

# High Quality True-Positive Prediction for Fiscal Fraud Detection

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# Outline

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- ▶ **Sniper Core**
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  - ▶ Merging Rule
- ▶ **Evaluation**
- ▶ **Conclusion**



# The Context: VAT frauds in Italy

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- ▶ DIVA - A joint initiative involving academic researchers, experts on fiscal laws, IT Professionals
- ▶ **Main objective:**
  - To tackle the VAT Fraud Detection issue raised by the credit mechanism via the adoption of data mining techniques.



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FUTURO SEMPLICE

# Scenario

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- ▶ Several challenges, both from a scientific and a practical point of view:
  - ▶ Sample selection bias
    - ▶ Audited subjects are not randomly chosen
    - ▶ Highly skewed data
      - Positive subjects larger than non-defrauders in audit data
  - ▶ Imprecise settings
    - ▶ Inaccurate, incomplete, and irrelevant data attributes
  - ▶ Only 0.004% of population audited



# Motivation

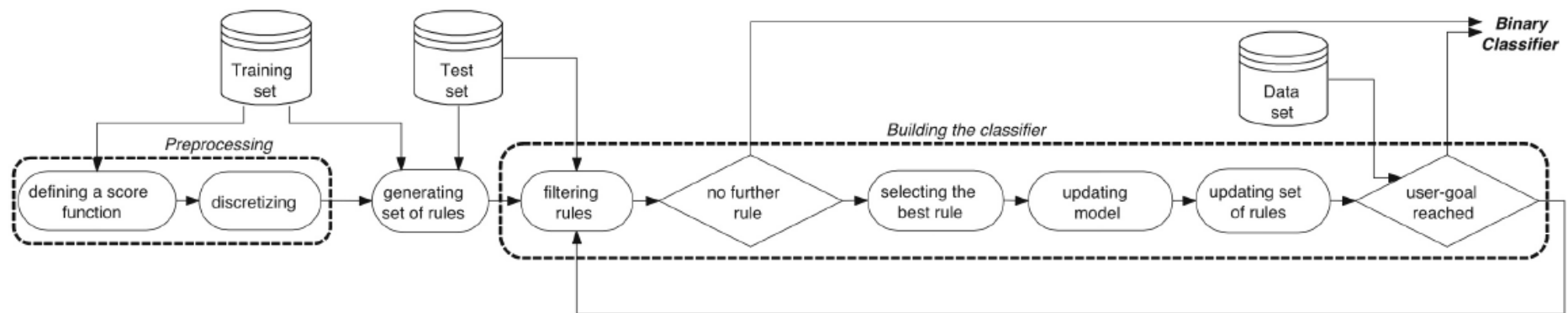
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- ▶ **Classical approaches to the problem of fraud detection are not very effective:**
  - ▶ Rule-Based classifiers are preferable for interpretability, but
    - ▶ Poor predictive accuracy in highly imprecise learning settings
    - ▶ Class-imbalance problem
  - ▶ Cost-sensitive classification and meta-learning approaches suffer from low interpretability



# The proposal: Sniper as a meta-learner

- ▶ The core of the Sniper technique is the extraction of a binary rule-based classifier able to identify  $X$  topmost defrauders
  - ▶ Based on the combined use of local models and the definition of multi-objective functions.



## DIVA Overview

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- ▶ The data made available by the agency consisted of about 34 million VAT declarations spread over 5 years.
- ▶ Data contain general ‘demographic’ information, plus specific information about VAT declarations.
- ▶ As a result of a data understanding process conducted jointly with domain experts, we chose a total of 135 such features and 45,442 audited subjects.



