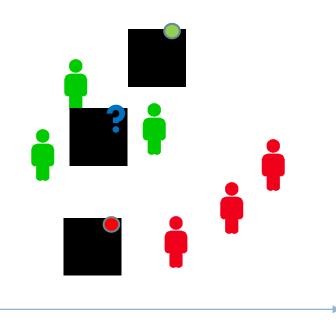
## Advanced classification methods

# The most stupid classifier

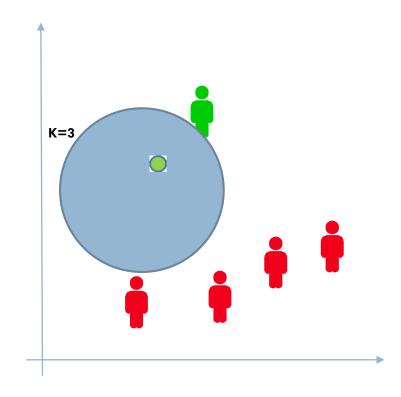
### Rote learner

- To classify object X, check if there is a labelled example in the training set identical to X
- Yes  $\rightarrow$  X has the same label
- $\square$  No  $\rightarrow$  I don't know



# Classify by similarity

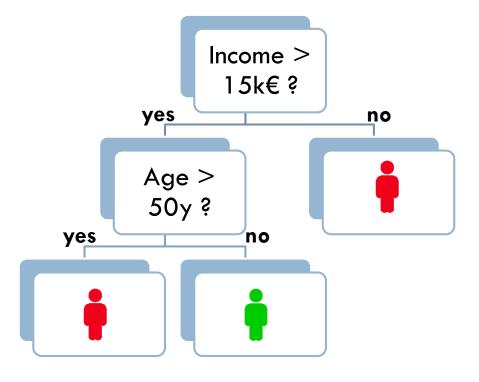
- K-Nearest Neighbors
  - Decide label based on K most similar examples

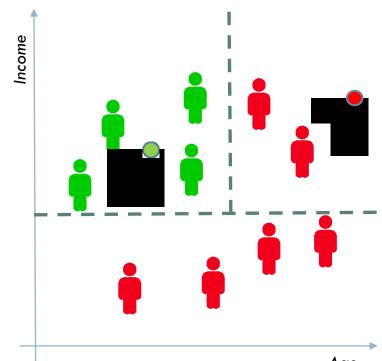


# Build a model

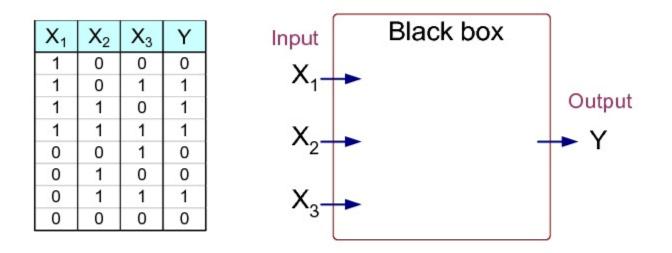
### Decision Trees

### Cut space by lines orthogonal to the axes



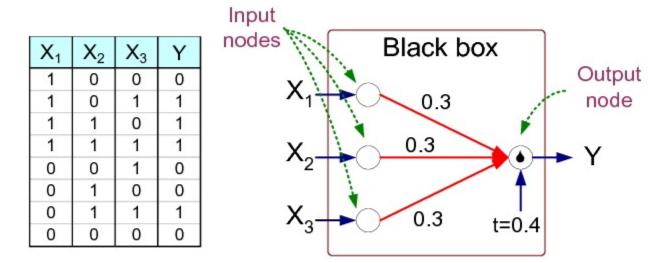


## Artificial Neural Networks (ANN)



Output Y is 1 if at least two of the three inputs are equal to 1.

