

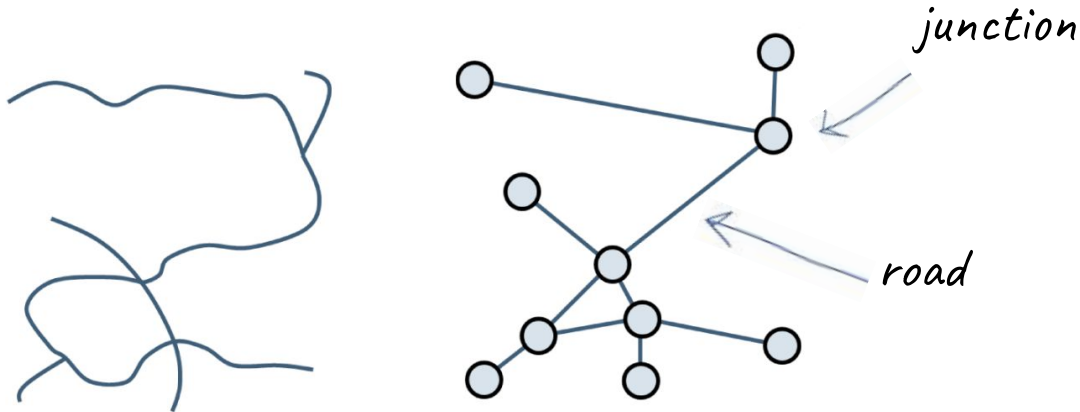
Consiglio Nazionale  
delle Ricerche

# Alternative Routing

# The Road Network

The road network is described as a **weighted directed graph**:

- **nodes** represent intersections/junctions
- **edges** represent roads/streets
- **edge weights** represent road length or expected travel time



# The Routing Problem

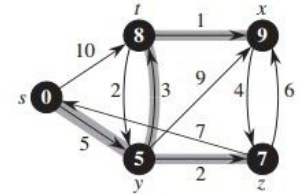
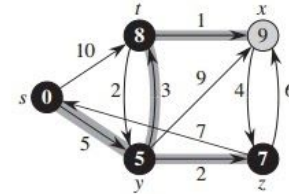
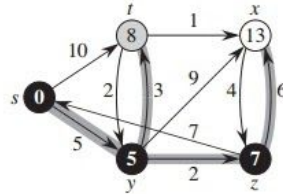
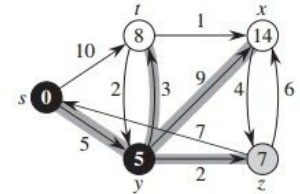
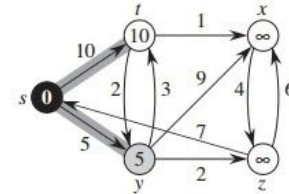
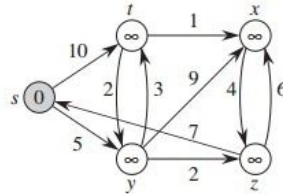
What is the “best” route to reach a destination from an origin?

- What does “good” mean? Its subjective (i.e., max. route dissimilarity, min. length, etc)
- The “best” route for an individual is not necessarily the best anymore when many vehicles are travelling at the same time

# Shortest/Fastest route

- The default solution to routing is providing the shortest/fastest path (Dijkstra algorithm)

```
1 function Dijkstra(Graph, source):
2
3   for each vertex v in Graph.Vertices:
4     dist[v] ← INFINITY
5     prev[v] ← UNDEFINED
6     add v to Q
7   dist[source] ← 0
8
9   while Q is not empty:
10    u ← vertex in Q with min dist[u]
11    remove u from Q
12
13    for each neighbor v of u still in Q:
14      alt ← dist[u] + Graph.Edges(u, v)
15      if alt < dist[v]:
16        dist[v] ← alt
17        prev[v] ← u
18
19  return dist[], prev[]
```



# Is the shortest enough?

In many scenarios, the shortest path is not enough:

- *Example 1: navigation systems*  
(longer) **alternative routes** with desirable properties
- *Example 2: humanitarian aid goods transport*  
distribution of vehicles on **non-overlapping routes** increases the chances that goods will be delivered
- *Example 3: emergencies*  
Alternative, **safe routes** in case of earthquakes, terrorist attacks, evacuation plans

# Alternative Routing Methods

Alternative Routing (AR) aims to generate  
a set of  **$k$  good alternative** routes  
between an **origin** and a **destination**

# Route generation framework

Input:

- road network  $G$
- an int  $k > 1$
- an  $(o, d)$  pair

Output:

- $k$  alternative paths



# k-Shortest Paths

*Naive solution:* generate **k-shortest paths** between an origin and a destination

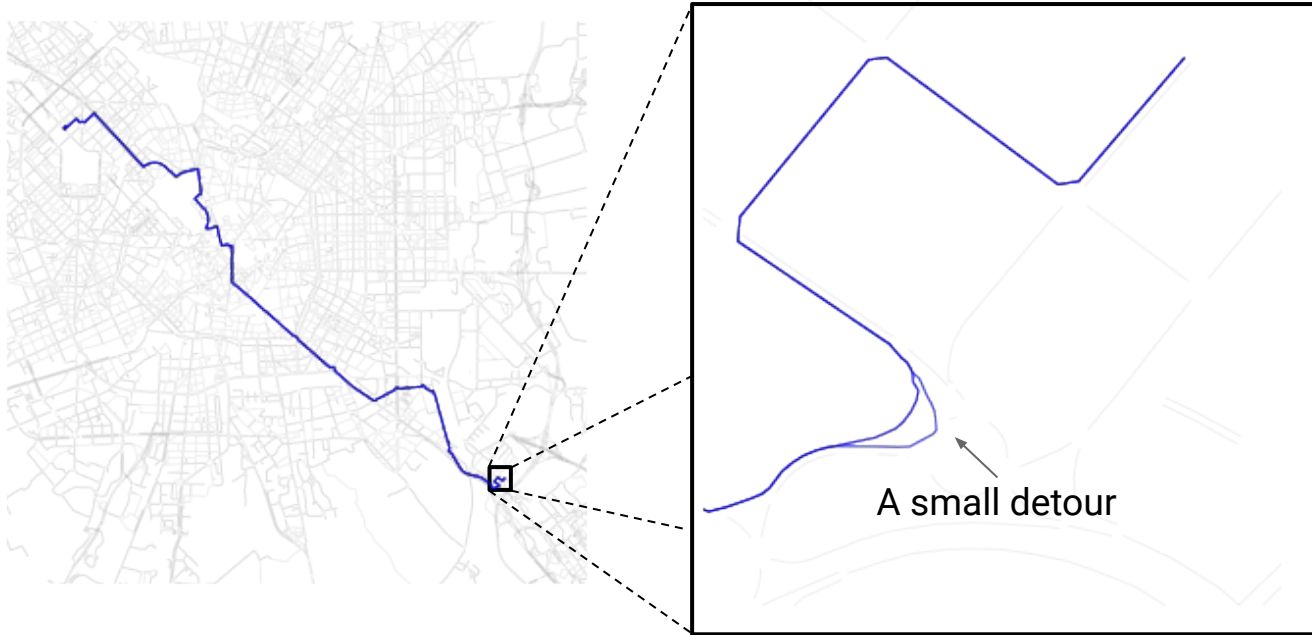
*Limitations:*

- the k-shortest path solutions **fail** to provide significant **path diversification**
- the routes exhibit a **99% overlap**, with minor differences (cutting a corner or small detours)





# k-Shortest Paths



# k-Disjoint Paths

Generate **k-shortest disjoint paths**, i.e., **k** alternative paths with **no common edges**