# Scoring individuals

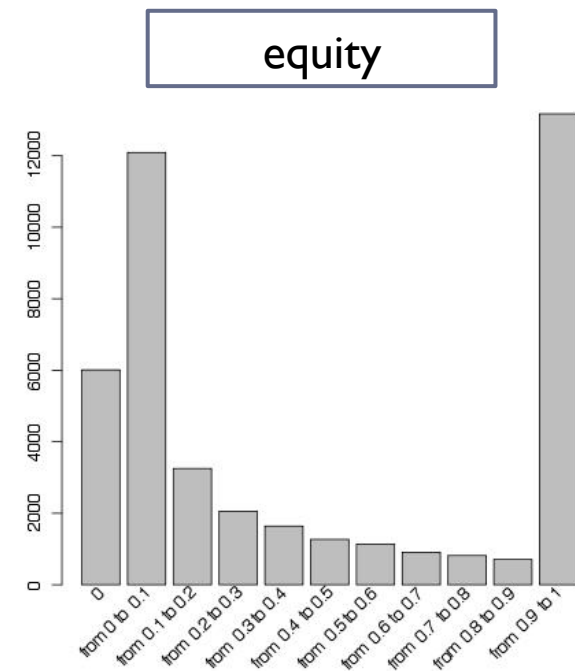
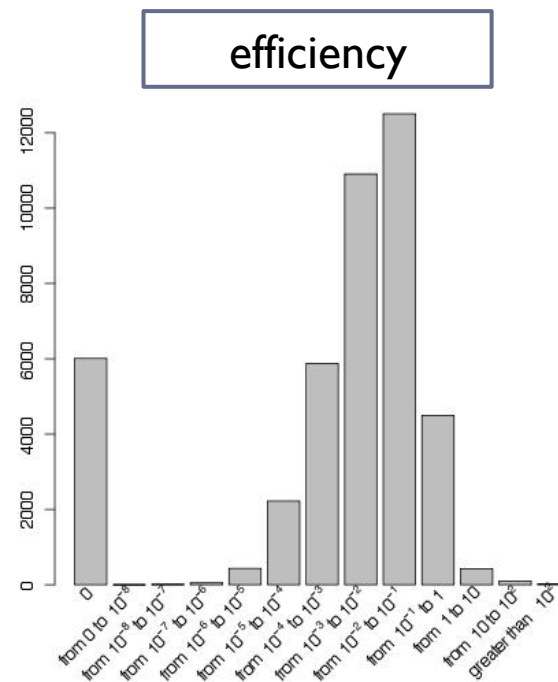
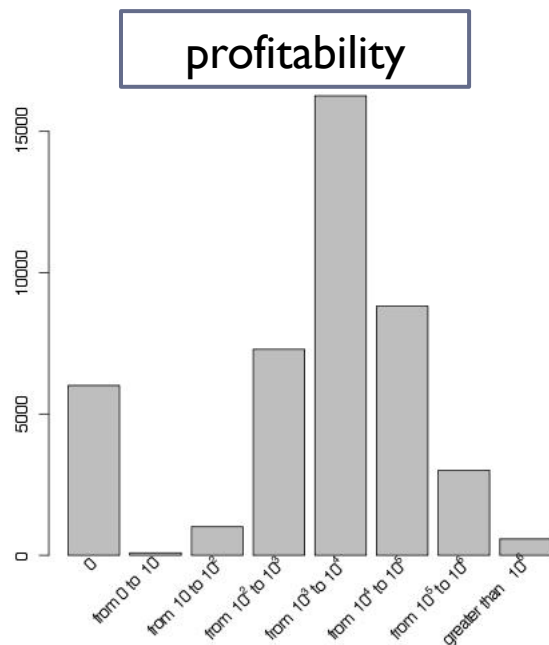
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- ▶ A multi-purpose modeling strategy, aiming at characterizing the exceptionalness and interestingness of an individual
  - ▶ **PROFITABILITY:** The amount of VAT fraud
    - ▶ The higher, the better
  - ▶ **EQUITY**
    - ▶ Low amounts do not necessarily correspond to meaningless fraudsters. The amount of fraud is relevant related to their business volume (1.000eur on 10.000eur is better than 1.000eur on 100.000eur)
  - ▶ **EFFICIENCY**
    - ▶ Scoring and detection should be sensitive to total/partial frauds (underclaring 200eur declaring 2.000eur is less dignificant than underclaring 200eur declaring 200eur)



# Issues

- ▶ Need to face a trade-off among profitability, equity and efficiency
  - ▶ Solution: a combination of baseline functions
  - ▶ AND,OR, FUZZY\_AND, FUZZY\_OR



