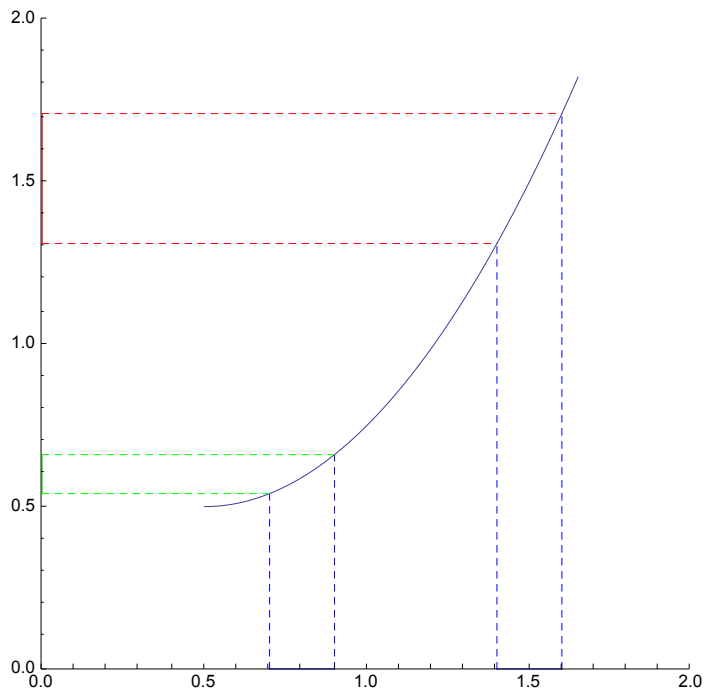


Errore inerente



Errore di troncamento (Formula di Taylor)

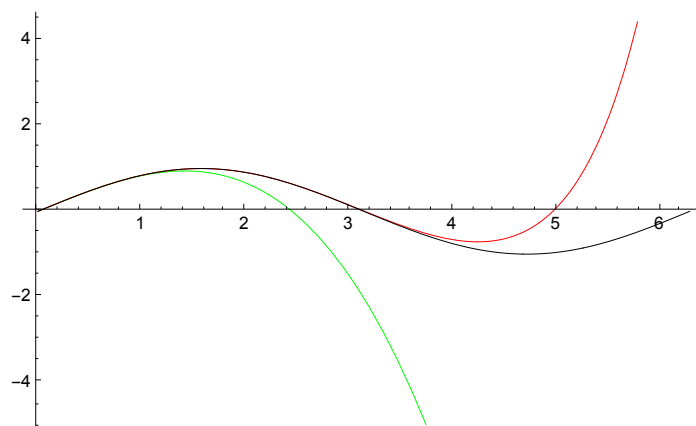
```
s1=Normal[Series[Sin[x],{x,0,3}]]
```

$$x - \frac{x^3}{6}$$

```
s2=Normal[Series[Sin[x],{x,0,10}]]
```

$$x - \frac{x^3}{6} + \frac{x^5}{120} - \frac{x^7}{5040} + \frac{x^9}{362880}$$

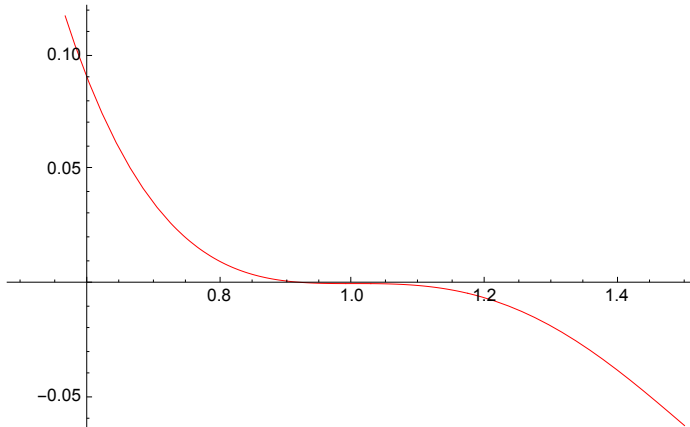
```
Plot[Evaluate[{s1, s2, Sin[x]}], {x, 0, 2 π}, PlotStyle → {Green, Red, Black}]
```