- In practice, we put the edge weights of the current shortest path to infinity
- This enforces the diversity among paths

*Limitations:*

- routes **significantly deviate** from the shortest path
  - increased travel time and length
- **no guarantee** that **k** disjoint paths exists



# Alternative Routing Approaches

Several existing Alternative Routing approaches lie between the k-shortest path and k-shortest disjoint paths:

## 1. Edge Weight Approaches

## 2. Plateau Approaches

## 3. Dissimilarity Approaches

# Edge Weight Approaches

Compute the shortest paths **iteratively**:

- at each iteration, **manipulate** the road network's **edge weights**
- edge weight manipulation involves the **randomization** of the weights or a **cumulative penalization** of the shortest path's edges



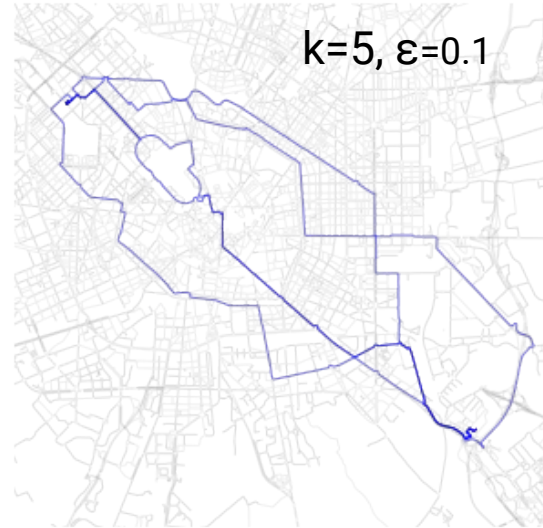
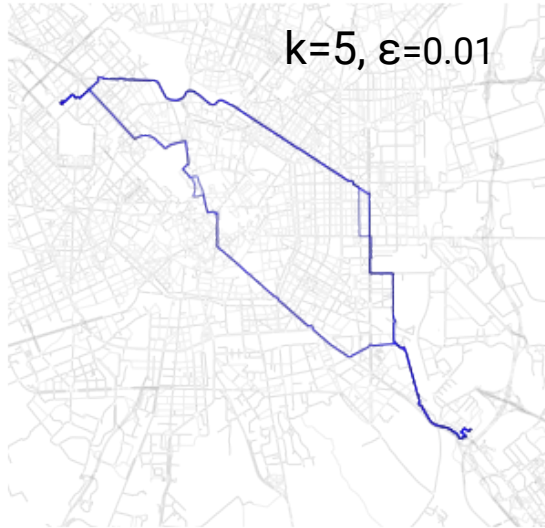
# Path Penalization

Until # of alternative paths  $< k$ :

- Compute the shortest path using the current edge weights
- Apply a **penalization factor  $\epsilon$**  to each edge weight in the shortest path

$$\forall e \in p_s, w(e) = w(e)(1 + \epsilon)$$

# Path Penalization



- The penalty factor  $\epsilon$  controls the degree of deviation of an alternative path from previously generated ones
- It influences the geographic distribution of alternative paths

# Graph Randomization

Until # of alternative paths < k:

- Compute the shortest path using the current edge weights
- Randomize the weights of **all edges in G** adding a value  $v$  drawn from a normal distribution

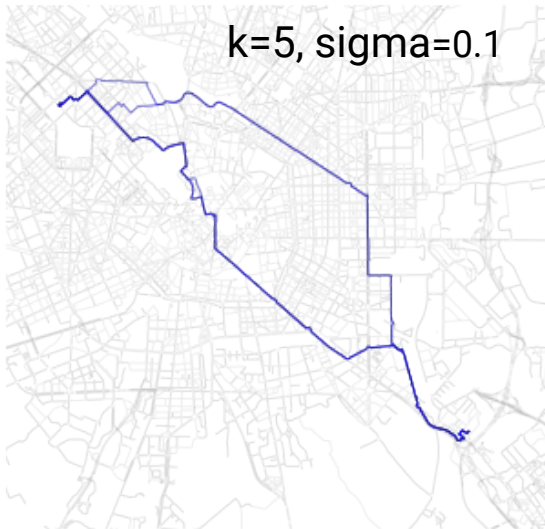
$$\forall e \in G, w(e) = w(e) + v$$

$$N(0, w(e)^2 \cdot \sigma^2)$$

normal distribution

# Graph Randomization

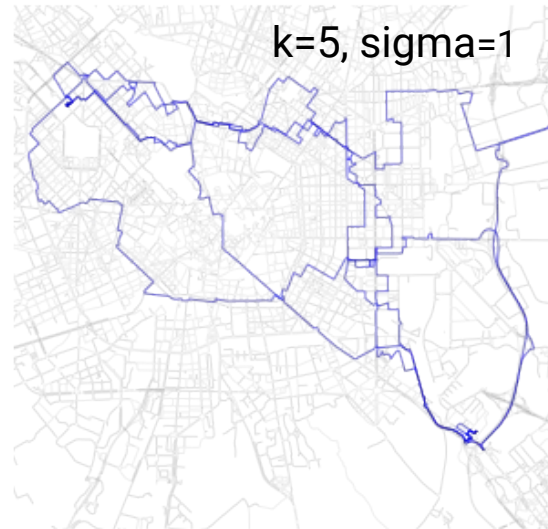
k=5, sigma=0.1



k=5, sigma=0.2



k=5, sigma=1





# Path Randomization

Until # of alternative paths  $< k$ :

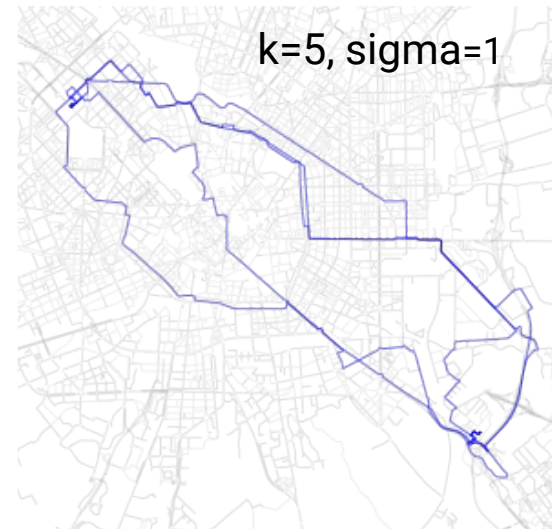
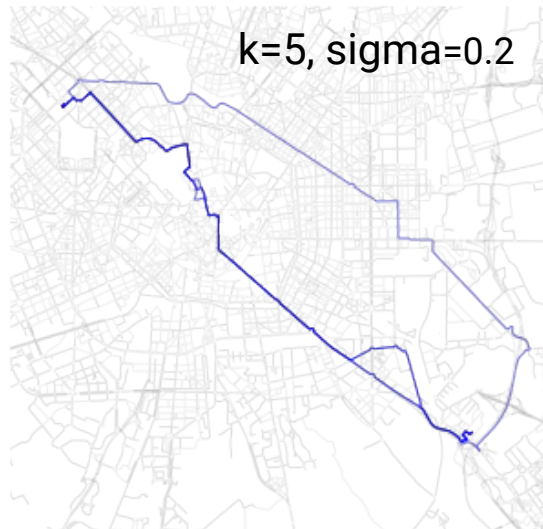
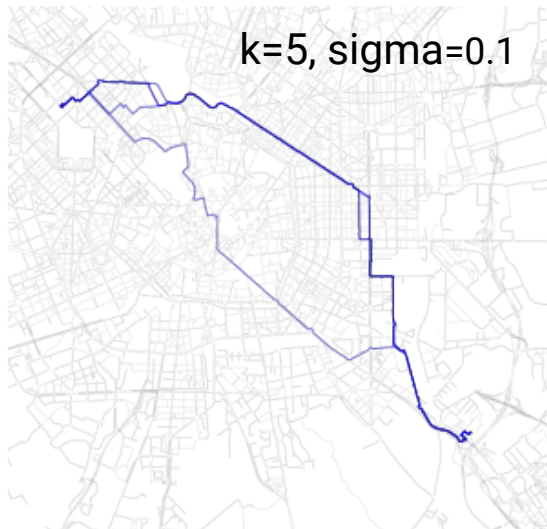
- Compute the shortest path using the current edge weights
- Randomize the weights of the shortest path adding a value  $v$  drawn from a normal distribution

$$\forall e \in p_s, w(e) = w(e) + v$$

$$N(0, w(e)^2 \cdot \sigma^2)$$

normal distribution

# Path Randomization





Which ones of the AR algorithms are deterministic?