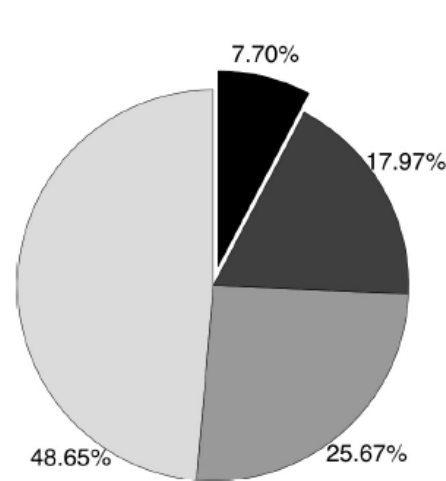
# The Fuzzy combination

- ▶ Two different objective functions, four main classes

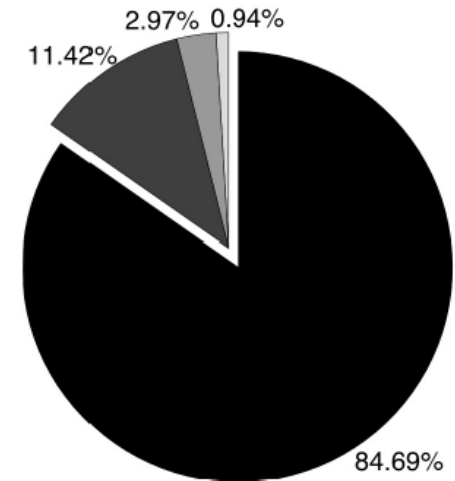
$$\mathcal{F}_{\Pi}(o) = \prod_{i \in [1, k]} (\mathcal{N}(f_i(o)))^{p_i}$$

harmonization f.      weight

$$\mathcal{F}_{\Sigma}(o) = \sum_{i \in [1, k]} p_i \cdot \mathcal{N}(f_i(o)),$$



Subject partitioning



Retrieved fraud

Score function results



# Generating rules

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- ▶ Sniper builds a hybrid classifier, resulting from the combination of the whole set of classifiers trained over the training set
- ▶ Advantages:
  - ▶ Separate model construction from model selection
  - ▶ Model construction
    - ▶ Several different strategies are attempted to build models focused on local peculiarities of the top class
  - ▶ Model selection
    - ▶ Several local fragments can be selected or discarded if the global accuracy improves



# Merging Rules

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- ▶ A candidate ruleset  $R$  is obtained by merging all the rules returned by  $h$  classifiers modeling the **top** class

$$\mathcal{R} = \left\{ r \in \bigcup_{i \in [1, h]} R_i \mid r.class = top \right\}$$

- ▶  $R$  still represents a classifier, and class  $top$  is assigned to a non-labeled object  $o$  if and only if there exists at least a rule in  $R$  that activates it.
- ▶ The model is distilled from  $R$  by *selecting accurate rules, and removing* inaccurate rules from  $R$  in a principled (confidence-based) way



