k-Nearest Neighbor Classifier

A medical expert is going to build up a case-based reasoning system for diagnosis tasks. Cases correspond to individual persons where the case problem parts are made up of a number of features describing possible symptoms and the solution parts represent the diagnosis (classification of disease). The case base contains the seven cases provided in the table below.

Training	Fever	Vomiting	Diarrhea	Shivering	Classification
c_1	no	no	no	no	healty (H)
c_2	average	no	no	no	influenza (I)
c_3	high	no	no	yes	influenza (I)
c_4	high	yes	yes	no	salmonella poisoning (S)
c_5	average	no	yes	no	salmonella poisoning (S)
c_6	no	yes	yes	no	bowel inflammation (B)
c_7	average	yes	yes	no	bowel inflammation (B)

Similarity provided by an expert

sim_F

q \ c	no	avg	high
no	1.0	0.7	0.2
avg	0.5	1.0	0.8
high	0.0	0.3	1.0

$sim_V = sim_D = sim_{Sh}$

q	yes	no
yes	1.0	0.0
no	0.2	1.0

Weights
$w_F = 0.3$
$w_V = 0.2$
$W_D = 0.2$
$w_{Sh} = 0.3$

Classify the new instance q = (high; no; no; no) by applying the KNN algorithm with K=1,2,3

Calculate the similarity between all cases from the case base and the new instance q = (high; no; no; no)

c1 = (no; no; no; no):

Sim(q; c1) = 0.3*0.0 + 0.2 *1.0 + 0.2*1.0 + 0.3* 1.0 = 0.70

c2 = (average; no; no; no):

Sim(q; c2) = 0.3* 0.3 + 0.2 *1.0 + 0.2*1.0 + 0.3*1.0 = 0.79

c3 = (high; no; no; yes)

Sim(q; c3) = 0.3*1.0 + 0.2*1.0 + 0.2*1.0 + 0.3*0.2 = 0.76

c4 = (high; yes; yes; no):

Sim(q; c4) = 0.3*1.0 + 0.2*0.2 + 0.2*0.2 + 0.3*1.0 = 0.68

c5 = (average; no; yes; no):

Sim(q; c5) = 0.3*0.3 + 0.2*1.0 + 0.2*0.2 + 0.3*1.0 = 0.63

c6 = (no; yes; yes; no):

Sim(q; c6) = 0.3*0.0 + 0.2*0.2 + 0.2*0.2 + 0.3*1.0 = 0.28

c7 = (average; yes; yes; no):

Sim(q; c7) = 0.3*0.3 + 0.2*0.2 + 0.2*0.2 + 0.3*1.0 = 0.47

sim_F

q \ c	no	avg	high
no	1.0	0.7	0.2
avg	0.5	1.0	0.8
high	0.0	0.3	1.0

$sim_V = sim_D = sim_{Sh}$

q \	yes	no
yes	1.0	0.0
no	0.2	1.0

Weights
$w_F = 0.3$
$w_V = 0.2$
$W_D = 0.2$
$w_{Sh} = 0.3$

KNN Classification for K=1

c1 = (no; no; no; no):

Sim(q; c1) = 0.3*0.0 + 0.2 *1.0 + 0.2*1.0 + 0.3* 1.0 = 0.70

c2 = (average; no; no; no):

Sim(q; c2) = 0.3* 0.3 + 0.2 *1.0 + 0.2*1.0 + 0.3*1.0 = 0.79

c3 = (high; no; no; yes)

Sim(q; c3) = 0.3*1.0 + 0.2*1.0 + 0.2*1.0 + 0.3*0.2 = 0.76

c4 = (high; yes; yes; no):

Sim(q; c4) = 0.3*1.0 + 0.2*0.2 + 0.2*0.2 + 0.3*1.0 = 0.68

c5 = (average; no; yes; no):

Sim(q; c5) = 0.3*0.3 + 0.2*1.0 + 0.2*0.2 + 0.3*1.0 = 0.63

c6 = (no; yes; yes; no):