- A. K-shortest ✓
- B. K-disjoint ✓
- C. Path Randomization
- D. Path Penalization ✓
- E. Graph Randomization



In which AR algorithm weight can also decrease?

- A. Path Randomization ✓
- B. Path Penalization
- C. Graph Randomization ✓



What is the range of possible path counts between locations O and D that Path Penalization may return after N iterations?

Minimum:

- 0 paths if O and D are not connected.
- 1 path if only the fastest path is found.

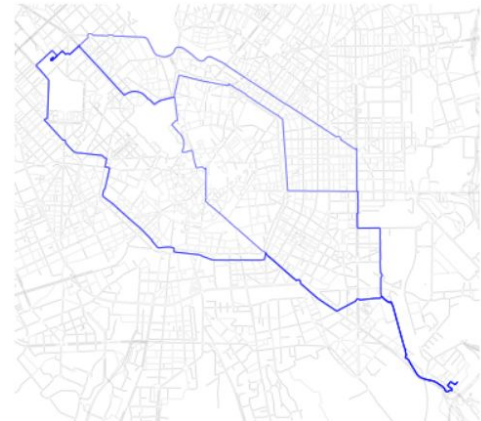
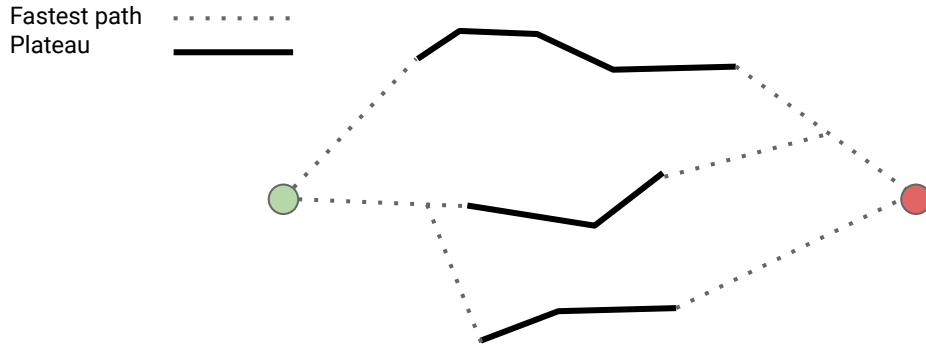
Maximum:

- N paths if a new path is discovered at each of the N iterations.

# Plateau Approaches

Build two shortest-path trees, one from the source and one from the destination:

- identify their common branches (**plateaus**)
- select top-k plateaus by length
- append the shortest paths from the source to the plateau's first edge and from the last edge to the target



# Dissimilarity Approaches

Dissimilarity approaches generate  $k$  alternative paths that satisfy a **dissimilarity constraint** and a desired **property**

- $k$ -Shortest Paths with Limited Overlap
- $k$ -Dissimilar Paths with Minimum Collective Length
- $k$ -Most Diverse Near Shortest Paths

# k-Most Diverse Near Shortest Paths (KMD)

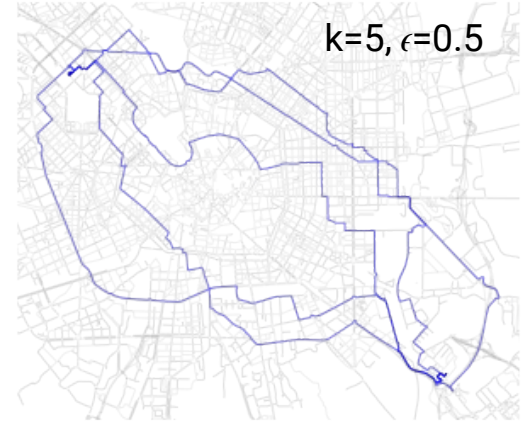
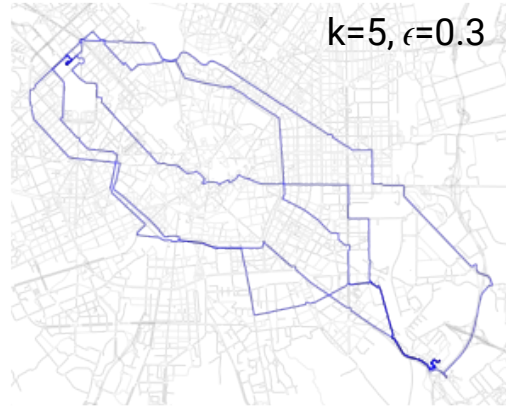
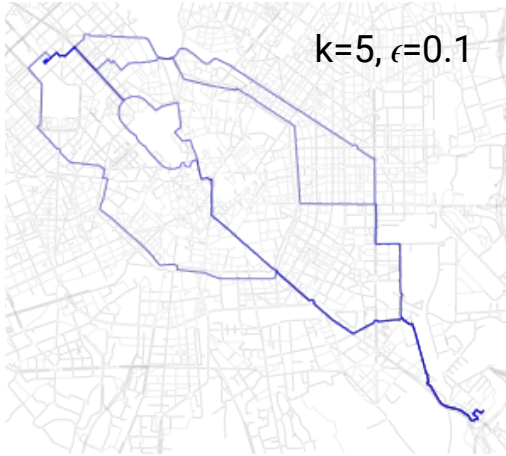
- KMD generates  $k$  routes with the **highest dissimilarity** while still adhering to a user-defined **cost threshold**  $\epsilon$
- It is **NP-Hard**: we need a **heuristic**

Given an origin  $o$  and a destination  $d$ :

1. Define a cost threshold  $c \cdot (1+\epsilon)$  for a path to be Near Shortest (NSP)
2. Until no more near-shortest paths can be found, repeat:
  - generate a new NSP  $\mathbf{p}$  and adds it to the set of NSPs  $\mathbf{S}$ .
    - Use path penalization algorithm
  - generate all possible **subsets** of  $\mathbf{S}$  with  $k$  elements containing  $\mathbf{p}$  and identifies  $S_{div}$  as the most diverse one (based on jaccard).  
If it is the most diverse found up to this point  $P_{kmd} = S_{div}$ .
3. Return the subset of  $k$  paths with the highest diversity, i.e.,  $P_{kmd}$ .