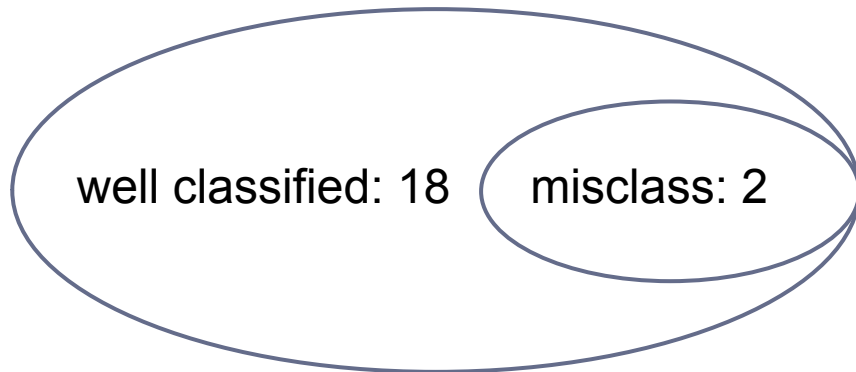
# Building Ruleset

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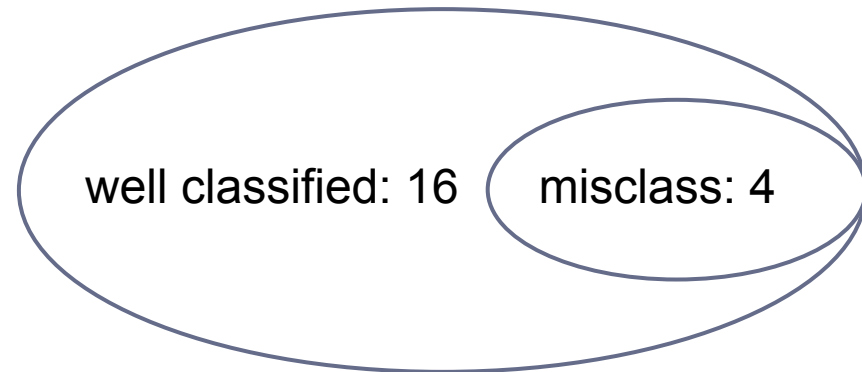
- ▶ Why we cannot just collect all the “good” rules from our classifiers?

$\text{conf}_{\min} = 0.8$

Rule 1: sup=20 conf=0.9



Rule 2: sup=20 conf=0.8



# Building Ruleset

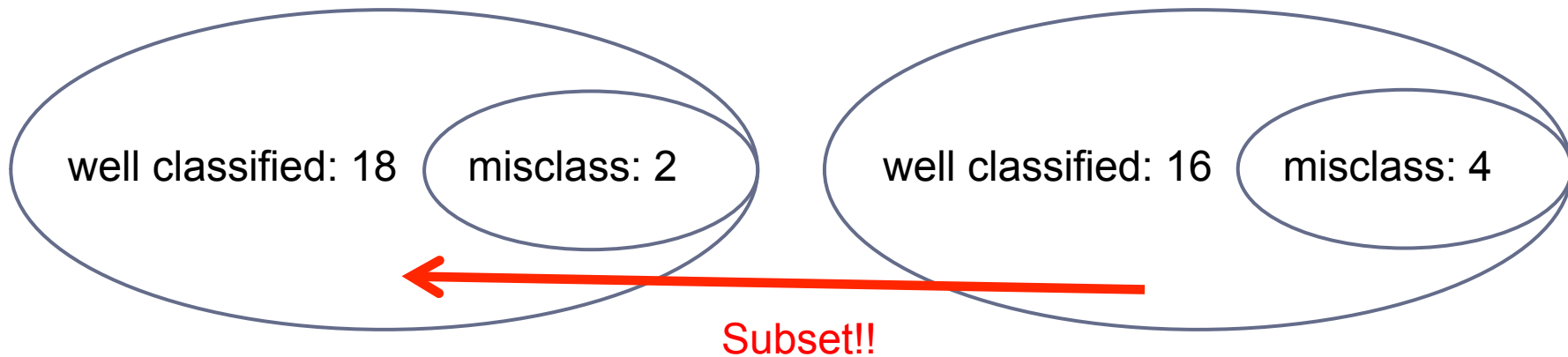
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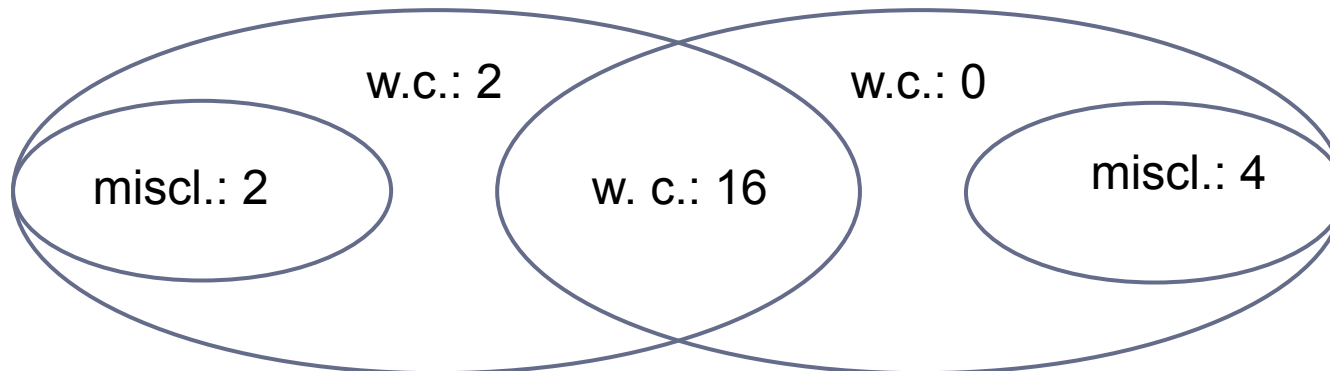
# Building Ruleset

