

Principles for software composition 2020/21

07 - Temporal and modal logics, GoogleGo and pi-calculus

[Ex. 1] Two processes p_1 and p_2 want to access a single shared resource r . Consider the atomic propositions:

req_i : holds when process p_i is requesting access to r ;

use_i : holds when process p_i has had access to r ;

rel_i : holds when process p_i has released r .

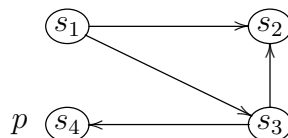
with $i \in [1, 2]$. Use LTL formulas to specify the following properties:

1. *mutual exclusion*: r is accessed by only one process at a time;
2. *release*: every time p_1 accesses r , it releases r after some time;
3. *priority*: whenever both p_1 and p_2 require r , p_1 is granted access first;
4. *no starvation*: whenever p_1 requires r , it is eventually granted access.

[Ex. 2] Three dogs live in a house with two couches and a front garden. Let $couch_{i,j}$ represent the predicate “the dog i sits on couch j ” and $garden_i$ represent the predicate “the dog i plays in the front garden”.

1. Write an LTL formula expressing the fact that whenever dog 1 plays in the garden then he keeps playing until he sits on some couch (but he may also play forever).
2. Write a CTL formula expressing the fact that dog 2 eventually plays in the garden whenever couch 1 is occupied by another dog.
3. Write a μ -calculus formula expressing the fact that no more than one couch is occupied at any time by dog 3.

[Ex. 3] Given the μ -calculus formula $\Phi = \mu x.((p \wedge \Box x) \vee (\neg p \wedge \Diamond x))$ write its denotational semantics $\llbracket \Phi \rrbracket \rho$ and evaluate it on the LTS below (where $V = \{s_1, s_2, s_3, s_4\}$ and $P = \{p\}$).



[Ex. 4] Write a Go function that takes one channel `ini` for receiving integers and one channel `ins` for receiving strings and returns a channel `outp` where all the messages received on `ini` and `ins` will be paired.

Hint: define a `struct` to form pairs

[Ex. 5] Write a Go function that takes two channels `f` and `q` and tries to send the stream of Fibonacci numbers on `f` but quits when it receives `true` on channel `q`. Write a `main` program to test the function by printing the first 10 Fibonacci numbers.

[Ex. 6] The *asynchronous* π -calculus requires that outputs have no continuation:

$$p ::= \mathbf{nil} \mid \bar{x}(y) \mid x(y).p \mid \tau.p \mid [x = y]p \mid p + p \mid p|p \mid (x)p \mid !p$$

Show that any process in the original π -calculus can be represented in the asynchronous π -calculus using an extra (fresh) channel to simulate explicit acknowledgement of name transmission.

[Ex. 7] The *polyadic* π -calculus allows communicating more than one name in a single action, i.e., its action prefixes are of the form:

$$\pi ::= \tau \mid \bar{x}(z_1, \dots, z_n) \mid x(z_1, \dots, z_n)$$

The polyadic extension is useful especially when studying types for name passing processes. Show that the polyadic π -calculus can be encoded in the ordinary (monadic) π -calculus by passing the name of a private channel through which the multiple arguments are then passed in a sequence.