# k-Most Diverse Near Shortest Paths (KMD)



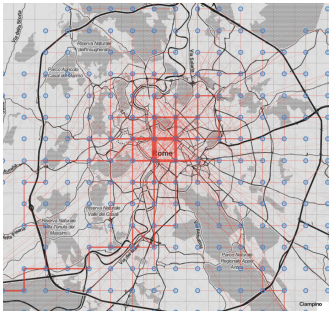
# Traffic Assignment Problem (TA)

Given a demand, assign each trip with a route

# Traffic Assignment Problem (TA)

Given a demand, assign each trip with a route

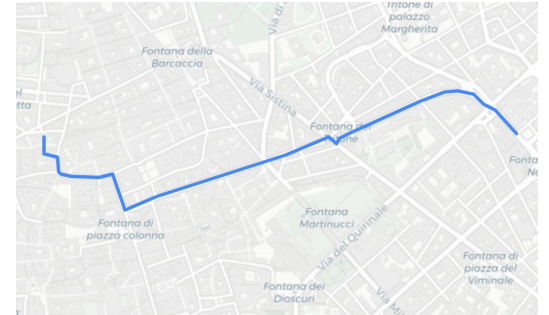
collection of origin-destination pairs



a single origin-destination pair



sequence of road edges



# AON vs ITA

**All or Nothing (AON):** assign the fastest path to each trip

- It creates concentration of the traffic on a few routes

**Incremental Traffic Assignment (ITA):** extends AON incorporating the dynamic travel time changes within a road edge

- create  $n$  splits of the demand (typically  $n = 4$  with 40%, 30%, ... 10%)
- Split 1: trips are assigned using AON; each edge's travel time is updated using the BPR function (Bureau of Public Roads)
- Split 2: trips are assigned using AON, considering the updated travel time
- Iterate

# METIS

---

**Algorithm 1: METIS**

---

**Input** : road network  $G$ , mobility demand  $D$ , penalization factor  $p$ , slow factor  $s$

**Output**: sequence of assigned routes  $R$

// Initialization Phase

```
1  $K_{\text{road}}^{(\text{source})}, K_{\text{road}}^{(\text{end})} \leftarrow KRoadEstimation(G, D);$   
2  $R \leftarrow \emptyset;$ 
```

// Perform the Traffic Assignment (TA)

```
3 foreach  $j = (o, d, t) \in D$  do
```

```
    // Apply the Forward-Looking Edge Penalization (FLEP)
```

```
4  $H \leftarrow FLEP(G, R, D, (p, s), t);$ 
```

```
    // Generate a set of k candidates on the penalized road network
```

```
5  $P \leftarrow kMDNSP(H, o, d);$ 
```

```
    // Select the route that minimizes the score function
```

```
6  $r \leftarrow RouteSelection(P, K_{\text{road}}^{(\text{source})}, K_{\text{road}}^{(\text{end})});$ 
```

```
    // Update the assigned routes set
```

```
7  $R \leftarrow R \cup \{r\};$ 
```

```
8 return  $R;$ 
```

---

# METIS

For each trip request (trips are time-sorted):

- **Forward-Looking Edge Penalization (FLEP)**
  - discourage selection of congested edges

---

**Algorithm 1: METIS**

---

**Input** : road network  $G$ , mobility demand  $D$ , penalization factor  $p$ , slow factor  $s$   
**Output**: sequence of assigned routes  $R$

// Initialization Phase

```
1  $K_{road}^{(source)}, K_{road}^{(end)} \leftarrow KRoadEstimation(G, D);$ 
2  $R \leftarrow \emptyset;$ 

// Perform the Traffic Assignment (TA)
3 foreach  $j = (o, d, t) \in D$  do
4   // Apply the Forward-Looking Edge Penalization (FLEP)
    $H \leftarrow FLEP(G, R, D, (p, s), t);$ 
5   // Generate a set of k candidates on the penalized road network
    $P \leftarrow kMDNSP(H, o, d);$ 
6   // Select the route that minimizes the score function
    $r \leftarrow RouteSelection(P, K_{road}^{(source)}, K_{road}^{(end)});$ 
7   // Update the assigned routes set
    $R \leftarrow R \cup \{r\};$ 
8 return  $R;$ 
```

---

# METIS

For each trip request (trips are time-sorted):

- **Forward-Looking Edge Penalization (FLEP)**
  - discourage selection of congested edges
- **Alternative Routing**
  - generate routed candidates

---

**Algorithm 1: METIS**

---

**Input** : road network  $G$ , mobility demand  $D$ , penalization factor  $p$ , slow factor  $s$   
**Output**: sequence of assigned routes  $R$

// Initialization Phase

```
1  $K_{road}^{(source)}, K_{road}^{(end)} \leftarrow KRoadEstimation(G, D);$ 
2  $R \leftarrow \emptyset;$ 
```

// Perform the Traffic Assignment (TA)

```
3 foreach  $j = (o, d, t) \in D$  do
    // Apply the Forward-Looking Edge Penalization (FLEP)
    4  $H \leftarrow FLEP(G, R, D, (p, s), t);$ 
    // Generate a set of k candidates on the penalized road network
    5  $P \leftarrow kMDNSP(H, o, d);$ 
    // Select the route that minimizes the score function
    6  $r \leftarrow RouteSelection(P, K_{road}^{(source)}, K_{road}^{(end)});$ 
    // Update the assigned routes set
    7  $R \leftarrow R \cup \{r\};$ 
8 return  $R;$ 
```

---

# METIS

For each trip request (trips are time-sorted):

- **Forward-Looking Edge Penalization (FLEP)**
  - discourage selection of congested edges
- **Alternative Routing**
  - generate routed candidates
- **Route Scoring**
  - rank routes based on popularity and capacity

---

**Algorithm 1: METIS**

---

**Input** : road network  $G$ , mobility demand  $D$ , penalization factor  $p$ , slow factor  $s$   
**Output**: sequence of assigned routes  $R$

// Initialization Phase

```
1  $K_{road}^{(source)}, K_{road}^{(end)} \leftarrow KRoadEstimation(G, D);$ 
2  $R \leftarrow \emptyset;$ 

// Perform the Traffic Assignment (TA)
3 foreach  $j = (o, d, t) \in D$  do
    // Apply the Forward-Looking Edge Penalization (FLEP)
4      $H \leftarrow FLEP(G, R, D, (p, s), t);$ 
    // Generate a set of k candidates on the penalized road network
5      $P \leftarrow kMDNSP(H, o, d);$ 
    // Select the route that minimizes the score function
6      $r \leftarrow RouteSelection(P, K_{road}^{(source)}, K_{road}^{(end)});$ 
    // Update the assigned routes set
7      $R \leftarrow R \cup \{r\};$ 
8 return  $R;$ 
```

---



# Forward-Looking Edge Penalization (FLEP)

- Penalizing road edges weight reflects dynamic changes in travel time due to traffic volume
  - Existing methods penalize the entire routes assigned to vehicles
  - FLEP estimates vehicle current position applying penalties to the un-visited edges only

---

## Algorithm 1: METIS

---

**Input** : road network  $G$ , mobility demand  $D$ , penalization factor  $p$ , slow factor  $s$   
**Output** : sequence of assigned routes  $R$

// Initialization Phase

```
1  $K_{\text{road}}^{(\text{source})}, K_{\text{road}}^{(\text{end})} \leftarrow KRoadEstimation(G, D);$ 
2  $R \leftarrow \emptyset;$ 

// Perform the Traffic Assignment (TA)
3 foreach  $j = (o, d, t) \in D$  do
    // Apply the Forward-Looking Edge Penalization (FLEP)
    4  $H \leftarrow FLEP(G, R, D, (p, s), t);$ 

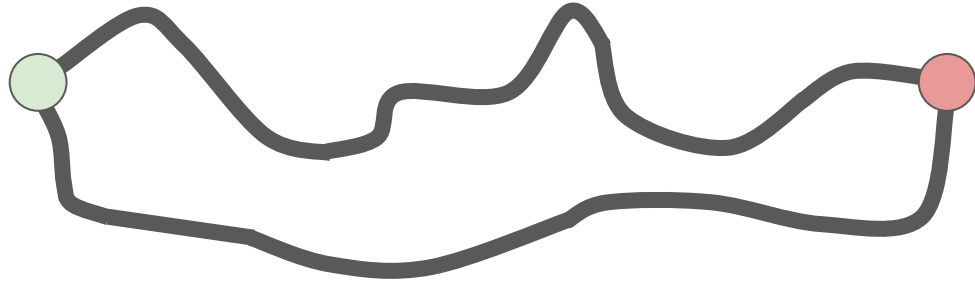
    // Generate a set of k candidates on the penalized road network
    5  $P \leftarrow kMDNSP(H, o, d);$ 

    // Select the route that minimizes the score function
    6  $r \leftarrow RouteSelection(P, K_{\text{road}}^{(\text{source})}, K_{\text{road}}^{(\text{end})});$ 

    // Update the assigned routes set
    7  $R \leftarrow R \cup \{r\};$ 
8 return  $R;$ 
```