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- ▶ Why we cannot just collect all the “good” rules from our classifiers?

$\text{conf}_{\min} = 0.8$

Rule 1 AND 2: sup=24 conf=0.75



# Merging Rules

**Input:** A set of non-exclusive positive rules  $\mathcal{R}$ ,  
a confidence threshold  $\gamma_{\min}$ ,  
an integer  $X$

**Output:** A model  $\mathcal{M}$

**Method:**

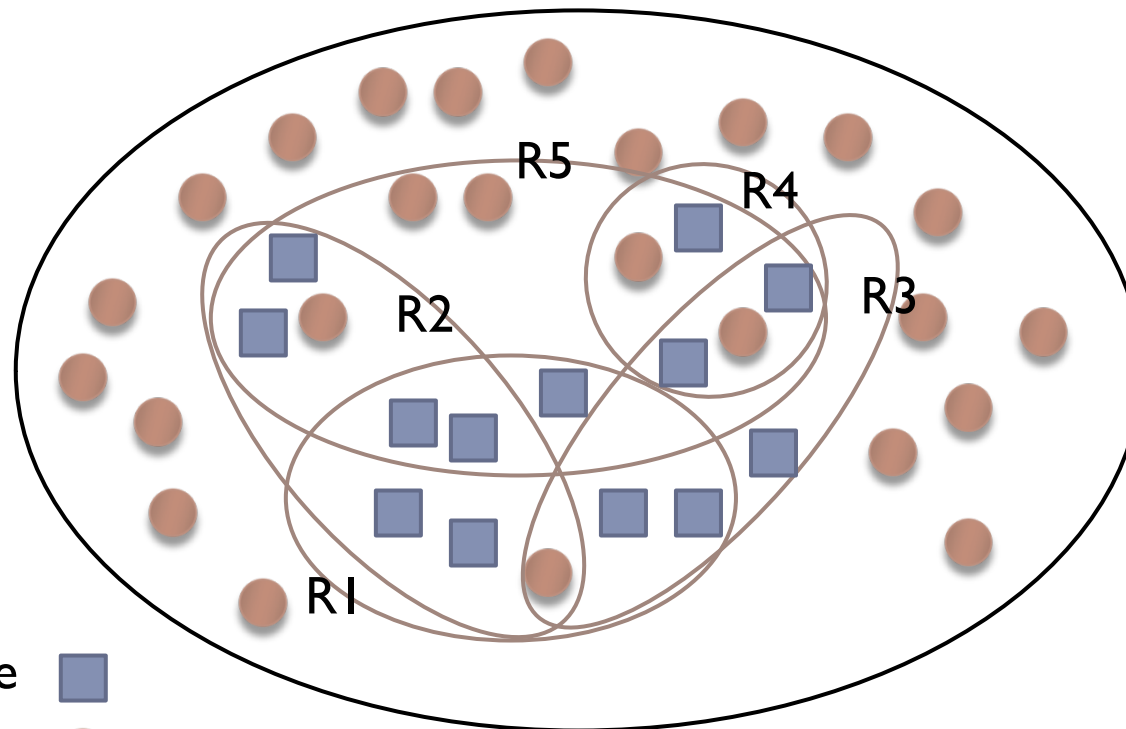
- 1:  $\mathcal{M} := \emptyset$
- 2:  $\mathcal{R} := \{r \in \mathcal{R} \mid \gamma(r) \geq \gamma_{\min}\}$
- 3: **while**  $\mathcal{R} \neq \emptyset$  **do** //first stop condition
- 4:      $r^* := \arg \max_{r \in \mathcal{R}} \{\gamma(r)\}$  //select the best rule
- 5:      $\mathcal{M} := \mathcal{M} \cup \{r^*\}$  //update the current model
- 6:     **if**  $\mathcal{M}(D) \geq X$  **then** //second stop condition
- 7:         **return**  $\mathcal{M}$
- 8:      $\mathcal{R}$  is updated by removing  $r^*$  and by replacing each rule  $r$  other than  $r^*$  with the rule  $r'$  if  $\gamma(r') = \gamma_{\min}$ , otherwise  $r$  is just removed from  $\mathcal{R}$
- 9: **return**  $\mathcal{M}$



