

PSC 2022/23 (375AA, 9CFU)

Principles for Software Composition

Roberto Bruni

<http://www.di.unipi.it/~bruni/>

<http://didawiki.di.unipi.it/doku.php/magistraleinformatica/psc/start>

01 - Introduction

English vs Italian



Classes

Every

Monday: 11:00-13:00, L1

Tuesday: 16:00-18:00, L1

Thursday: 14:00-16:00, L1

Classes, typically

no break (unless requested)

Monday: 11:00-12:30, L1

Tuesday: 16:15-17:45, L1

Thursday: 14:15-15:45, L1

Course material

The image shows two overlapping screenshots. The top one is a DidaWiki page for the course 'Principles for Software Composition'. The page header includes the DidaWiki logo, a search bar, and navigation links for 'Ultime modifiche', 'Gestore Media', and 'Indice'. The breadcrumb trail reads 'Ti trovi qui: DidaWiki » Corso di Laurea Magistrale in Informatica » Principles for Software Composition'. The main content area features the course title, a diagram with two yellow boxes labeled 'C[.]' and green boxes labeled 'p' and 'q' connected by a double-headed arrow, and text providing course details: 'PSC 2022/23 (375AA, 9 CFU)', 'Lecturer: Roberto Bruni', contact information for web, email, and Microsoft Teams, and office hours: 'Tuesday 14:00-16:00 or by appointment'. A right-hand sidebar titled 'Indice' lists course components: 'Principles for Software Composition', 'Objectives', 'Prerequisites', 'Textbook(s)', 'Exam', 'Oral Exams: schedule', 'Announcements', and 'Lectures (1st part)'. The bottom screenshot is a Microsoft Teams meeting interface for the same course. The meeting title is '375AA 22/23 - PRINCIPLES ...'. The main content area displays a welcome message: 'Benvenuto in 375AA 22/23 - PRINCIPLES FOR SOFTWARE COMPOSITION [WIF-LM]' and 'Scegli da dove vuoi iniziare'. Below this are three icons: a Teams icon, a book icon with scissors and a pencil, and a document icon with a pencil. Two buttons are positioned below the icons: 'Carica il materiale del corso' and 'Configura blocco appunti per la classe'. A left-hand sidebar shows navigation options: 'Tutti i team', '375AA 22/23 - PRINCIPLES ...', 'Pagina iniziale', 'Blocco appunti per la classe', 'Attività', 'Voti', 'Reflect', 'Insights', 'Canali', 'Generale', and 'Exams'.

Who am I?



<http://www.di.unipi.it/~bruni>



bruni@di.unipi.it



Office hours: by appointment
preferably



Tuesday 14:00-16:00

Research topics (theses?)

False alarm detection in Abstract Interpretation

Formal approaches to code obfuscation

Quantum Computation and concurrency models

Modelling and analysis of biological systems

Graphical specification languages

Algebraic approaches to structured graphs

Rewrite rules for reversible languages



Who are you?



Forms

First Name:

Last Name:

Enrollment number:

email:

Bachelor degree:

MSc course of enrollment:

Please fill the form!

Who are you?



Forms

First Name:

Last Name:

Enrollment number:

email:

Bachelor degree:

MSc course of enrollment:

Please fill the form!

The Course

Some quotes

Computer science is no more about computers than astronomy is about telescopes

- Edsger W. Dijkstra

Studying programming languages without formal semantics would be like studying physics without math

- from the web

All models are wrong, but some are useful

- George Box

Subjects are divided in two categories:

- 1) too difficult matters, that CANNOT be studied*
- 2) easy matters, that DO NOT NEED to be studied*

- back of a t-shirt

Objectives

Programming paradigms
(imperative, declarative,
higher order, concurrent,
mobile, stochastic)



Mathematical frameworks
(concrete & abstract)
(domains, inference rules, transition
systems, λ -calculus, process algebras)



Understand
(recursion, semantics,
compositionality)



Reason
(induction, modal and
temporal logics,
behavioural and
logical equivalences)

Explain
(correctness,
compliance,
performance)