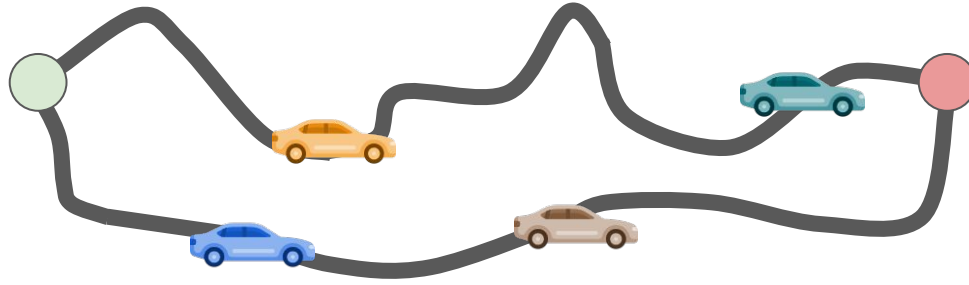
---

# Forward-Looking Edge Penalization (FLEP)



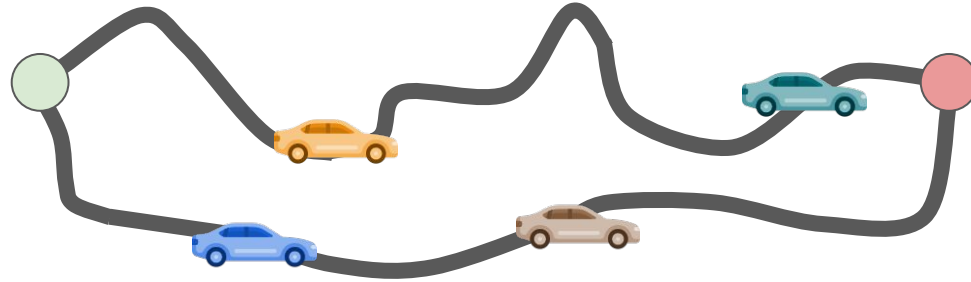
# Forward-Looking Edge Penalization (FLEP)

The position of  
already departed  
vehicles is **estimated**.



# Forward-Looking Edge Penalization (FLEP)

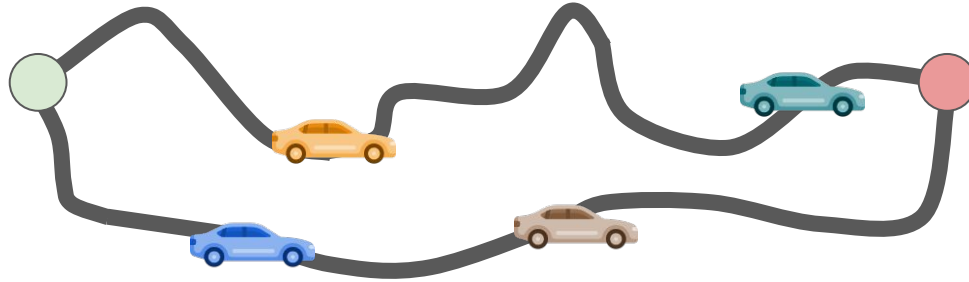
The position of already departed vehicles is **estimated**.



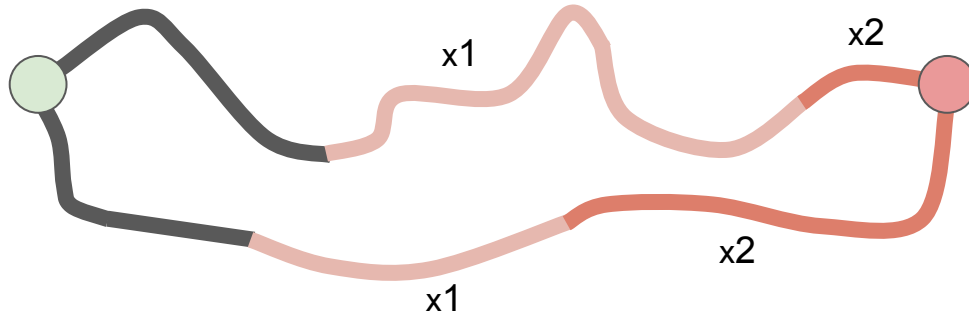
For each vehicle we **penalize** the edges **projected** to be visited by that vehicle

# Forward-Looking Edge Penalization (FLEP)

The position of already departed vehicles is **estimated**.



The penalized road network at the current time



# Alternative Routing

After the FLEP phase:

- Apply **kMD** [1] on the penalized road network to obtain  $k$  ( $=3$ ) alternative routes



---

## Algorithm 1: METIS

---

**Input** : road network  $G$ , mobility demand  $D$ , penalization factor  $p$ , slow factor  $s$   
**Output**: sequence of assigned routes  $R$

// Initialization Phase

- 1  $K_{\text{road}}^{(\text{source})}, K_{\text{road}}^{(\text{end})} \leftarrow \text{KRoadEstimation}(G, D)$ ;
- 2  $R \leftarrow \emptyset$ ;

// Perform the Traffic Assignment (TA)

- 3 **foreach**  $j = (o, d, t) \in D$  **do**
  - // Apply the Forward-Looking Edge Penalization (FLEP)
  - 4  $H \leftarrow \text{FLEP}(G, R, D, (p, s), t)$ ;
  - 5  $P \leftarrow \text{kMDNSP}(H, o, d)$ ;
  - // Select the route that minimizes the score function
  - 6  $r \leftarrow \text{RouteSelection}(P, K_{\text{road}}^{(\text{source})}, K_{\text{road}}^{(\text{end})})$ ;
  - // Update the assigned routes set
  - 7  $R \leftarrow R \cup \{r\}$ ;
- 8 **return**  $R$ ;

---

# Route Scoring

After the route generation:

1. Compute a score for each route (based on **K-Road** [2]) that favours high-capacity roads and disfavour popular ones
2. Select the route with the minimum score

$$\frac{\overline{KR_s} \cdot \overline{KR_d}}{\overline{C}}$$

---

## Algorithm 1: METIS

---

**Input** : road network  $G$ , mobility demand  $D$ , penalization factor  $p$ , slow factor  $s$   
**Output** : sequence of assigned routes  $R$

// Initialization Phase  
1  $K_{road}^{(source)}, K_{road}^{(end)} \leftarrow KRoadEstimation(G, D);$   
2  $R \leftarrow \emptyset;$

// Perform the Traffic Assignment (TA)  
3 **foreach**  $j = (o, d, t) \in D$  **do**  
    // Apply the Forward-Looking Edge Penalization (FLEP)  
    4  $H \leftarrow FLEP(G, R, D, (p, s), t);$   
    // Generate a set of k candidates on the penalized road network  
    5  $P \leftarrow kMDNSP(H, o, d);$   
    // Select the route that minimizes the score function  
    6  $r \leftarrow RouteSelection(P, K_{road}^{(source)}, K_{road}^{(end)});$   
    // Update the assigned routes set  
    7  $R \leftarrow R \cup \{r\};$   
8 **return**  $R;$

