretization based on Entropy
 - discretization based on percentiles



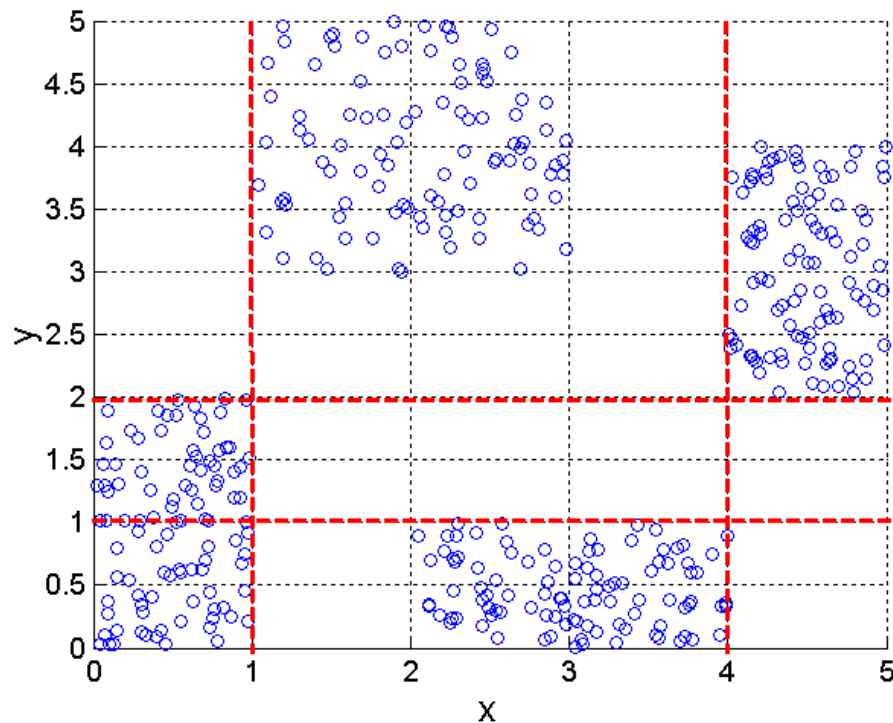
Supervised Discretization: ChiMerge

- Bottom-up Process:
 - Initially each value corresponds to an interval
 - Adjacent Intervals are iteratively merged if similar
 - The similarity is measured on the bases of the target attribute, measuring how much the two intervals are “different”.