The approach

(in their simplest form,
still Turing equivalent)

programming
paradigms

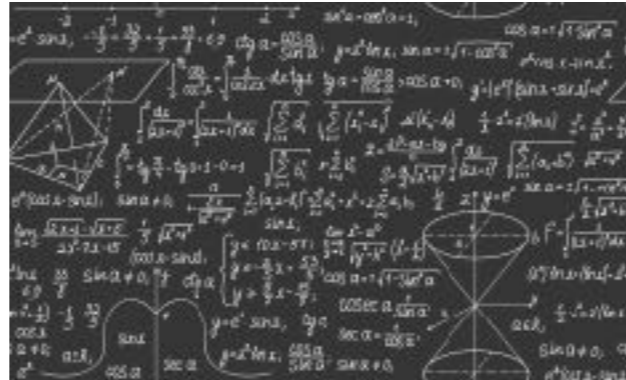


mathematical
frameworks



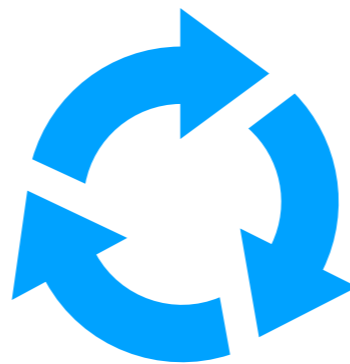
meta-properties
+
proof techniques

(for all programs
or just
some classes of programs)

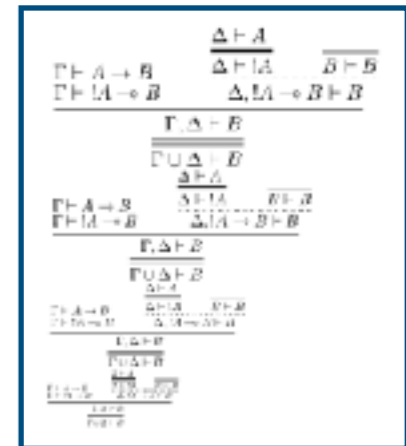


models

programs



specifications

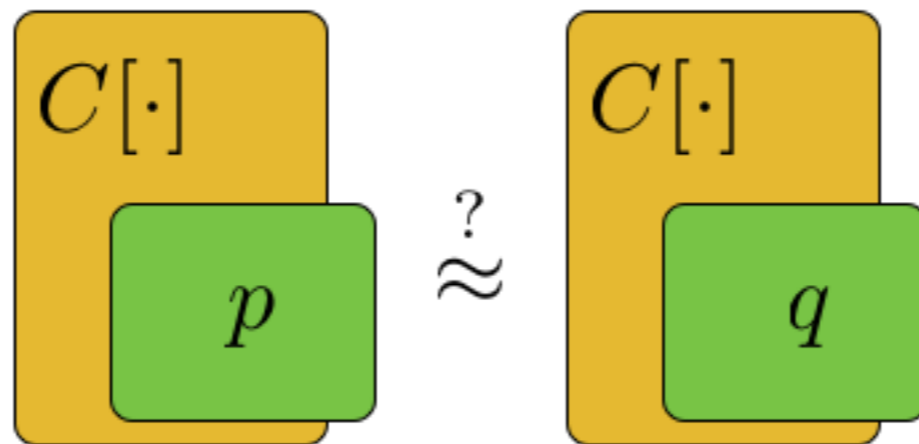


Key question

Given two programs p and q :

Do they behave the same?

Is it safe to replace one with the other in any context?



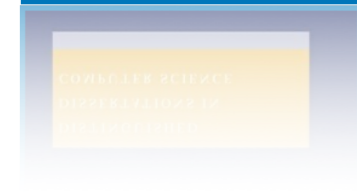
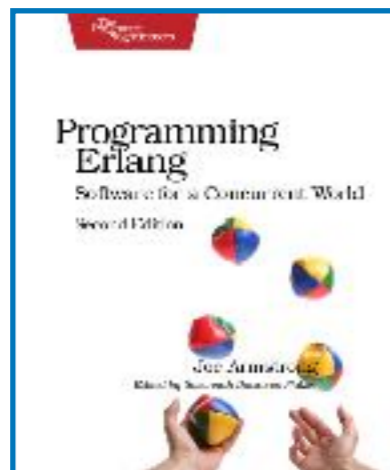
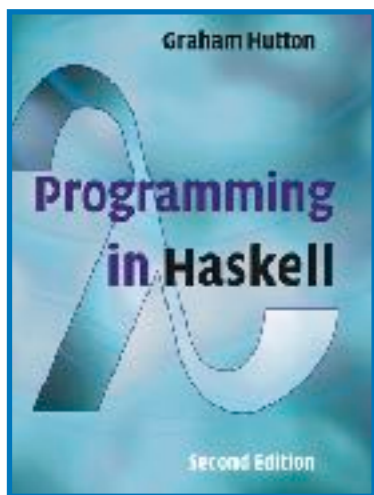
Textbooks



