Methods for the specification and verification of business processes
MPB (6 cfu, 295AA)

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12 - Workflow nets
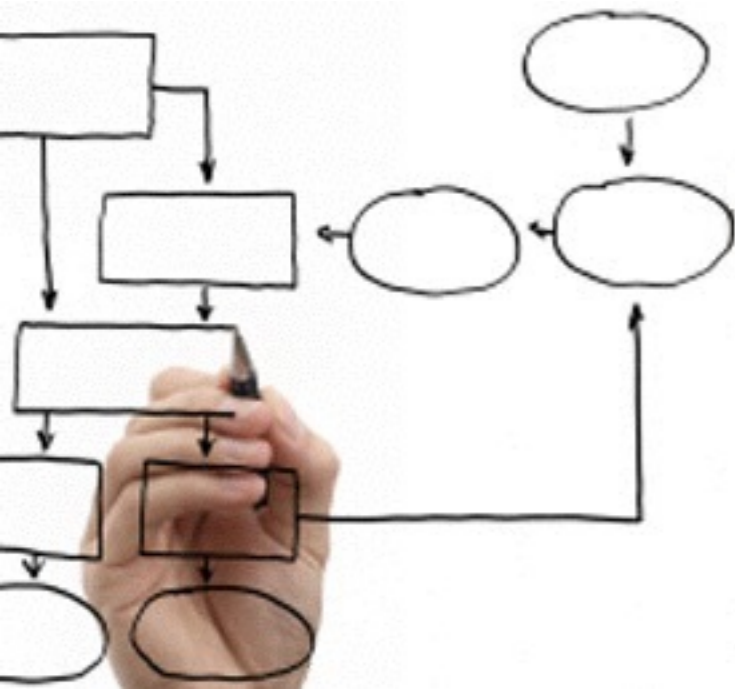
Object

We study some special kind of Petri nets,
that are suitable models of workflows

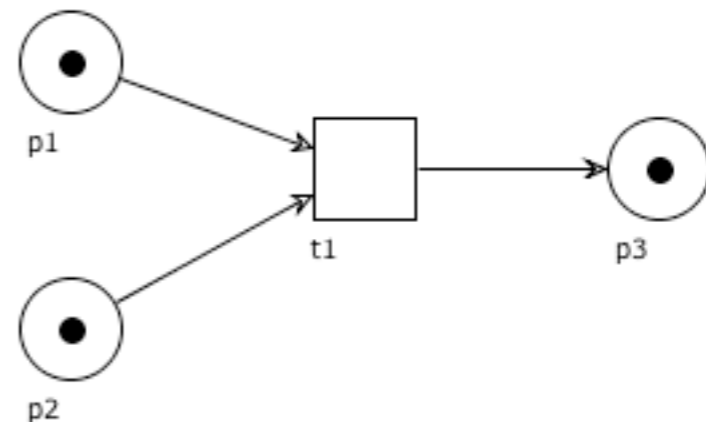# There are many, many variants of Petri nets

Condition / Event Systems

A **C/E system** is a Petri net whose places have all capacity equal to 1
(i.e., each place can contain one token at most)

Markings are just subsets of P (not multisets)

Firing rule is more restrictive:
t is enabled at M if $\bullet t \subseteq M$ **and t$\bullet \cap$ M =** $\varnothing$
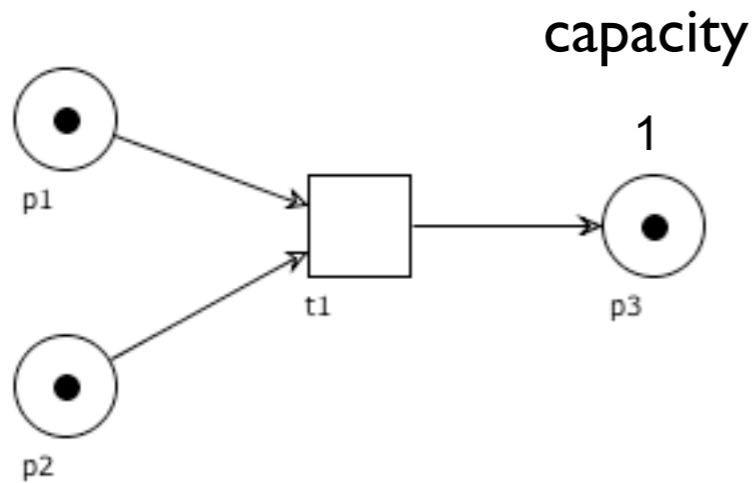
Is t_1 enabled?

Place / Transition Petri nets

A **P/T net** is a Petri net (P,T,F) together with a weight function $w : F \rightarrow Nat$