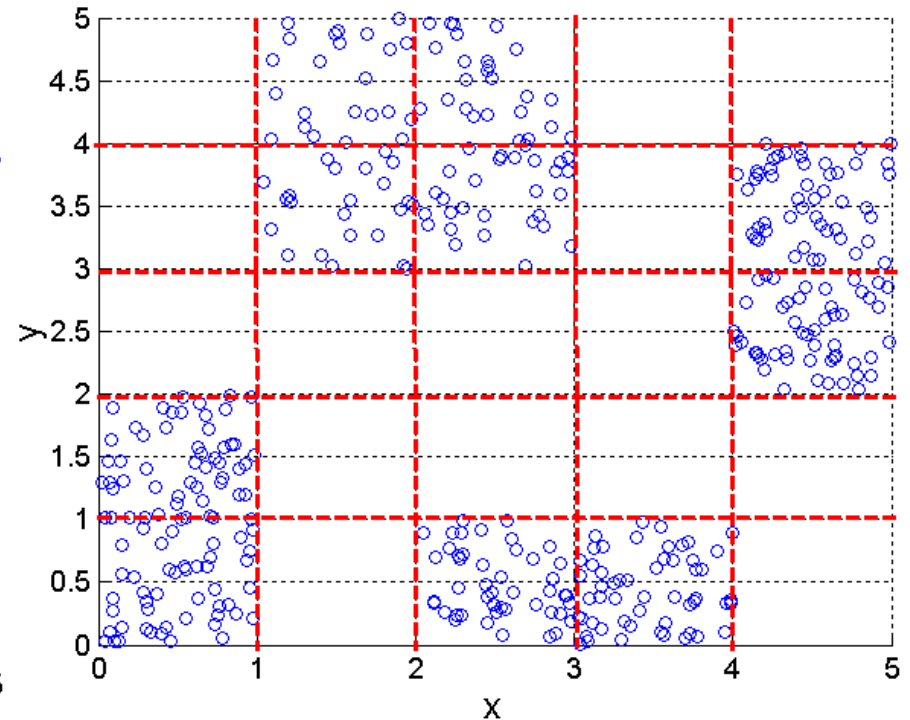


Entropy based approach

- Minimizes the entropy



3 categories for both x and y



5 categories for both x and y



Similarity



Similarity and Dissimilarity

- **Similarity**
 - Numerical measure of how alike two data objects are.
 - Is higher when objects are more alike.
 - Often falls in the range $[0,1]$
- **Dissimilarity**
 - Numerical measure of how different are two data objects
 - Lower when objects are more alike
 - Minimum dissimilarity is often 0
 - Upper limit varies
- **Proximity refers to a similarity or dissimilarity**



Similarity/Dissimilarity for ONE Attribute

p and q are the attribute values for two data objects.

Attribute Type	Dissimilarity	Similarity
Nominal	$d = \begin{cases} 0 & \text{if } p = q \\ 1 & \text{if } p \neq q \end{cases}$	$s = \begin{cases} 1 & \text{if } p = q \\ 0 & \text{if } p \neq q \end{cases}$
Ordinal	$d = \frac{ p-q }{n-1}$ <p>(values mapped to integers 0 to $n-1$, where n is the number of values)</p>	$s = 1 - \frac{ p-q }{n-1}$
Interval or Ratio	$d = p - q $	$s = -d, s = \frac{1}{1+d} \text{ or } s = 1 - \frac{d - \min_d}{\max_d - \min_d}$

Table 5.1. Similarity and dissimilarity for simple attributes



Many attributes: Euclidean Distance

- Euclidean Distance

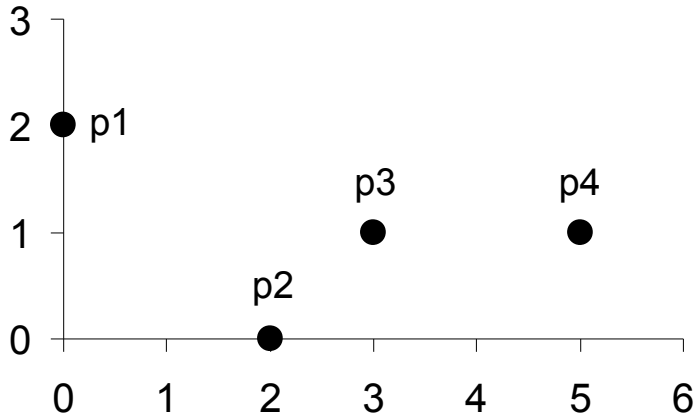
$$\mathit{dist} = \sqrt{\sum_{k=1}^n (p_k - q_k)^2}$$

Where n is the number of dimensions (attributes) and p_k and q_k are, respectively, the value of k^{th} attributes (components) or data objects p and q .

- Standardization is necessary, if scales differ.



Euclidean Distance



point	x	y
p1	0	2
p2	2	0
p3	3	1
p4	5	1

	p1	p2	p3	p4
p1	0	2.828	3.162	5.099
p2	2.828	0	1.414	3.162
p3	3.162	1.414	0	2
p4	5.099	3.162	2	0

Distance Matrix



Minkowski Distance

- Minkowski Distance is a generalization of Euclidean Distance

$$\mathit{dist} = \left(\sum_{k=1}^n |p_k - q_k|^r \right)^{\frac{1}{r}}$$

Where r is a parameter, n is the number of dimensions (attributes) and p_k and q_k are, respectively, the k_{th} attributes (components) or data objects p and q .