Roberto Bruni and Ugo Montanari
Models of Computation

Texts in Theoretical Computer Science (an EATCS series)

<https://www.springer.com/book/9783319428987>

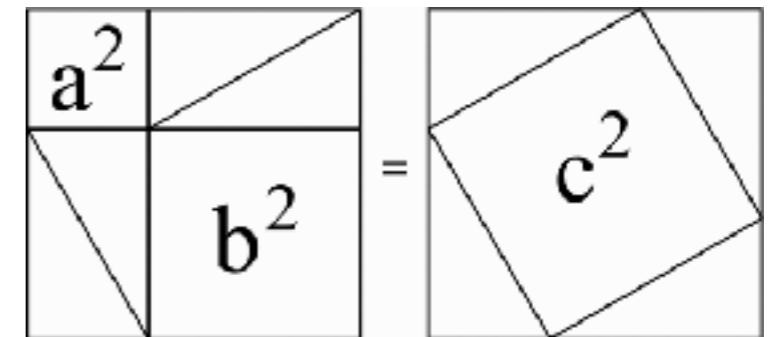


Course activities



attend virtual
classrooms:
ask questions!
(sleep quietly)

learn theorems:
(drink many coffees)



do some thinking:
solve ALL your
homework
(at least try to)

give the exam:
time for a party!



Be proactive!

Let's spell out definitions together

```
% find the least (non-unitary) divisor  $p$  of  $n > 0$ 

$p := 0$ ;


```

```
 $x := 2$ ;
```

```
while (.....) do {
    if (  $n \% x == 0$  ) then {
         $p := x$ ;
    } else {
         $x := x + 1$ ;
    }
}
```

Be proactive!

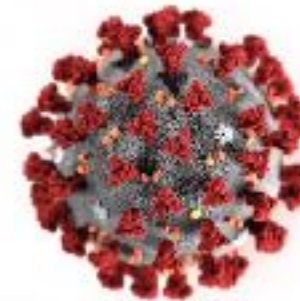
Correct me if I'm wrong

```
% find the index of the last occurrence of n in a
i := length(a)-1;
while ( i>0 && n!=a[i] ) do {
    i := i-1;
}
```

Exam

In past years, the evaluation was based on written and oral exams.

Since the covid-19 emergency, and for the current period, the evaluation will be solely based on a final oral exam.



Registration to exams is mandatory:

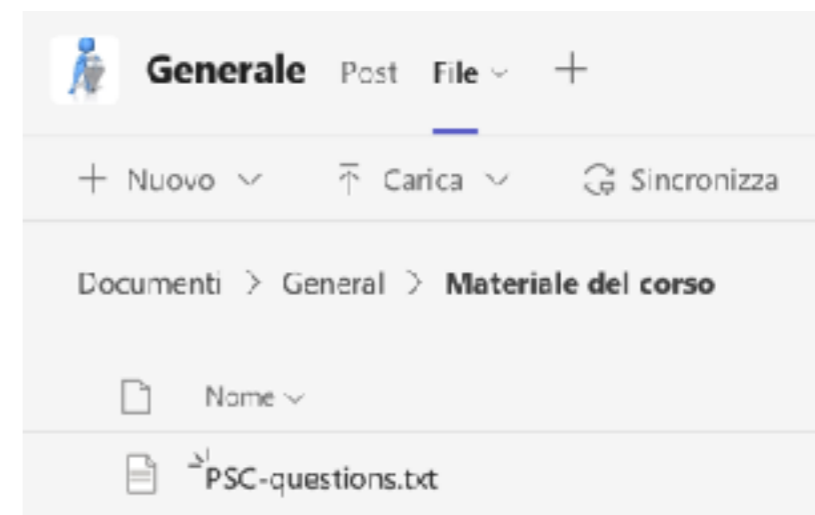
<https://esami.unipi.it/esami>

The exam will typically consist of:

1. three to four preliminary questions
2. one exercise (analogous to past written exams)
3. redoing one of the proofs seen in the course
4. some additional questions

The list of preliminary questions is available on Microsoft Teams, in the File tab

([PSC-questions.txt](#))



A sample exam

What is a complete partial order?