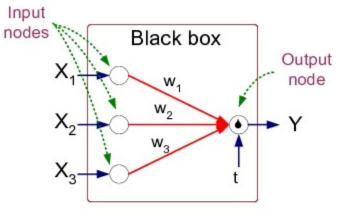
## Artificial Neural Networks (ANN)



$$Y = I(0.3X_1 + 0.3X_2 + 0.3X_3 - 0.4 > 0)$$
  
where  $I(z) = \begin{cases} 1 & \text{if } z \text{ is true} \\ 0 & \text{otherwise} \end{cases}$ 

### Artificial Neural Networks (ANN)

- Model is an assembly of inter-connected nodes and weighted links
- Output node sums up each of its input value according to the weights of its links
- Compare output node against some threshold t

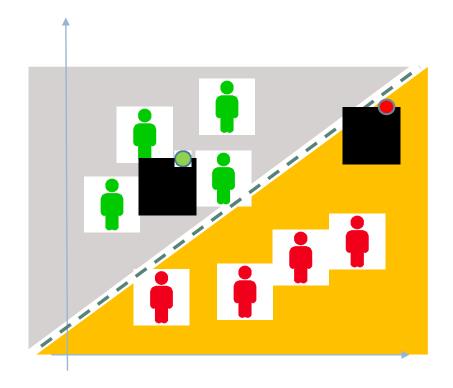


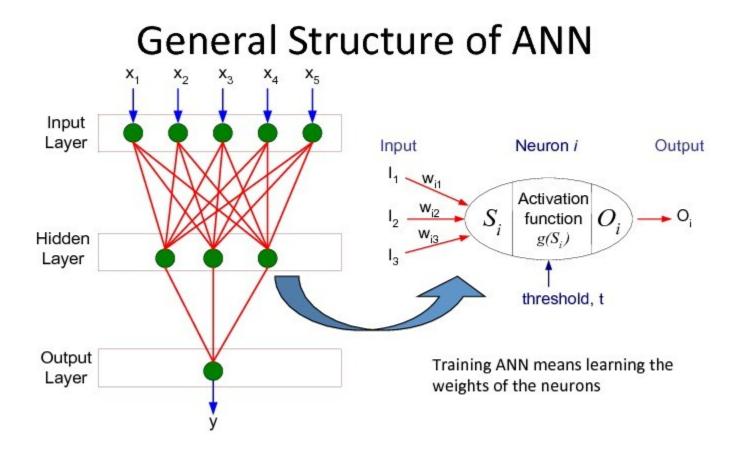
Perceptron Model

$$Y = I(\sum_{i} w_{i}X_{i} - t) \text{ or }$$
$$Y = sign(\sum_{i} w_{i}X_{i} - t)$$

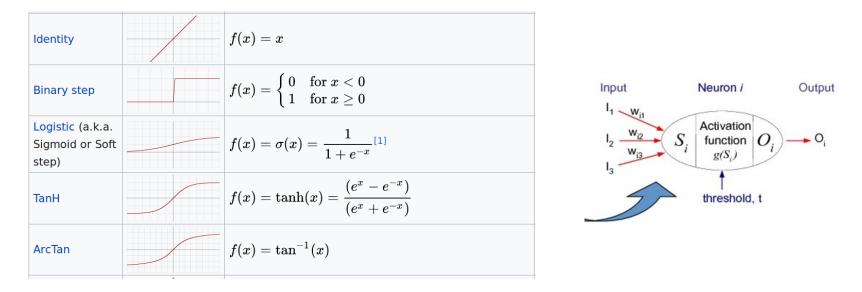
# Sample model on 2-D

- □ Linear separation line
  - General case: lines can be oblique





### Notice: activation function is fundamental !!!



With Identity (= no activation function) the ANN reduces to a simple perceptron
Proof: a linear sum of linear sums, is just another linear sum

# Algorithm for learning ANN

- Initialize the weights (w<sub>0</sub>, w<sub>1</sub>, ..., w<sub>k</sub>)
- Adjust the weights in such a way that the output of ANN is consistent with class labels of training examples E