# Merging Rules: Example

- ▶ Assume  $\gamma_{\min} = 60\%$
- ▶ Initially,  $R = \{R1, R2, R3, R4, R5\}$ ,  $M = \{\}$

| Rule_ID | Confidence |
|---------|------------|
| R1      | 87,50%     |
| R2      | 75%        |
| R3      | 71,4%      |
| R4      | 60%        |
| R5      | 58,30%     |



- ▶ Positive Example ■
- ▶ Negative Example ●

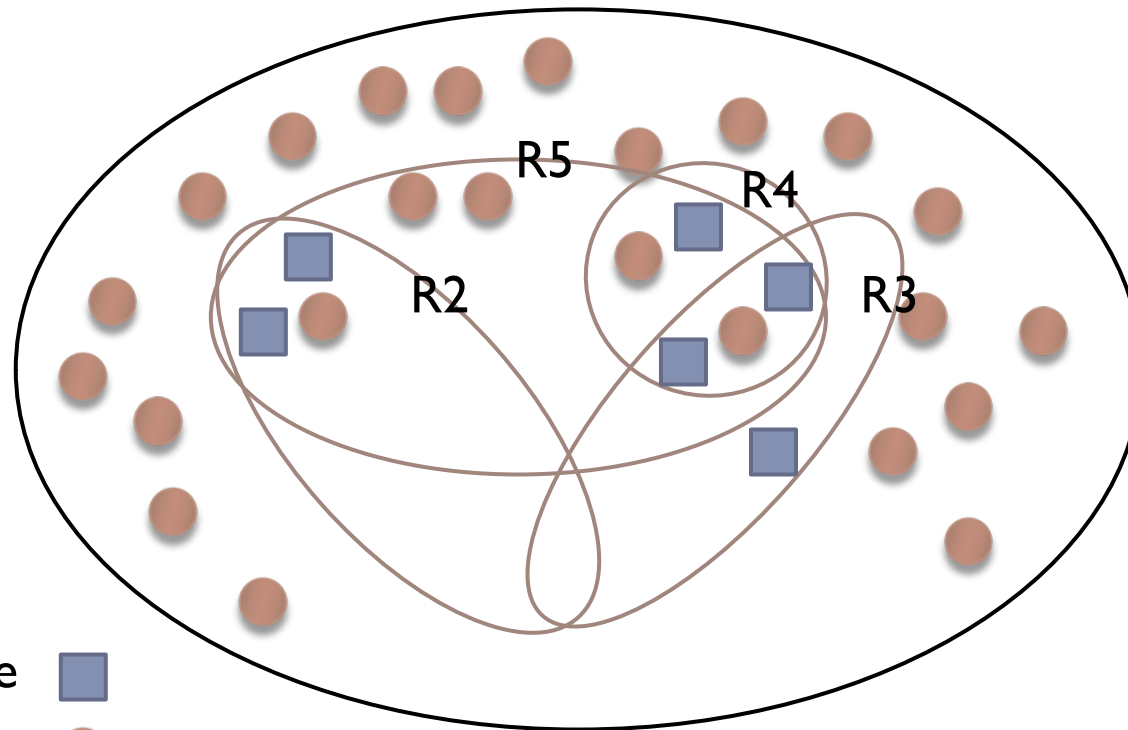


# Merging Rules: Example

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- ▶  $R = \{R2, R3, R4, R5\}, M = \{R1\}$

| Rule_ID | Confidence |
|---------|------------|
| R2      | 66,6%      |
| R3      | 75%        |
| R4      | 60%        |
| R5      | 50%        |