What are the rules of the type system of HOFL?

How is iteration achieved in CCS?

Why only positive normal forms are considered in the mu-calculus?

Consider the HOFL term

$$t \stackrel{\text{def}}{=} \mathbf{rec} \ f. \ \lambda x. \ \mathbf{if} \ x \ \mathbf{then} \ (x, \mathbf{fst}(f \ x)) \ \mathbf{else} \ (\mathbf{snd}(f \ x), x)$$

1. Find the principal type of t .
2. Find the denotational semantics of t .

Prove the Switch Lemma

Given the initial state distribution and a DTMC,
how do we compute the state distribution at time 3?

Badges

No mid-terms

No self-evaluation tests

During the course: some “badge” exercises

Submit your solutions by email to earn
bronze / silver / gold badges
(no extra scores, but be proud of yourselves)



Prerequisites

Basic set theory

 \emptyset $A \cap B$ $A \cup B$ $A \setminus B$ \overline{A} $a \in A$ $A \subset B$ $A \subseteq B$ $A \times B$ $a \notin A$ $A \not\subset B$ $A \cap B = \emptyset$ \mathbb{N} \mathbb{Z} \mathbb{Q} \mathbb{R} \mathbb{B} $\mathbb{N} \subseteq \mathbb{N}$ $\mathbb{N} \in \wp(\mathbb{N})$ $S \subseteq \wp(\mathbb{N})$

Prerequisites

Basic set theory: functions, relations

$$f : A \rightarrow B$$

$$R \subseteq A \times B$$

functions as relations

$$R_f \triangleq \{(a, f(a)) \mid a \in A\}$$

sets as functions
(characteristic function)

$$f_N : \mathbb{N} \rightarrow \mathbb{B}$$

$$f_N(n) \triangleq \begin{cases} 1 & n \in N \\ 0 & \text{otherwise} \end{cases}$$

$$N = \{n \mid f_N(n) = 1\}$$

Prerequisites

First order logic

ff	false	tt	true				
0	F	1	T	$P \wedge Q$	$P \vee Q$	$\neg P$	
				$\exists x. P(x)$	$\forall x. P(x)$	$P \Rightarrow Q$	$P \Leftrightarrow Q$

meaning of implication!

$$P \Rightarrow Q$$

$$Q \vee \neg P$$

$$\neg Q \Rightarrow \neg P$$

order of quantifiers matters!

$$\forall n \in \mathbb{N}. \exists m \in \mathbb{N}. n < m$$

$$\exists m \in \mathbb{N}. \forall n \in \mathbb{N}. n < m$$

Prerequisites

Strings and context-free grammars

$$\text{Alphabet } A \quad A^n \triangleq \underbrace{A \times \cdots \times A}_n \quad A^* \triangleq \bigcup_{n \in \mathbb{N}} A^n$$

$$\mathbb{B} = \{0, 1\}$$

$$\mathbb{B}^0 = \{\epsilon\}$$

$$\mathbb{B}^1 = \{0, 1\}$$

$$\mathbb{B}^2 = \{00, 01, 10, 11\}$$

$$\mathbb{B}^3 = \{000, 001, 010, 011, 100, 101, 110, 111\}$$

...