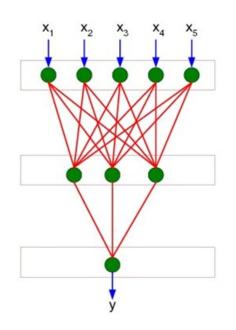
Objective function:

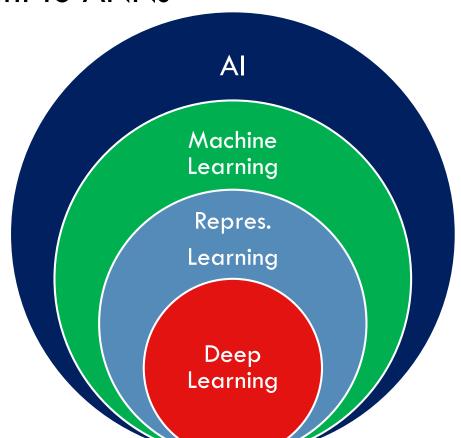
$$=\sum_{i}\left[Y_{i}-f(w_{i},X_{i})\right]^{2}$$

- Find the weights w<sub>i</sub>'s that minimize the above objective function
  - e.g., backpropagation algorithm (see lecture notes)

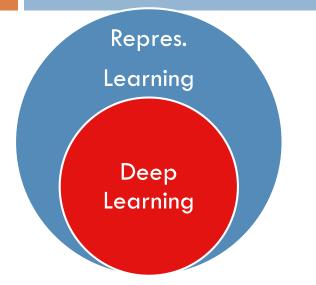
# A quick look on Deep Learning

- Various approaches exist
- Basic examples equivalent to ANNs with several levels





# Deep learning



#### Representation learning methods that

- allow a machine to be fed with raw data and
- to automatically discover the representations needed for detection or classification.

#### Raw representation

- Age
- Weight
- Income
- Children

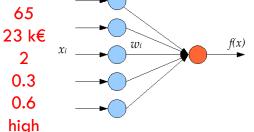
. . .

- Likes sport
- Likes reading (

35

• • •

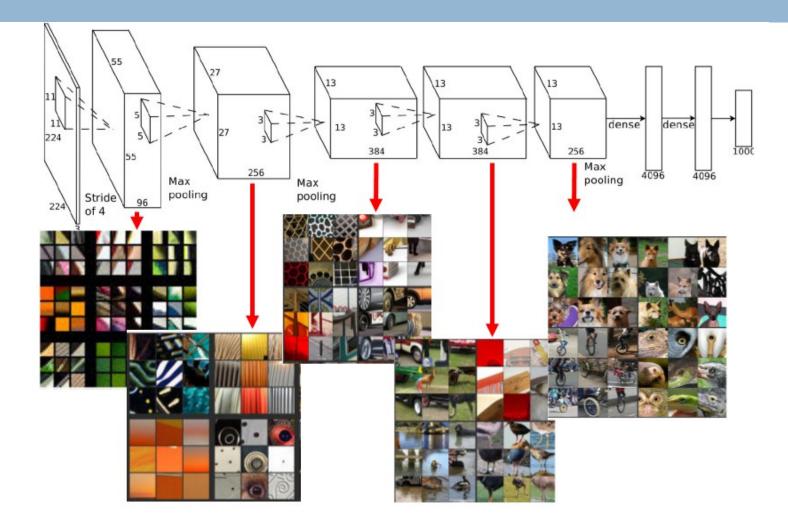
Education



#### **Higher-level representation**

- Young parent 0.9
- Fit sportsman 0.1
- High-educated reader 0.8
- Rich obese 0.0
- ... ...

# **Multiple Levels Of Abstraction**



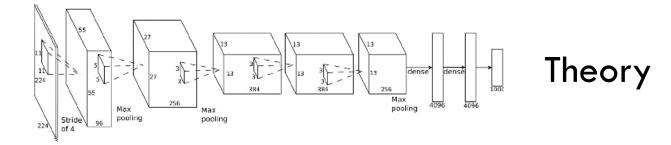
Why now?