---

# Route Scoring

$$K_{\text{road}}^{(\text{source})}(e_1) = 2$$

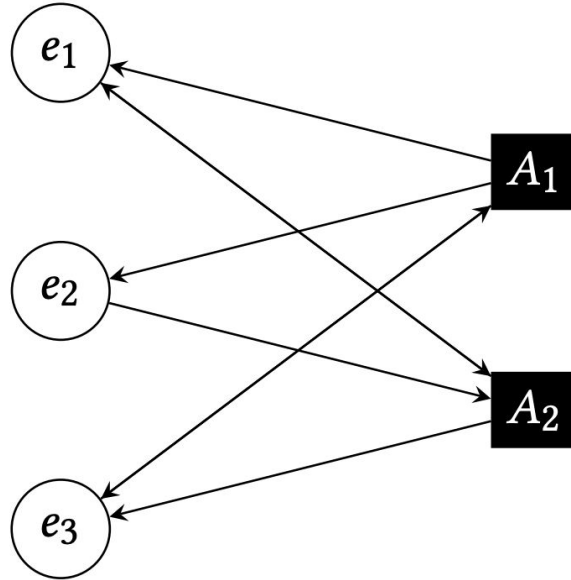
$$K_{\text{road}}^{(\text{end})}(e_1) = 1$$

$$K_{\text{road}}^{(\text{source})}(e_2) = 1$$

$$K_{\text{road}}^{(\text{end})}(e_2) = 1$$

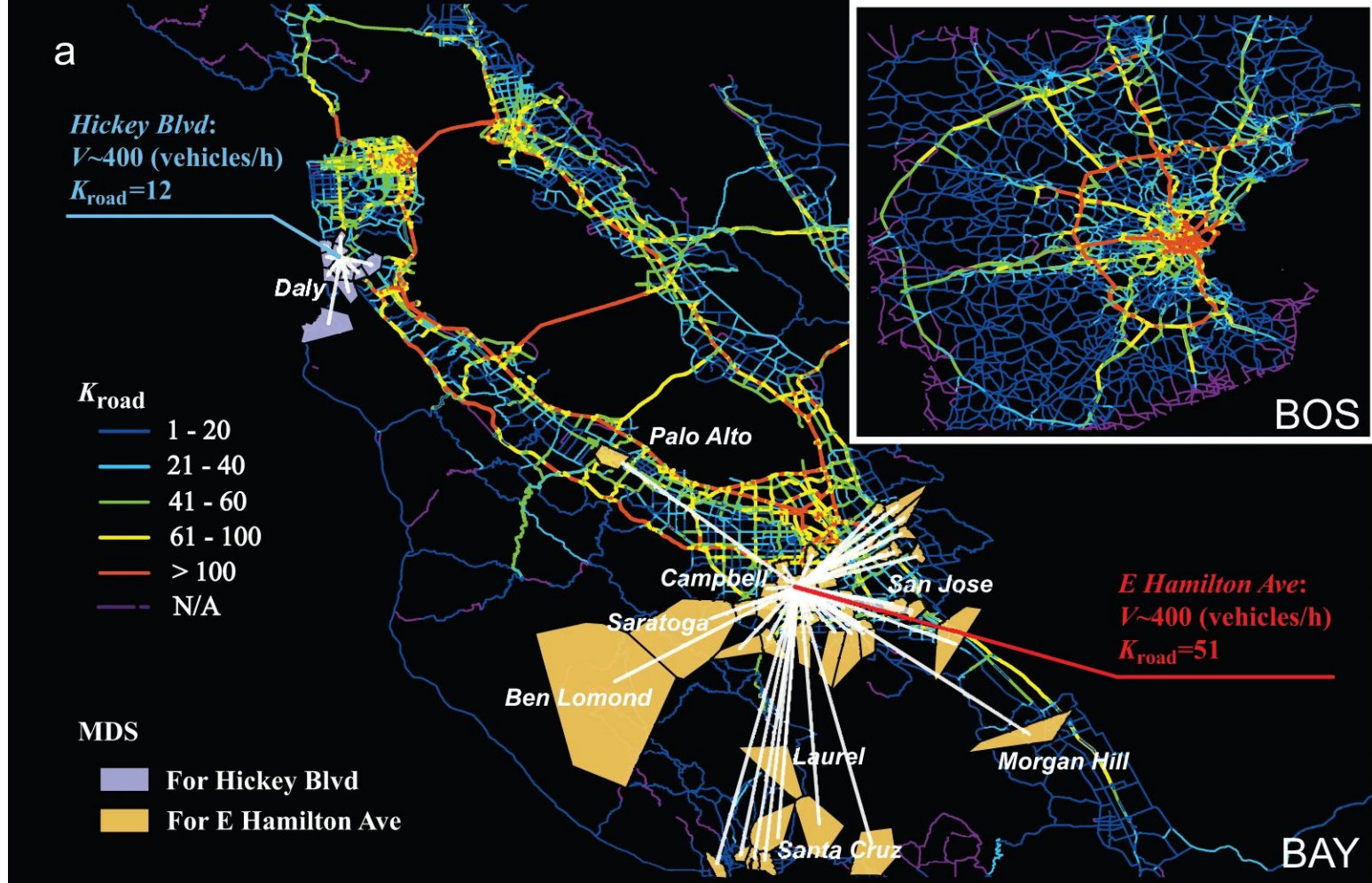
$$K_{\text{road}}^{(\text{source})}(e_3) = 2$$

$$K_{\text{road}}^{(\text{end})}(e_3) = 1$$



$$\frac{\overbrace{KR_s \cdot KR_d}^{\text{Route Popularity}}}{\underbrace{\bar{C}}_{\text{Route capacity}}}$$





# Evaluation Metrics

We can characterize the paths generate by the TA algorithms with several metrics.

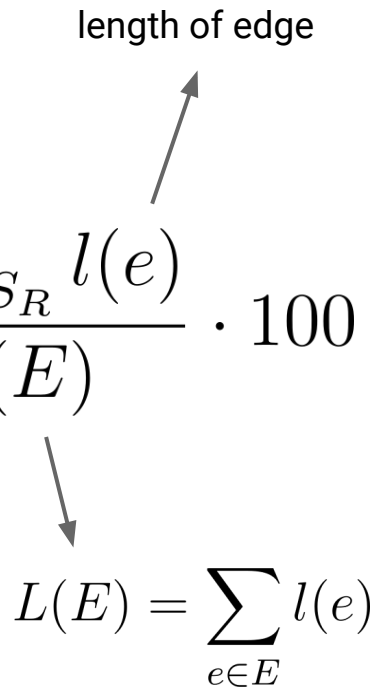
For example:

- Road Coverage
- Redundancy
- Time Redundancy
- CO2 emissions

# Road Coverage (RC)

- Given a set of routes  $R$ , and their edges

$$S_R = \bigcup_{p \in R} \{e \in p\}$$

$$RC(R) = \frac{\sum_{e \in S_R} l(e)}{L(E)} \cdot 100$$


RC characterizes road infrastructure usage:

- A higher road coverage indicates a larger proportion of the  $G$  being utilized

$$L(E) = \sum_{e \in E} l(e)$$

# Redundancy

- Given a set of routes  $R$ , and their edges

$$S_R = \bigcup_{p \in R} \{e \in p\} \quad \text{Red}(R) = \frac{\sum_{p \in R} |p|}{|S_R|}$$