Sim(q; c6) = 0.3*0.0 + 0.2*0.2 + 0.2*0.2 + 0.3*1.0 = 0.28

c7 = (average; yes; yes; no):

Sim(q; c7) = 0.3*0.3 + 0.2*0.2 + 0.2*0.2 + 0.3*1.0 = 0.47

sim_F

q \ c	no	avg	high
no	1.0	0.7	0.2
avg	0.5	1.0	0.8
high	0.0	0.3	1.0

Weights

$w_F = 0.3$

$w_V = 0.2$

$W_D = 0.2$

$w_{Sh} = 0.3$

Class: Influenza

KNN Classification for K=2

c1 = (no; no; no; no):

Sim(q; c1) = 0.3*0.0 + 0.2 *1.0 + 0.2*1.0 + 0.3* 1.0 = 0.70

c2 = (average; no; no; no):

Sim(q; c2) = 0.3* 0.3 + 0.2 *1.0 + 0.2*1.0 + 0.3*1.0 = 0.79

c3 = (high; no; no; yes):

Sim(q; c3) = 0.3*1.0 + 0.2*1.0 + 0.2*1.0 + 0.3*0.2 = 0.76

c4 = (high; yes; yes; no):

Sim(q; c4) = 0.3*1.0 + 0.2*0.2 + 0.2*0.2 + 0.3*1.0 = 0.68

c5 = (average; no; yes; no):

Sim(q; c5) = 0.3*0.3 + 0.2*1.0 + 0.2*0.2 + 0.3*1.0 = 0.63

c6 = (no; yes; yes; no):

Sim(q; c6) = 0.3*0.0 + 0.2*0.2 + 0.2*0.2 + 0.3*1.0 = 0.28

c7 = (average; yes; yes; no):

Sim(q; c7) = 0.3*0.3 + 0.2*0.2 + 0.2*0.2 + 0.3*1.0 = 0.47

sim_F

q \ c	no	avg	high
no	1.0	0.7	0.2
avg	0.5	1.0	0.8
high	0.0	0.3	1.0

Weights
$w_F = 0.3$
$w_V = 0.2$
$W_D = 0.2$
$w_{Sh} = 0.3$

C2: Influenza
C3: Influenza

Class: Influenza

KNN Classification for K=3

c1 = (no; no; no; no):
Sim(q; c1) = 0.3*0.0 + 0.2 *1.0 + 0.2*1.0 + 0.3* 1.0 = 0.70

c2 = (average; no; no; no):
Sim(q; c2) = 0.3* 0.3 + 0.2 *1.0 + 0.2*1.0 + 0.3*1.0 = 0.79

c3 = (high; no; no; yes):
Sim(q; c3) = 0.3*1.0 + 0.2*1.0 + 0.2*1.0 + 0.3*0.2 = 0.76

c4 = (high; yes; yes; no):
Sim(q; c4) = 0.3*1.0 + 0.2*0.2 + 0.2*0.2 + 0.3*1.0 = 0.68

c5 = (average; no; yes; no):
Sim(q; c5) = 0.3*0.3 + 0.2*1.0 + 0.2*0.2 + 0.3*1.0 = 0.63

c6 = (no; yes; yes; no):
Sim(q; c6) = 0.3*0.0 + 0.2*0.2 + 0.2*0.2 + 0.3*1.0 = 0.28

c7 = (average; yes; yes; no):
Sim(q; c7) = 0.3*0.3 + 0.2*0.2 + 0.2*0.2 + 0.3*1.0 = 0.47

sim_F

q \ c	no	avg	high
no	1.0	0.7	0.2
avg	0.5	1.0	0.8
high	0.0	0.3	1.0

Weights
$w_F = 0.3$
$w_V = 0.2$
$W_D = 0.2$
$w_{Sh} = 0.3$

C1: healty
C2: Influenza
C3: Influenza

Class: Influenza