$$\mathbb{B}^* = \{\epsilon, 0, 1, 00, 01, 10, 11, 000, \dots\}$$

Prerequisites

Strings and context-free grammars

Alphabet A $A^n \triangleq \underbrace{A \times \cdots \times A}_n$ $A^* \triangleq \bigcup_{n \in \mathbb{N}} A^n$

$$\mathbb{B}^* = \{\epsilon, 0, 1, 00, 01, 10, 11, 000, \dots\}$$

$$A ::= \epsilon \mid 0A \mid 1B$$

$$B ::= 0B \mid 1A$$

$$\underbrace{A}_{\rightarrow} \underbrace{0A}_{\rightarrow} \underbrace{01B}_{\rightarrow} \underbrace{011A}_{\rightarrow} \underbrace{011\epsilon}_{=} = 011$$

$$\mathcal{L}(A) = ?$$

$$\mathcal{L}(B) = ?$$

Prerequisites

Inductive and recursive definitions

$$\begin{aligned} 0! &\triangleq 1 \\ (n+1)! &\triangleq n! \cdot (n+1) \end{aligned}$$

$$\begin{aligned} A^0 &\triangleq \{\epsilon\} \\ A^{(n+1)} &\triangleq A \times A^n \end{aligned}$$

$$f(n) \triangleq \begin{cases} 1 & \text{if } n \leq 1 \\ f(n/2) & \text{if } n > 1 \wedge n \% 2 = 0 \\ f(3n+1) & \text{otherwise} \end{cases}$$

$$f(12) = f(6) = f(3) = f(10) = f(5) = f(16) = f(8) = f(4) = f(2) = f(1) = 1$$

Prerequisites

Conjectures vs theorems

a natural number p is **prime**

if it cannot be written as the product of two smaller numbers

n	Is n prime?	$2^n - 1$	Is $2^n - 1$ prime?
2	yes	3	yes
3	yes	7	yes
4	no: $4 = 2 \cdot 2$	15	no: $15 = 3 \cdot 5$
5	yes	31	yes
6	no: $6 = 2 \cdot 3$	63	no: $63 = 7 \cdot 9$
7	yes	127	yes
8	no: $8 = 2 \cdot 4$	255	no: $255 = 15 \cdot 17$
9	no: $9 = 3 \cdot 3$	511	no: $511 = 7 \cdot 73$
10	no: $10 = 2 \cdot 5$	1023	no: $1023 = 31 \cdot 33$

Prerequisites

Conjectures vs theorems

if p is prime
then $2^p - 1$ is prime

if $n > 1$ is not prime
then $2^n - 1$ is not prime



Use any mean to prove or disprove the above conjectures

Your background?

Please fill the form about “Familiar subjects”

← Tutti i team

PF **Generale** Post File Familiar subjects (P... 1 altra +

Avvia riunione

375AA 22/23 - PRINCIPLES ...

Pagina iniziale
Blocco appunti per la classe
Attività
Voti
Reflect
Insights

Canali

Generale
Exams

Familiar subjects (PSC 2022/23)

Ciao, Roberto. Quando invii questo modulo, il proprietario vedrà il tuo nome e indirizzo email.