- ▶ Positive Example ■
  - ▶ Negative Example ●
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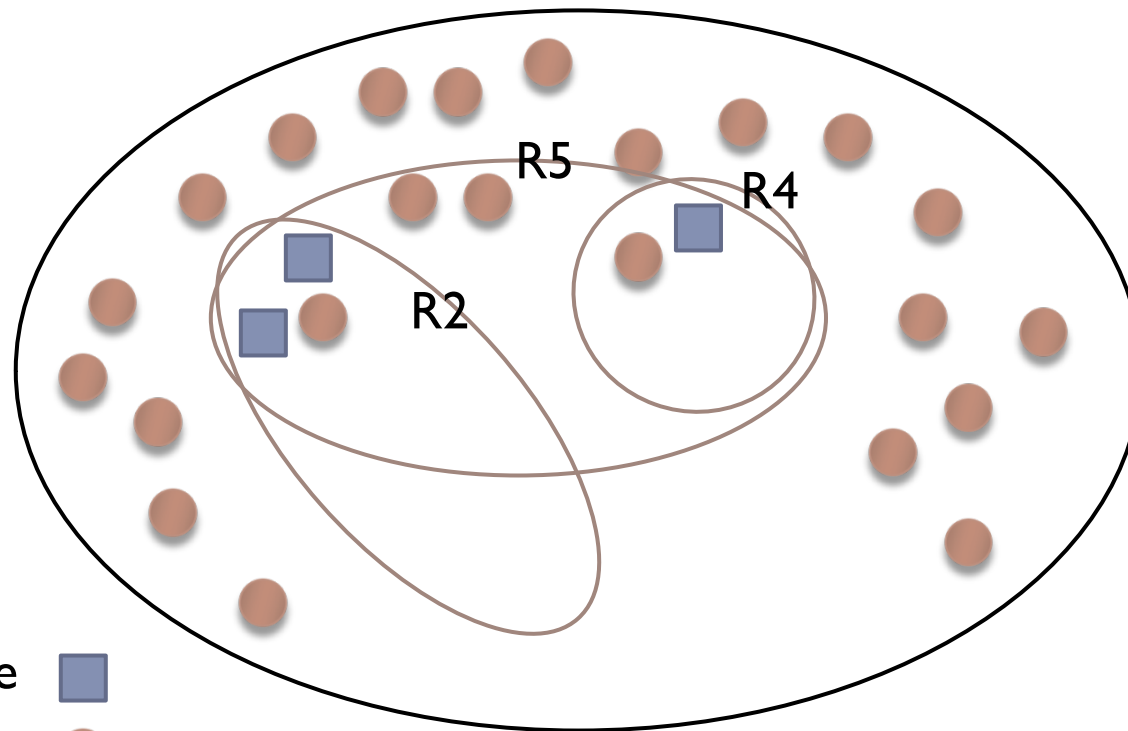


# Merging Rules: Example

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▶  $R = \{R2, R4, R5\}$ ,  $M = \{R1, R3\}$

| Rule_ID | Confidence |
|---------|------------|
| R2      | 66,6%      |
| R4      | 50%        |
| R5      | 42,8%      |