Errore di arrotondamento

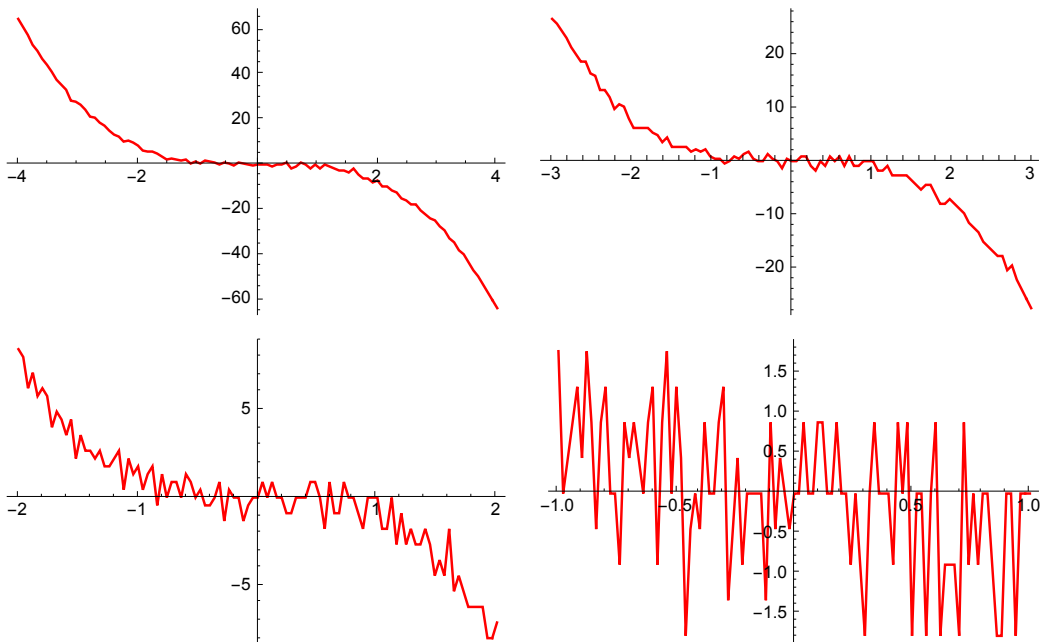
```
f[x_] := Evaluate[Expand[(x-1)(x-1)(x-1)(x-2)]]
```

```
Plot[f[x], {x, 0.5, 1.5}, PlotStyle -> Red]
```

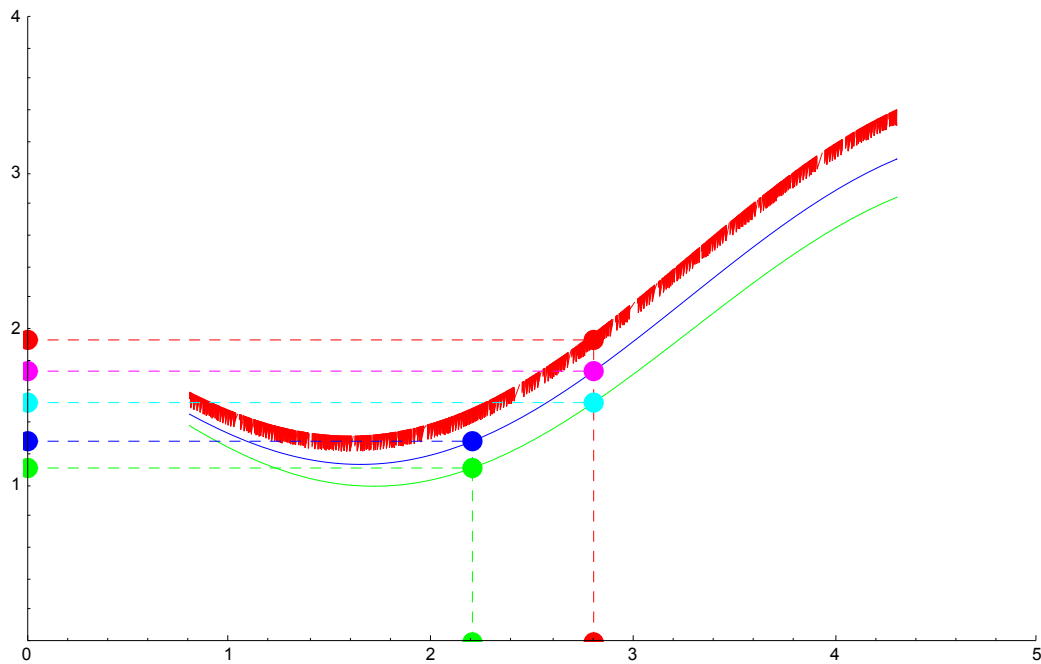


```
ll[i_] := Table[{N[105 x], 1015 f[N[x + 1]]}, {x, - $\frac{i}{10^5}$ ,  $\frac{i}{10^5}$ ,  $\frac{2 i}{10^7}$ }]
```

```
GraphicsGrid[
  Partition[
    Table[
      ListPlot[ll[i], Joined -> True,
        PlotStyle -> {Thickness[0.005], Red}], {i, 4, 1, -1}], 2]]
```