If  $\text{Red}(R) = 1$ , there is no overlap among the routes in  $R$ , while  $\text{Red}(R) = |R|$  when all routes are identical

- average utilization of edges that appear in at least one route

# Time Redundancy (RED)

- Given a set of routes  $R$ , their edges, and a time window  $t$

$$S_R = \bigcup_{p \in R} \{e \in p\} \quad RED(R, t) = \frac{1}{|I|} \sum_{i \in I} RED(R_{i,t})$$

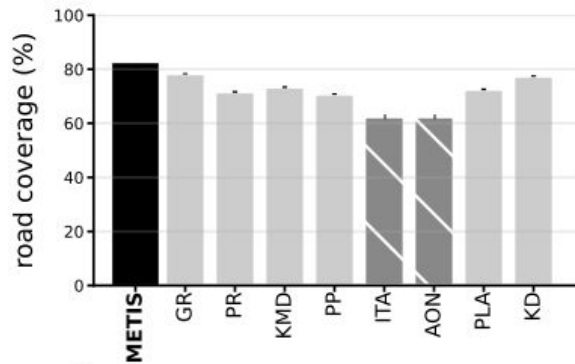
$I = \{t_0, t_0 + \sigma, t_0 + 2\sigma, \dots, t_{max}\}$

$RED(R_{i,t})$  is the Red of trips in  $R$  departed within time interval  $[i, i + t)$ .

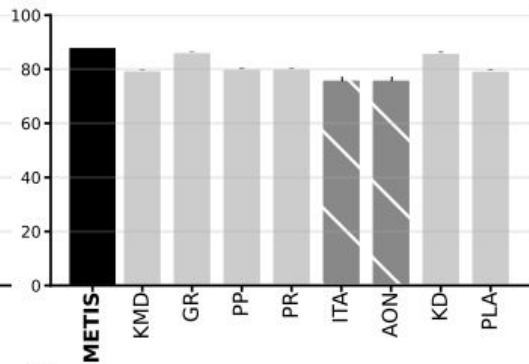
- Low  $RED(R, t)$  indicates that routes close in time are better distributed across edges

# Characterization Metrics

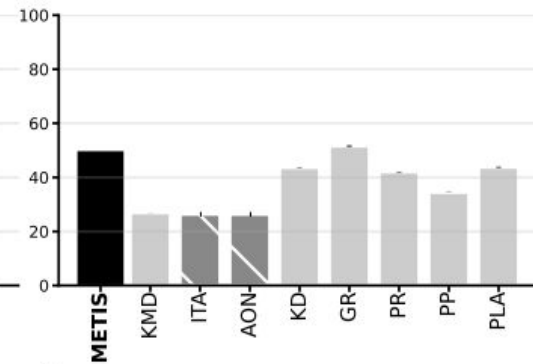
## Florence



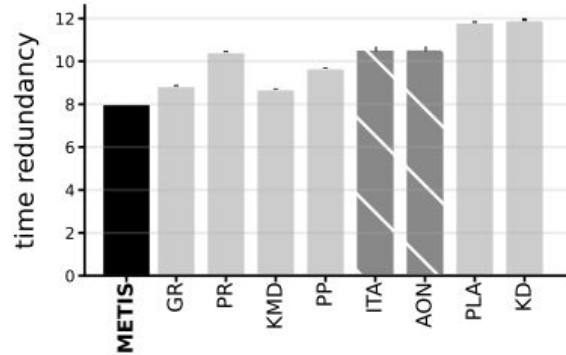
## Milan



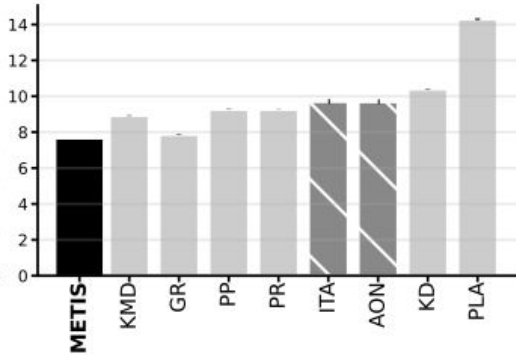
## Rome



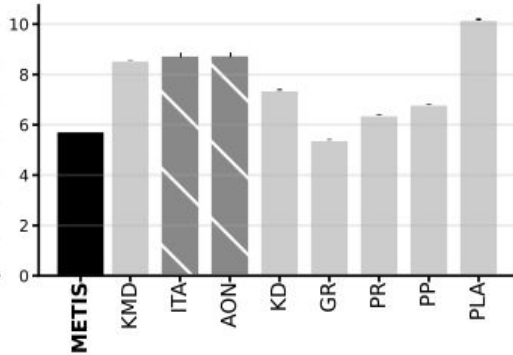
### g)



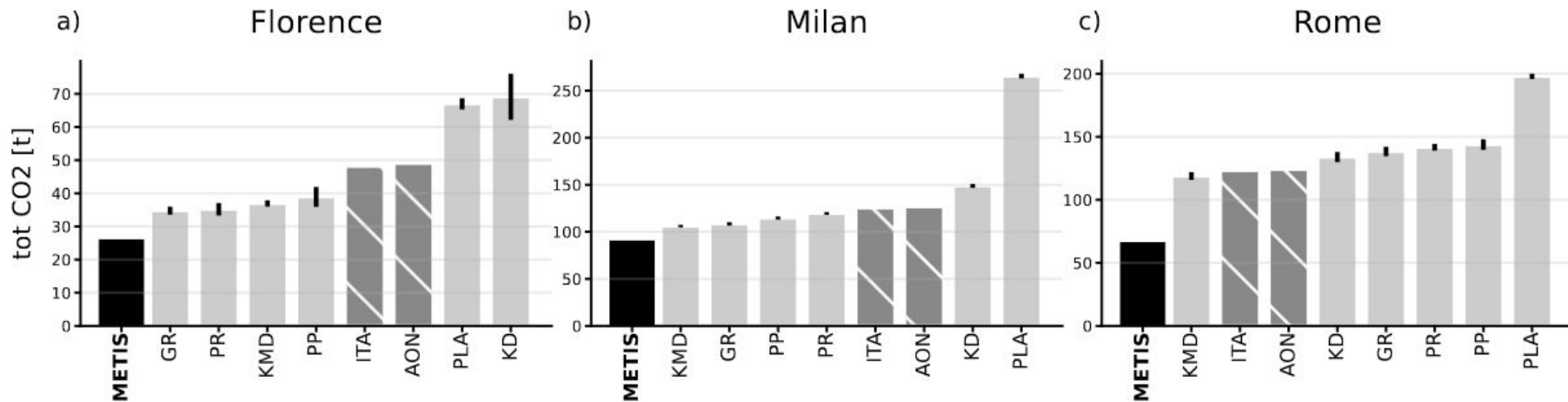
### h)