- ▶ Positive Example ■
  - ▶ Negative Example ●
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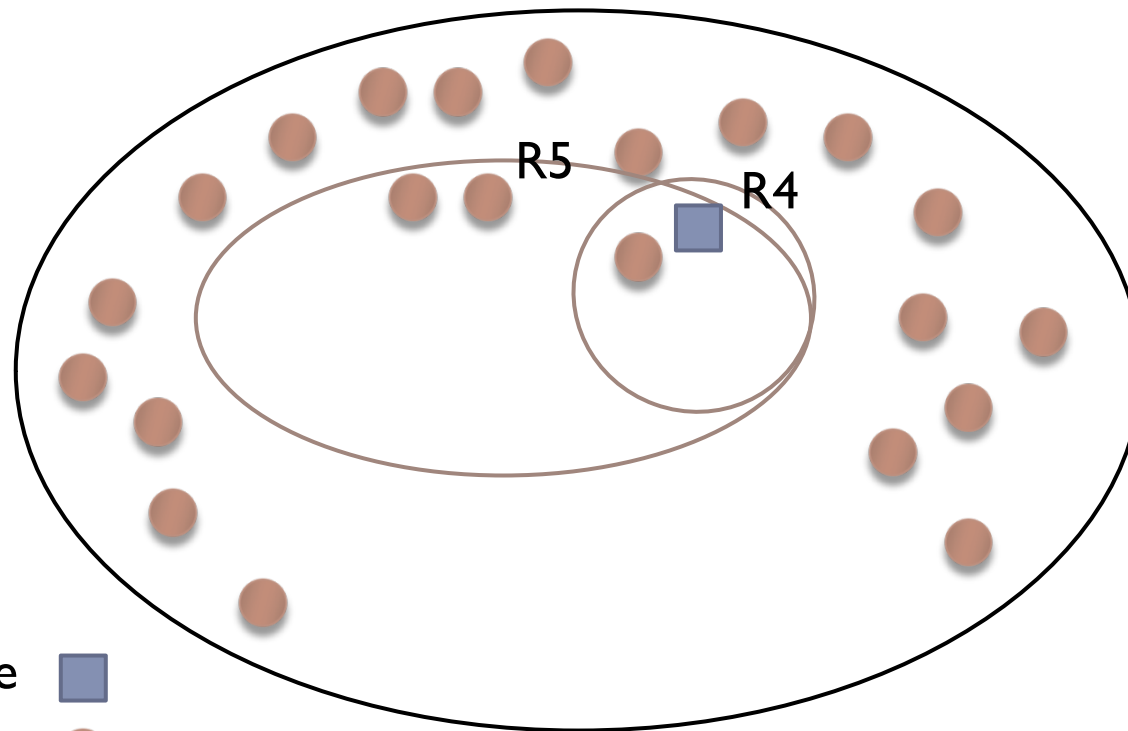


# Merging Rules: Example

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▶  $R = \{R4, R5\}, M = \{R1, R3, R2\}$

| Rule_ID | Confidence |
|---------|------------|
| R4      | 50%        |
| R5      | 25%        |



- ▶ Positive Example ■
  - ▶ Negative Example ●
- 



# Evaluation

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- ▶ We compared the results obtained from a single classifier against those obtained by Sniper in terms of confidence and support of the rules generated

| <i>classifier</i> | <i>supp (%)</i> | <i>conf (%)</i> | <i>dataset subjects</i> |
|-------------------|-----------------|-----------------|-------------------------|
| $C_1$             | 1.01            | 84.90           | 1,910                   |
| $C_2$             | 1.10            | 82.97           | 2,240                   |
| $C_3$             | 3.11            | 77.28           | 4,955                   |
| $C_4$             | 3.44            | 77.12           | 5,675                   |
| $C_5^*$           | 6.36            | 62.26           | 10,056                  |
| $C_6^*$           | 6.81            | 60.80           | 8,875                   |
| $C_7^*$           | 7.07            | 59.72           | 9,059                   |
| $C_8^*$           | 5.22            | 52.64           | 9,950                   |
| $C_9^*$           | 4.56            | 49.18           | 12,584                  |
| <b>S</b>          | 8.78            | 80.41           | 9,840                   |



# (Partial) Results

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- ▶ **1475 subjects identified**
  - ▶ 276 subjects audited (feb-2010)
    - ▶ 147 in class 3 (53,26%)
  
- ▶ **Mean Values:**
  - ▶ Proficiency: 77.5 | 4,14
  - ▶ Equity: 32,5738
  - ▶ Efficiency: 0,4252