Tutto insieme



Catastrofi

cancellazione

```
Clear[b, f, f1]
```

```
f[b_] := 1 - Sqrt[1 + b^2]
```

```
f[10^-8]
```

$$1 - \frac{\sqrt{10\,000\,000\,000\,000\,001}}{100\,000\,000}$$

```
f[10.^-8]
```

```
0.
```

```
N[f[10.^-8], 30]
```

```
0.
```

```
N[f[10^-8], 30]
```

$$-4.999999999999999875000000000000 \times 10^{-17}$$

```
N[Sqrt[1 + b^2], 40] /. b -> 10^-8
```

$$1.000000000000000049999999999999987500000$$

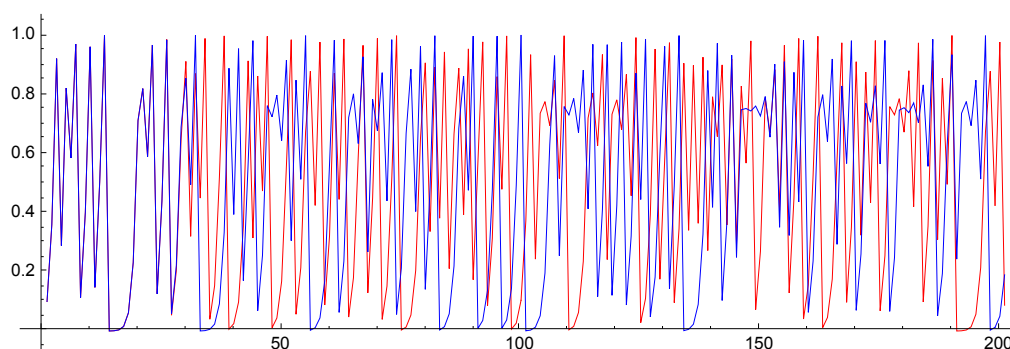
```
Series[1 - Sqrt[1 + b^2], {b, 0, 2}]
```

$$-\frac{b^2}{2} + O[b]^3$$

```
f1[b_]:= -b^2/2
f1[10.^-8]
-5. × 10-17
```

Instabilità

```
Clear[f];
f[x_]:=4. x(1-x)
n=200;
lp[z_, c_] := ListPlot[NestList[f, 0.1`+N[z], n], Joined → True, PlotStyle → c];
Show[lp[0, Red], lp[1/1010, Blue], AspectRatio → 1/3]
```