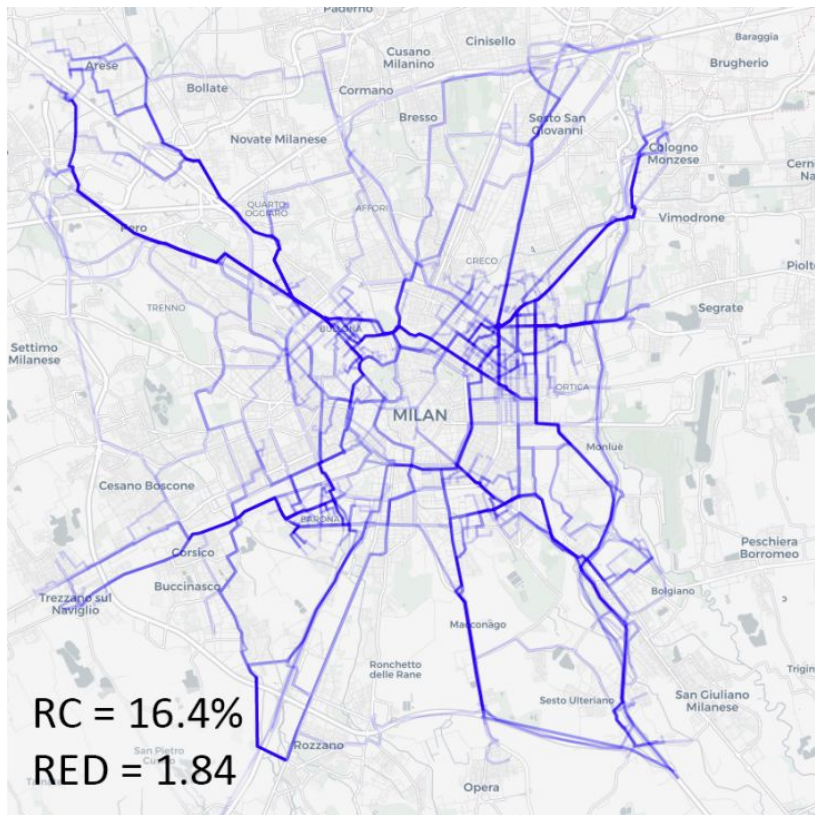


### i)

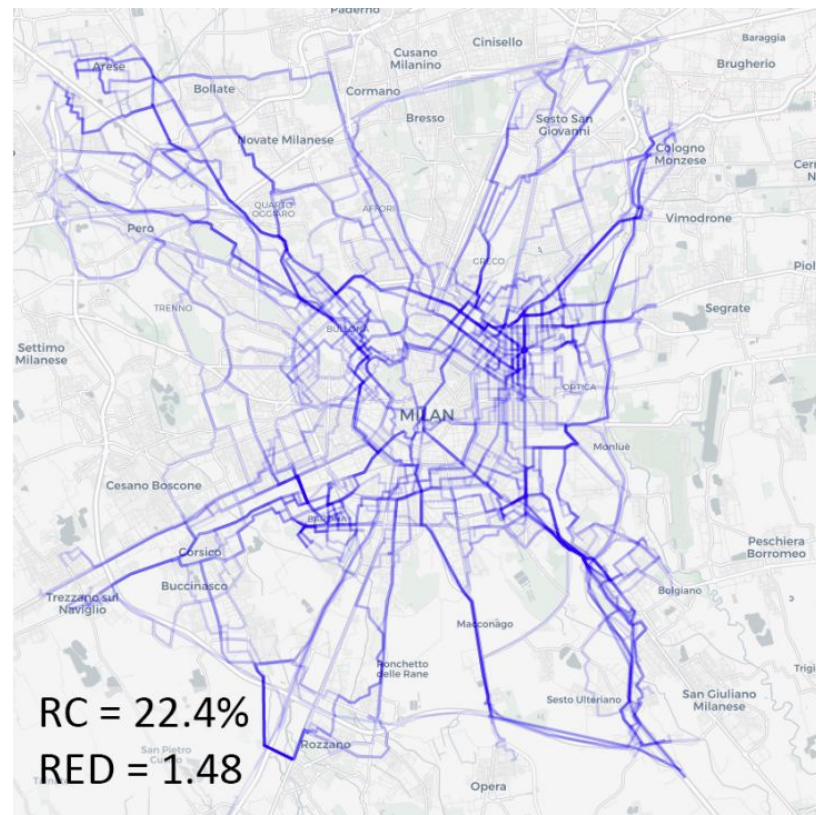


# Characterization Metrics





KMD



METIS



**INTERVALLO**

# **Satellite Navigation Services: What Impact?**



The New York Times

## *Navigation Apps Are Turning Quiet Neighborhoods Into Traffic Nightmares*

The corner of Fort Lee Road and Broad Avenue in Leonia, N.J. With traffic apps suggesting shortcuts for commuters through the borough, officials have decided to take a stand. Bryan Anselm for The New York Times

CBC | MENU

radio Top Stories Shows Podcasts Schedules Frequency Listen Live

The Current

## Overuse of GPS navigation shrinks part of the brain, says researcher

Home > News > Technology

## Navigation App Sends People Looking to Get Tested to Family Farm

Published: 23 Dec 2020, 06:01 UTC • By: [Boydian Pope](#)

While navigation apps are most of the time pretty accurate, errors do tend to happen. In some cases, they could end up becoming fatal for the drivers who follow their guidance blindly.

Verdict

News Analysis Sectors Themes Insights Events Reports Premium Insights

Disruptor Hardware Internet & Media IT Services Telecom

April 18, 2019

## Almost all young people would be lost without their sat navs, survey finds

By Ellen Daniel



Sat Nav (Pic:PA)

NEWS POLITICS FOOTBALL CELEBS TV CHOICE

## SatNav danger revealed: Navigation device blamed for causing 300,000 crashes

Road safety chiefs last night warned of the dangers of satnavs after figures blaming 300,000 smashes and near prangs.

SUBSCRIBE & SAVE Less than £3 per week

THE WEEK

Home Daily Briefing Talking Points The Week Recommends Newsletters Cartoons From the Magazine Menu The Week Junior

## 8 drivers who blindly followed their GPS into disaster

Take note: The machine does not always know where it's going

DRIVE

News Reviews Guides Car of the Year New Car Showroom

News

## Sat-nav systems cause accidents: study

According to a recent police study, GPS satellite navigation systems have caused a spike in road accidents due to drivers paying attention to the guidance rather than the road. The study says GPS devices distract drivers in a similar way to mobile phones.

www.salernonline.it

HOME CAMPANIA SALERNO SPORT PROVINCIA RUBRICHE SPETTACOLI R. STAMPA ALTRO

## Il gps fa sbagliare strada e l'auto si rompe: vacanze da incubo

1 Agosto 2023 1 Min. di lettura

## All mapped out? Using satnav 'switches off' parts of the brain, study suggests

Brain activity linked to simulating possible journeys appears to be absent when a person is following directions rather than independently planning a route

WalesOnline

NEWS RUGBY FOOTBALL IN YOUR AREA WHAT'S ON MORE

BUY A PAPER FUNERAL NOTICES JOBS VOUCHER CODES DIRECTORY ADVERTISE WITH US BOOK AN AD MARKETPLACE BUY A PHOTO NEWSLETTER SIGNUP

News > Latest Wales News > Pembrokeshire

## Driver jams car in narrow footpath after relying on sat-nav

The white Nissan Juke was stuck for a week after the two visitors to the seaside town went the wrong way

By **Wales News Service & Bramwen Jones** Reporter

Bookmark

07:41, 9 OCT 2023

Vox

EXPLAINERS CROSSWORD VIDEO PODCASTS POLITICS POLICY CULTURE SCIENCE MORE

AD NIKE SELECTS

TECHNOLOGY SCIENCE

## Have we become too reliant on GPS? This satellite expert thinks so.

By Brad Plumer | @bradplumer | brad@vox.com | Apr 10, 2016, 10:00am EDT

# Homeworks

- Given the path penalization algorithm, how does the geographic distribution of paths if we apply the logarithmic function on all edge weights?
- Create your own alternative routing algorithm combining concepts seen during the lesson.

# Material

- Shortest-Path Diversification through Network Penalization: A Washington DC Area Case Study
- One-Shot Traffic Assignment with Forward-Looking Penalization
- Comparing Alternative Route Planning Techniques: A Comparative User Study on Melbourne, Dhaka and Copenhagen Road Networks