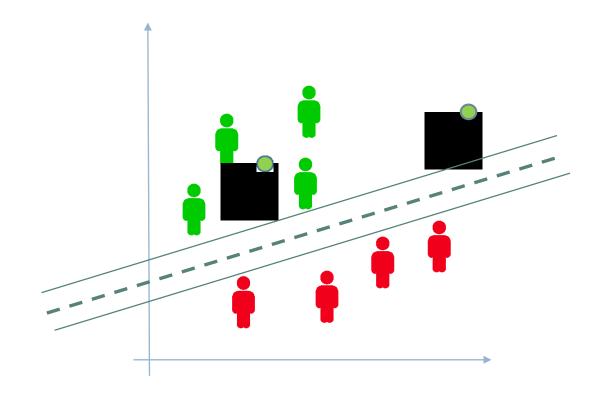
## (Big) Data

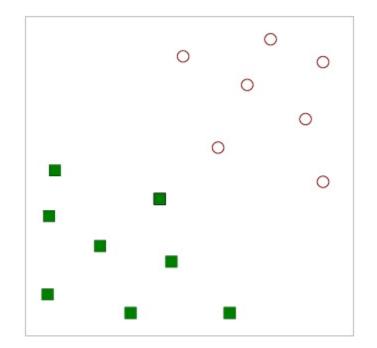




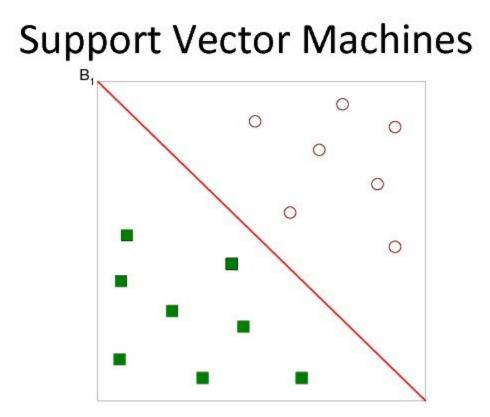


### Support Vector Machine

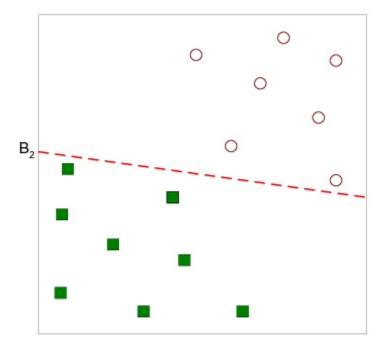




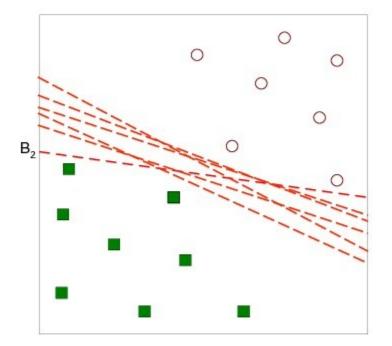
Find a linear hyperplane (decision boundary) that will separate the data