* Obbligatoria

1. Structural recursion * [🗑]

★ ★ ★ ★ ☆

2. Type systems * [🗑]

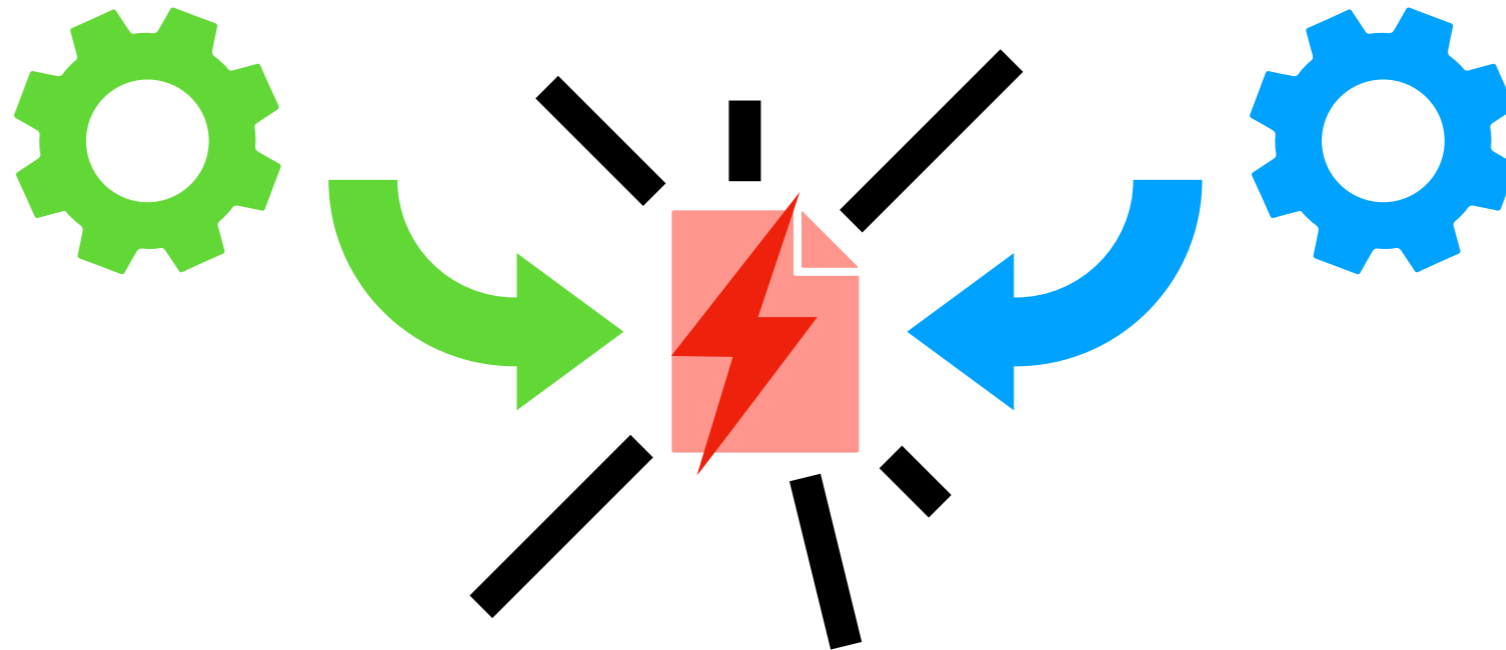
☆ ☆ ☆ ☆ ☆

3. Proof systems (axioms and inference rules) * [🗑]

☆ ☆ ☆ ☆ ☆

An Appetiser

The problem



Two concurrent processes share a single-use resource

They can communicate using shared memory

We want to guarantee that there are no conflicts
when the processes access the resource

No strict alternation of naive turn taking is imposed

Peterson's mutual exclusion algorithm (1981)

```
% Two processes P1, P2
% Two boolean variables b1, b2 (both initially false)
% when Pi wants to enter the critical section, then it sets bi to true
% An integer variable k, taking values in {1,2}
% (initial value is arbitrary)
% the process Pk has priority over the other process
%
% Process P1 in pseudocode
while (true) {
    ...                % non critical section
    b1 := true ;      % P1 wants to enter the critical section
    k := 2 ;          % P1 gives priority to the other process
    while (b2 && k==2) skip ; % P1 waits its turn
    ...                % P1 enters the critical section
    b1 := false       % P1 leaves the critical section
}

% Process P2 is analogous to P1
```

Which question?

Does Peterson's algorithm work?

What does it mean that "it works"? What do we expect?

(Progress)

If the resource is available, no process is forced to wait

(Bounded Waiting)

No process will wait forever for the resource
(otherwise the easiest solution is no one gets in)

(Mutual Exclusion)

P1 and P2 are never in the critical section at the same time

Hyman's mutual exclusion algorithm (1966)

```
% Two processes H1, H2
% Two boolean variables b1, b2 (both initially false)
% when Hi wants to enter the critical section, then it sets bi to true
% An integer variable k, taking values in {1,2}
% (initial value is arbitrary)
% the process Hk has priority over the other process
%
% Process H1 in pseudocode
while (true) {
    ... % non critical section
    b1 := true ; % H1 wants to enter the critical section
    while (k==2) { % while H2 has priority
        while (b2) skip ; % H1 waits
        k := 1; % H1 sets priority to itself
    }
    ... % H1 enters the critical section
    b1 := false % H1 leaves the critical section
}

% Process H2 is analogous to H1
```

The question

Does Peterson's algorithm satisfy mutual exclusion?

Does Hyman's algorithm satisfy mutual exclusion?

For the answers be patient and wait early-May lectures