Serie a termini alterni

```
ss = Series[Exp[x], {x, 0, 10}]
1 + x +  $\frac{x^2}{2}$  +  $\frac{x^3}{6}$  +  $\frac{x^4}{24}$  +  $\frac{x^5}{120}$  +  $\frac{x^6}{720}$  +  $\frac{x^7}{5040}$  +  $\frac{x^8}{40320}$  +  $\frac{x^9}{362880}$  +  $\frac{x^{10}}{3628800}$  + O[x]11
sn = ss // Normal
1 + x +  $\frac{x^2}{2}$  +  $\frac{x^3}{6}$  +  $\frac{x^4}{24}$  +  $\frac{x^5}{120}$  +  $\frac{x^6}{720}$  +  $\frac{x^7}{5040}$  +  $\frac{x^8}{40320}$  +  $\frac{x^9}{362880}$  +  $\frac{x^{10}}{3628800}$ 
sn = Normal[Series[Exp[x], {x, 0, 10000}]];
```

calcolo per $x = -10$

```
sn /. x → -10.
0.0000453999
1 / (sn /. x → 10.)
0.0000453999
```



```
N[Exp[-10]]  
0.0000453999
```

calcolo per $x = -100$

```
sn /. x -> -100.  
5.14084 × 1026  
1 / (sn /. x -> 100.)  
3.72008 × 10-44  
N[Exp[-100]]  
3.72008 × 10-44
```

Calcolo della derivata

f è una funzione

```
f=Cos[x]  
Cos[x]
```

f1 la sua derivata

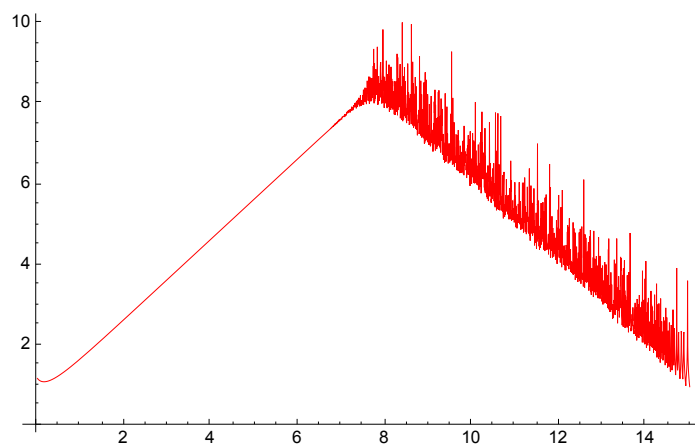
```
f1=D[f,x]  
-Sin[x]
```

f1app1 la sua approssimazione con il rapporto incrementale

```
f1app1[h_]:= (Cos[x+h]-Cos[x])/h
```

L10 definisce la funzione $-\text{Log}_{10} |x|$ con una protezione ...

```
L10[x_]:=If[Abs[x]<10-20,20,N[-Log[10,Abs[x]]]];  
err[k_]:=L10[(f1-f1app1[10-k])/x->1.1]  
Plot[err[h],{h,0,15},PlotStyle->{Red}]
```



```
Series[flapp1[h]-f1,{h,0,3}]
```

$$-\frac{1}{2} \cos[x] h + \frac{1}{6} \sin[x] h^2 + \frac{1}{24} \cos[x] h^3 + O[h]^4$$

```
(flapp1[h]+flapp1[-h])/2
```

$$\frac{1}{2} \left(-\frac{\cos[h-x] - \cos[x]}{h} + \frac{-\cos[x] + \cos[h+x]}{h} \right)$$

```
Together[%]
```

$$\frac{-\cos[h-x] + \cos[h+x]}{2h}$$

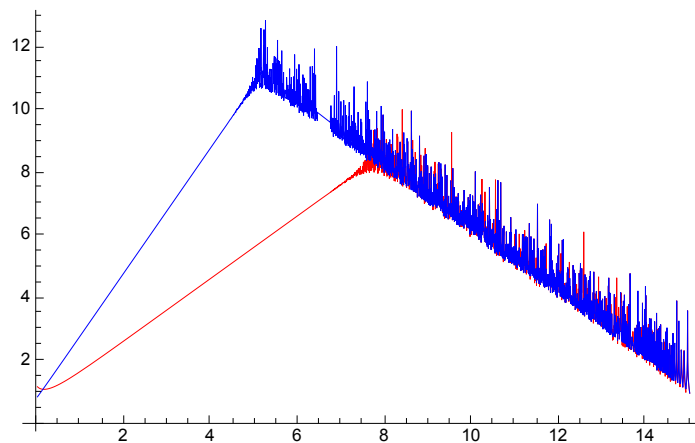
```
flapp2[h_] := (Cos[x+h]-Cos[x-h])/(2h)
```

```
Series[flapp2[h]-f1,{h,0,3}]
```