Minkowski Distance: Examples

- $r = 1$. City block (Manhattan, taxicab, L_1 norm) distance.
 - A common example of this is the Hamming distance, which is just the number of bits that are different between two binary vectors
- $r = 2$. Euclidean distance
- $r \rightarrow \infty$. “supremum” (L_{\max} norm, L_{∞} norm) distance.
 - This is the maximum difference between any component of the vectors
- Do not confuse r with n , i.e., all these distances are defined for all numbers of dimensions.



Minkowski Distance

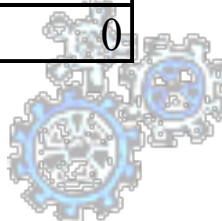
point	x	y
p1	0	2
p2	2	0
p3	3	1
p4	5	1

L1	p1	p2	p3	p4
p1	0	4	4	6
p2	4	0	2	4
p3	4	2	0	2
p4	6	4	2	0

L2	p1	p2	p3	p4
p1	0	2.828	3.162	5.099
p2	2.828	0	1.414	3.162
p3	3.162	1.414	0	2
p4	5.099	3.162	2	0

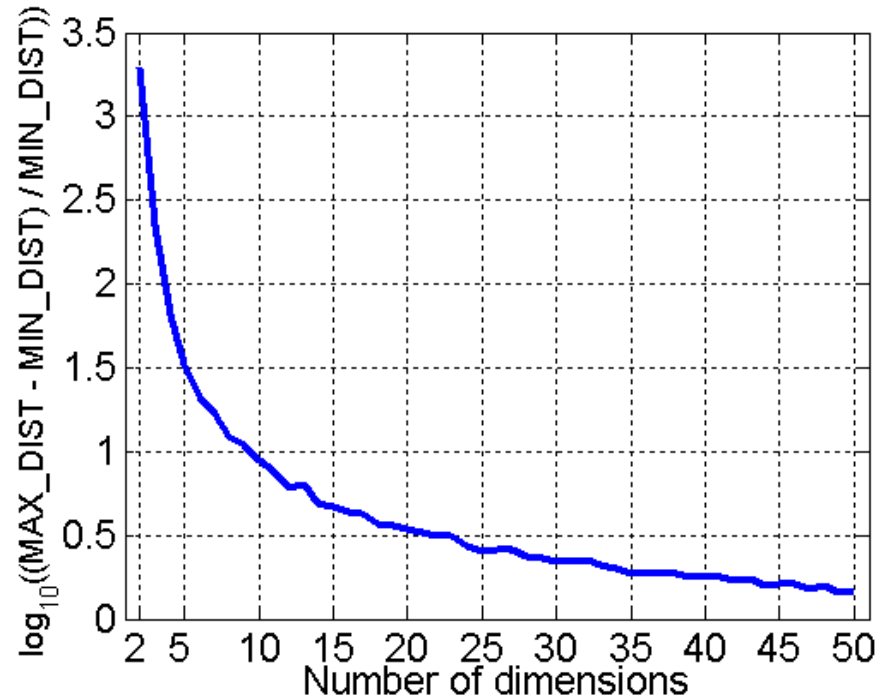
L ∞	p1	p2	p3	p4
p1	0	2	3	5
p2	2	0	1	3
p3	3	1	0	2
p4	5	3	2	0

Distance Matrix



Curse of Dimensionality

- When dimensionality increases, data becomes increasingly sparse in the space that it occupies
- Definitions of density and distance between points, which is critical for clustering and outlier detection, become less meaningful



- Randomly generate 500 points
- Compute difference between max and min distance between any pair of points



Common Properties of a Distance

- Distances, such as the Euclidean distance, have some well known properties.
 1. $d(p, q) \geq 0$ for all p and q and $d(p, q) = 0$ only if $p = q$. (Positive definiteness)
 2. $d(p, q) = d(q, p)$ for all p and q . (Symmetry)
 3. $d(p, r) \leq d(p, q) + d(q, r)$ for all points $p, q,$ and r . (Triangle Inequality)

where $d(p, q)$ is the distance (dissimilarity) between points (data objects), p and q .