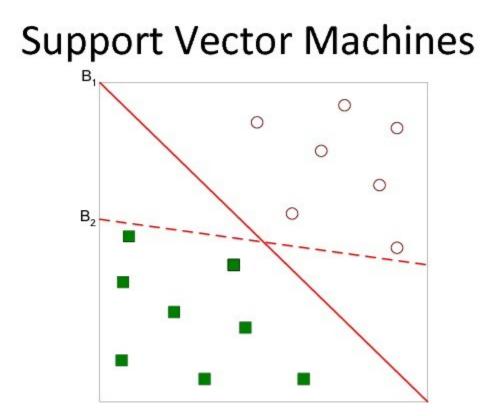
One Possible Solution



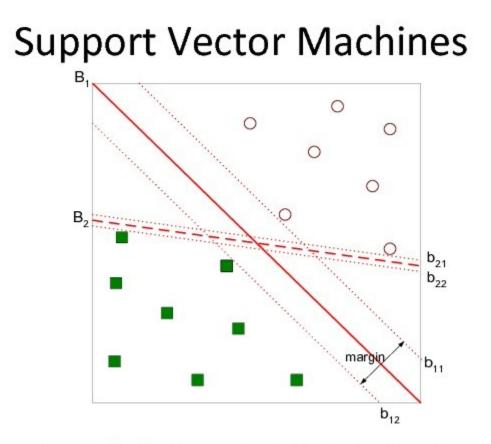
Another possible solution



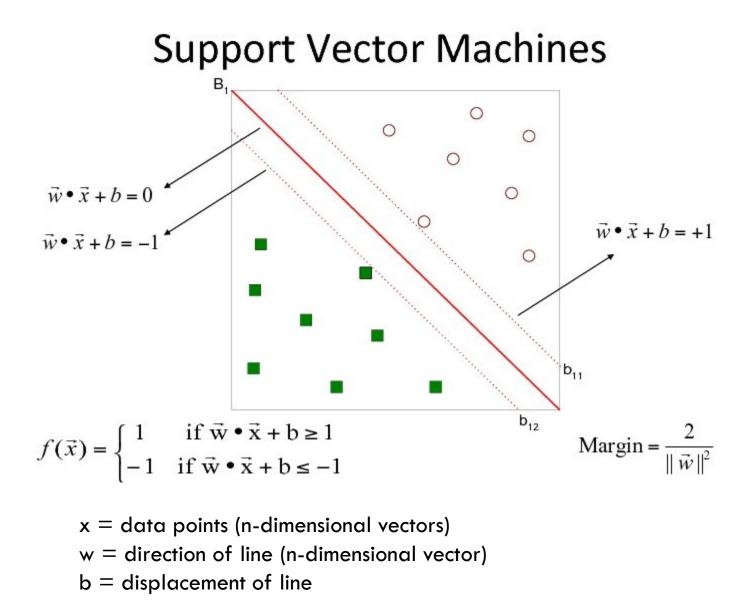
Other possible solutions



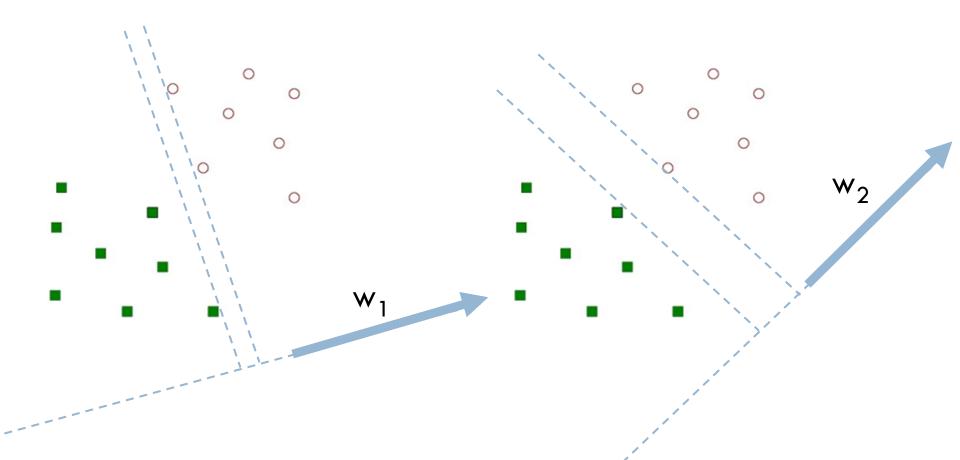
- Which one is better? B1 or B2?
- How do you define better?