$$\frac{1}{6} \sin[x] h^2 + O[h]^4$$

```
err2[h_] := L10[(f1-flapp2[10^-h])/ .x->1.1]
```

```
Plot[{err[h], err2[h]}, {h, 0, 15}, PlotStyle -> {Red, Blue}]
```



```
Series[flapp2[h]-f1,{h,0,5}]
```

$$\frac{1}{6} \sin[x] h^2 - \frac{1}{120} \sin[x] h^4 + O[h]^6$$

```
Series[flapp2[h/2]-f1,{h,0,5}]
```

$$\frac{1}{24} \sin[x] h^2 - \frac{\sin[x] h^4}{1920} + O[h]^6$$

```
Solve[{a+b==1,a/6+b/24==0}]
```

```
{}
```

```
-1/3 flapp2[h] + 4/3 flapp2[h/2]
```

$$\frac{4 \left(-\cos\left[\frac{h}{2}-x\right] + \cos\left[\frac{h}{2}+x\right] \right)}{3h} - \frac{-\cos[h-x] + \cos[h+x]}{6h}$$

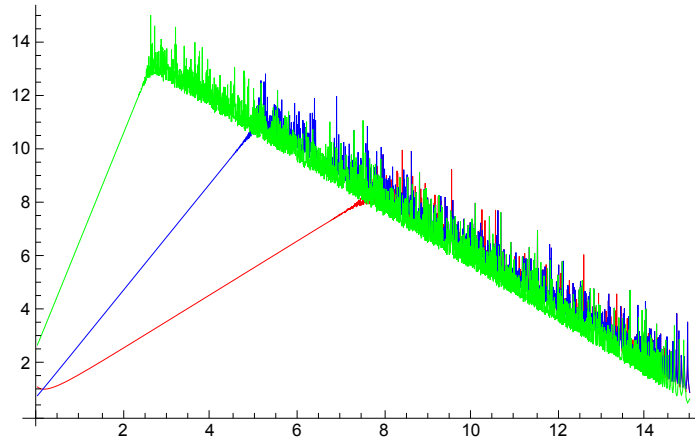
```
flapp3[h_] := -1/3 flapp2[h] + 4/3 flapp2[h/2]
```

```
Series[f1app3[h]-f1,{h,0,5}]
```

$$\frac{1}{480} \sin[x] h^4 + O[h]^6$$

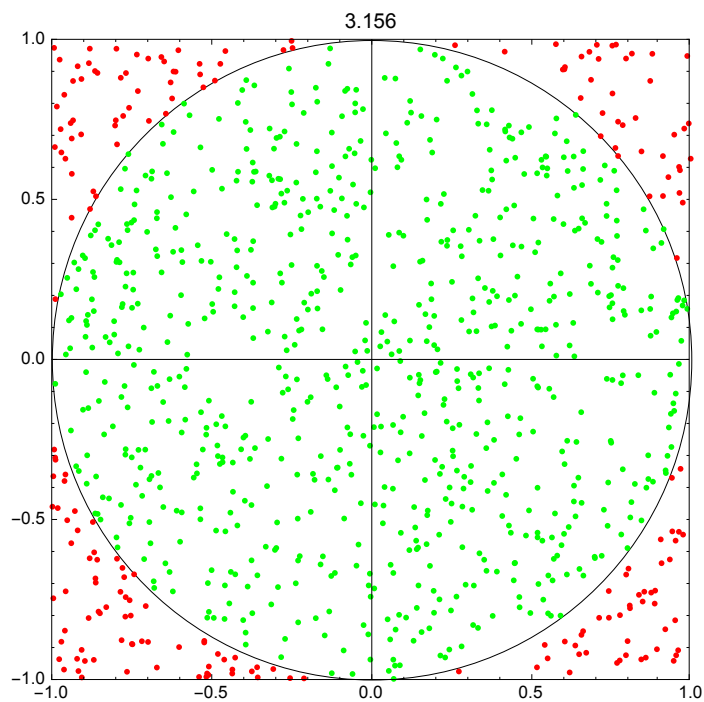
```
err3[h_]:=L10[(f1-f1app3[10^-h])/x->1.1]
```

```
Plot[{err[h],err2[h],err3[h]},{h,0,15},PlotStyle->{Red,Blue,Green}]
```