- A distance that satisfies these properties is a **metric**



Common Properties of a Similarity

- Similarities, also have some well known properties.

1. $s(p, q) = 1$ (or maximum similarity) only if $p = q$.

2. $s(p, q) = s(q, p)$ for all p and q . (Symmetry)

where $s(p, q)$ is the similarity between points (data objects), p and q .



Binary Data

Categorical	insufficient	sufficient	good	very good	excellent
p1	0	0	1	0	0
p2	0	0	1	0	0
p3	1	0	0	0	0
p4	0	1	0	0	0
item	bread	butter	milk	apple	tooth-past
p1	1	1	0	1	0
p2	0	0	1	1	1
p3	1	1	1	0	0
p4	1	0	1	1	0



Similarity Between Binary Vectors

- Common situation is that objects, p and q , have only binary attributes

- Compute similarities using the following quantities

M_{01} = the number of attributes where p was 0 and q was 1

M_{10} = the number of attributes where p was 1 and q was 0

M_{00} = the number of attributes where p was 0 and q was 0

M_{11} = the number of attributes where p was 1 and q was 1

- Simple Matching and Jaccard Coefficients

SMC = number of matches / number of attributes

$$= (M_{11} + M_{00}) / (M_{01} + M_{10} + M_{11} + M_{00})$$

J = number of 11 matches / number of not-both-zero attributes values

$$= (M_{11}) / (M_{01} + M_{10} + M_{11})$$



SMC versus Jaccard: Example

$p = 1000000000$

$q = 0000001001$

$M_{01} = 2$ (the number of attributes where p was 0 and q was 1)

$M_{10} = 1$ (the number of attributes where p was 1 and q was 0)

$M_{00} = 7$ (the number of attributes where p was 0 and q was 0)

$M_{11} = 0$ (the number of attributes where p was 1 and q was 1)

$$SMC = (M_{11} + M_{00}) / (M_{01} + M_{10} + M_{11} + M_{00}) = (0+7) / (2+1+0+7) = 0.7$$

$$J = (M_{11}) / (M_{01} + M_{10} + M_{11}) = 0 / (2 + 1 + 0) = 0$$



Document Data

	team	coach	play	ball	score	game	win	lost	timeout	season
Document 1	3	0	5	0	2	6	0	2	0	2
Document 2	0	7	0	2	1	0	0	3	0	0
Document 3	0	1	0	0	1	2	2	0	3	0



Cosine Similarity

- If d_1 and d_2 are two document vectors, then

$$\cos(d_1, d_2) = (d_1 \bullet d_2) / (||d_1|| ||d_2||),$$

where \bullet indicates vector dot product and $||d||$ is the length of vector d .

- Example:

$$d_1 = 3\ 2\ 0\ 5\ 0\ 0\ 0\ 2\ 0\ 0$$

$$d_2 = 1\ 0\ 0\ 0\ 0\ 0\ 0\ 1\ 0\ 2$$

$$d_1 \bullet d_2 = 3*1 + 2*0 + 0*0 + 5*0 + 0*0 + 0*0 + 0*0 + 2*1 + 0*0 + 0*2 = 5$$

$$||d_1|| = (3*3 + 2*2 + 0*0 + 5*5 + 0*0 + 0*0 + 0*0 + 2*2 + 0*0 + 0*0)^{0.5} = (42)^{0.5} = 6.481$$

$$||d_2|| = (1*1 + 0*0 + 0*0 + 0*0 + 0*0 + 0*0 + 0*0 + 1*1 + 0*0 + 2*2)^{0.5} = (6)^{0.5} = 2.245$$

$$\cos(d_1, d_2) = .3150$$



Correlation

- Correlation measures the linear relationship between objects (binary or continuous)
- To compute correlation, we standardize data objects, p and q , and then take their dot product (covariance/standard deviation)

$$p'_k = (p_k - \text{mean}(p))$$

$$q'_k = (q_k - \text{mean}(q))$$

$$\text{correlation}(p, q) = (p' \cdot q') / (n - 1) \text{std}(p) \text{std}(q)$$