• Find hyperplane maximizes the margin => B1 is better than B2







Each data point is projected over direction w

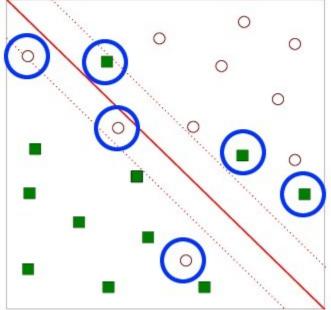
 $\square$  Projections along w<sub>2</sub> have much larger margin than w<sub>1</sub>

- We want to maximize: Margin =  $\frac{2}{\|\vec{w}\|^2}$ - Which is equivalent to minimizing:  $L(w) = \frac{\|\vec{w}\|^2}{2}$ 
  - But subjected to the following constraints:

$$f(\vec{x}_i) = \begin{cases} 1 & \text{if } \vec{w} \cdot \vec{x}_i + b \ge 1 \\ -1 & \text{if } \vec{w} \cdot \vec{x}_i + b \le -1 \end{cases}$$

- This is a constrained optimization problem
  - Numerical approaches to solve it (e.g., quadratic programming)

• What if the problem is not linearly separable?



- What if the problem is not linearly separable?
  - Introduce slack variables
    - Need to minimize:

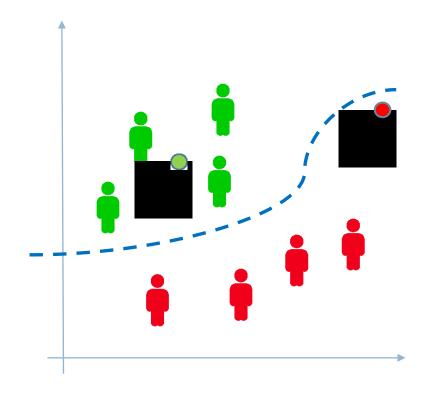
$$L(w) = \frac{\|\vec{w}\|^2}{2} + C\left(\sum_{i=1}^N \xi_i^k\right)$$

Subject to:

$$f(\vec{x}_i) = \begin{cases} 1 & \text{if } \vec{w} \cdot \vec{x}_i + b \neq 1 - \xi_i \\ -1 & \text{if } \vec{w} \cdot \vec{x}_i + b \neq -1 + \xi_i \end{cases}$$

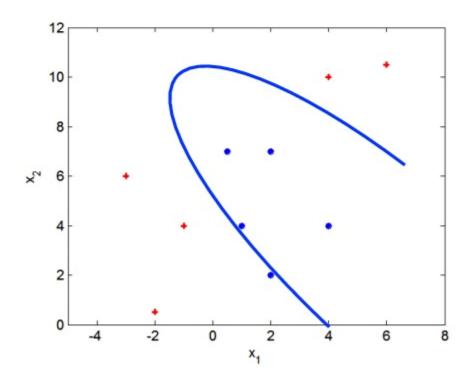
- Basically, each point is "moved" by a a specific amount along the w direction
- The cost function "pays" for each extra movement

### Non-linear separation line



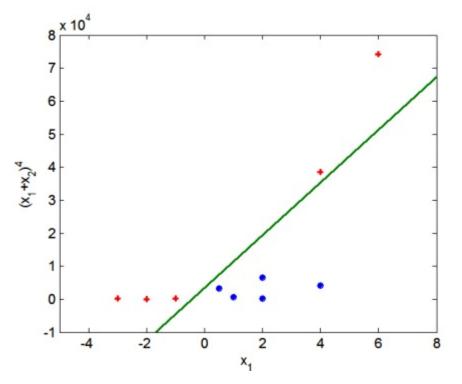
### Nonlinear Support Vector Machines

• What if decision boundary is not linear?



### **Nonlinear Support Vector Machines**

• Transform data into higher dimensional space



- Key problem: find the most appropriate set of extra dimensions
  - They are derived from original attributes
  - Most common:  $x^2$ ,  $(x+y)^2$ , and other polynomials