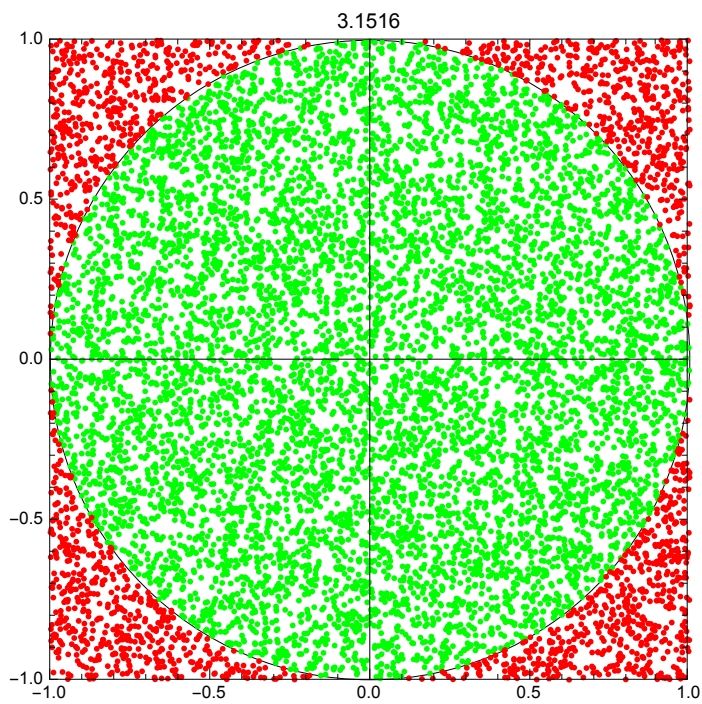


Calcolo di π con un metodo Montecarlo

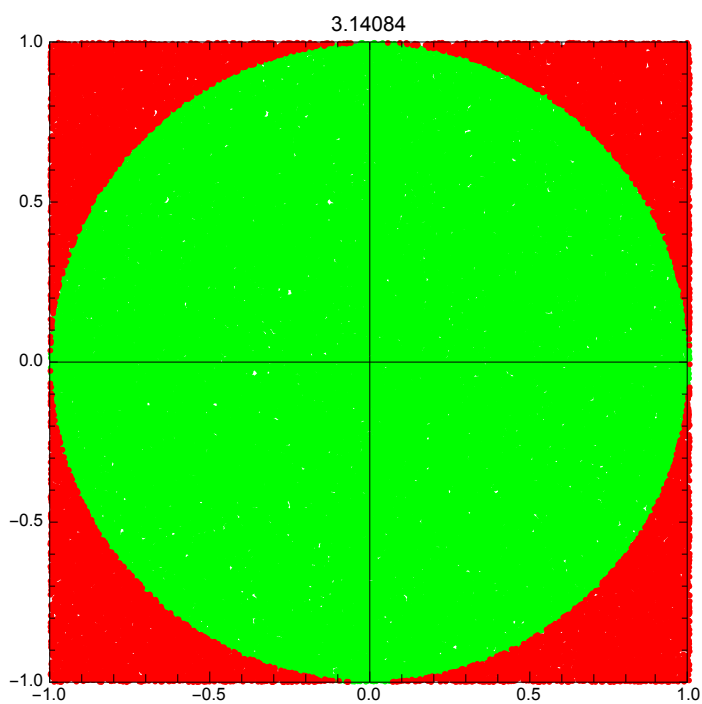
1000 punti



10000 punti



100000 punti



programma semplificato

```
rand:=Random[Real,{-1,1}];
```

```
i=0;  
j=1000000;  
Do[If[rand^2+rand^2 < 1,i++],{j}];  
N[4 i/j]  
3.14248
```

Con un generatore cattivo