Firings consume and produce tokens according to the weight function
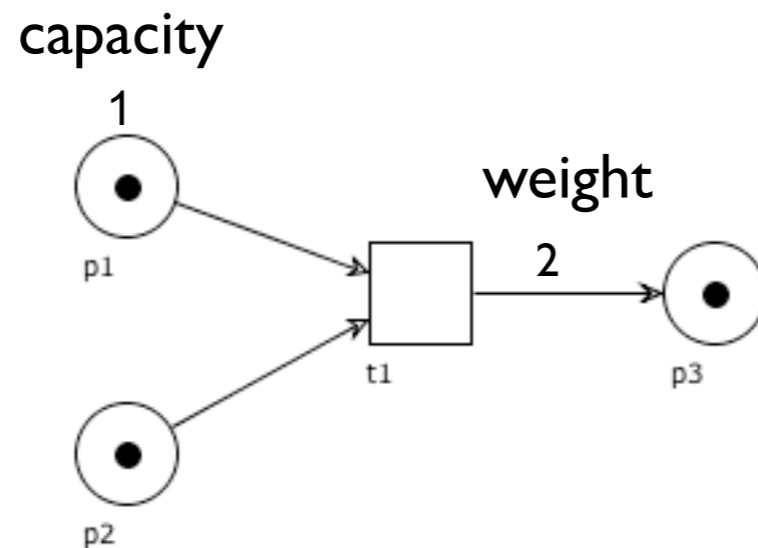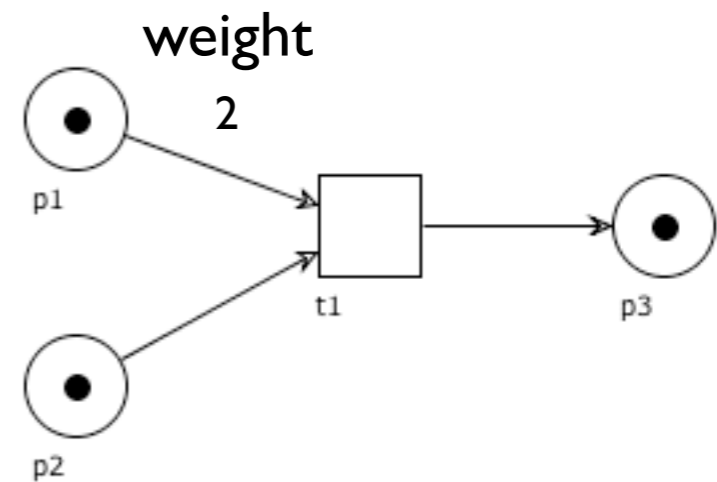
Sometimes a place capacity function $c : P \rightarrow Nat \cup \{\infty\}$ is also considered

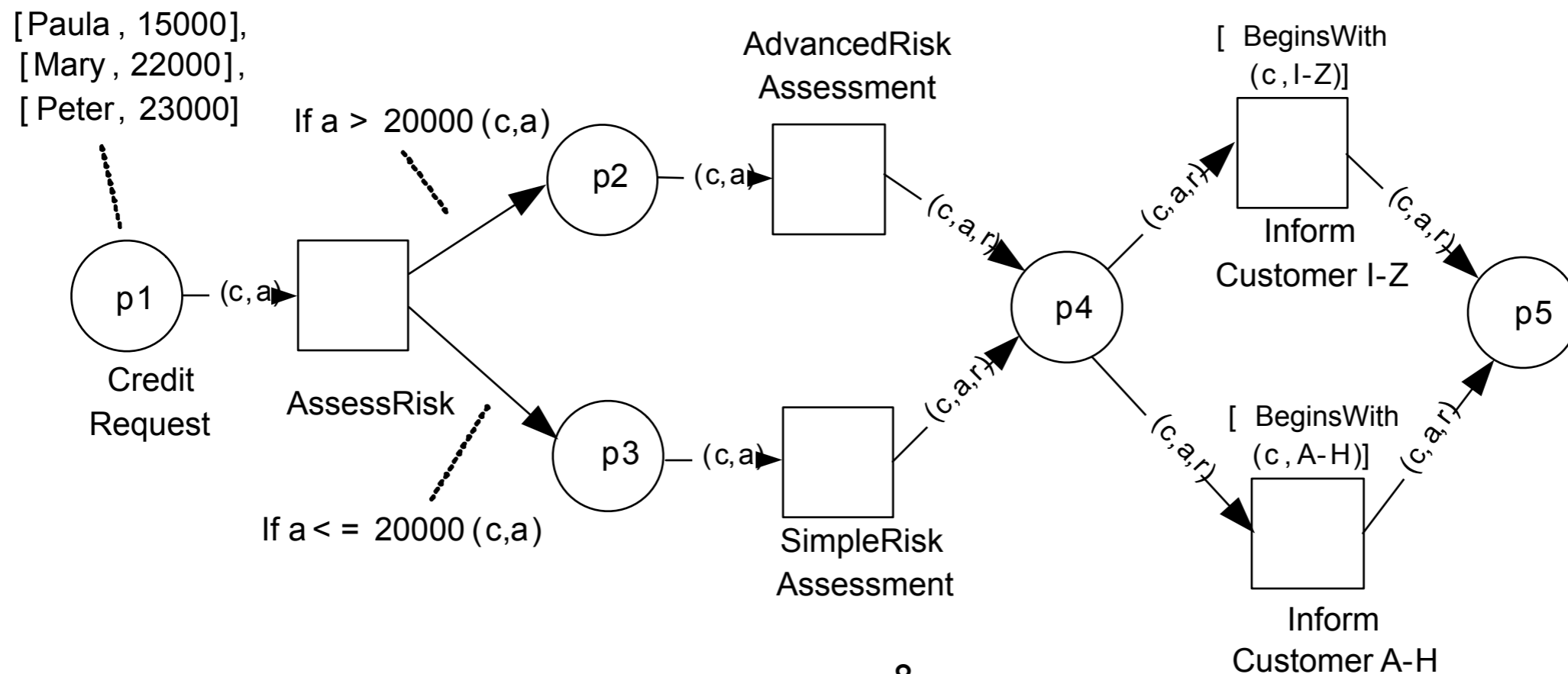Firings cannot lead to markings where the capacity of a place is exceeded

P/T net: examples

capacity

1

p1

p2

t1

p3

Is t₁ enabled?

weight

2

p1

p2

t1

p3

capacity

1

weight

2

p1

p2

t1

p3

Coloured nets
(also called High-Level)

A **coloured net** is a Petri net whose
tokens can carry data and
whose transitions can check data
(see exact definition in Weske's book)

Workflow nets

Workflow nets features

Aim: To ease the representation of business processes
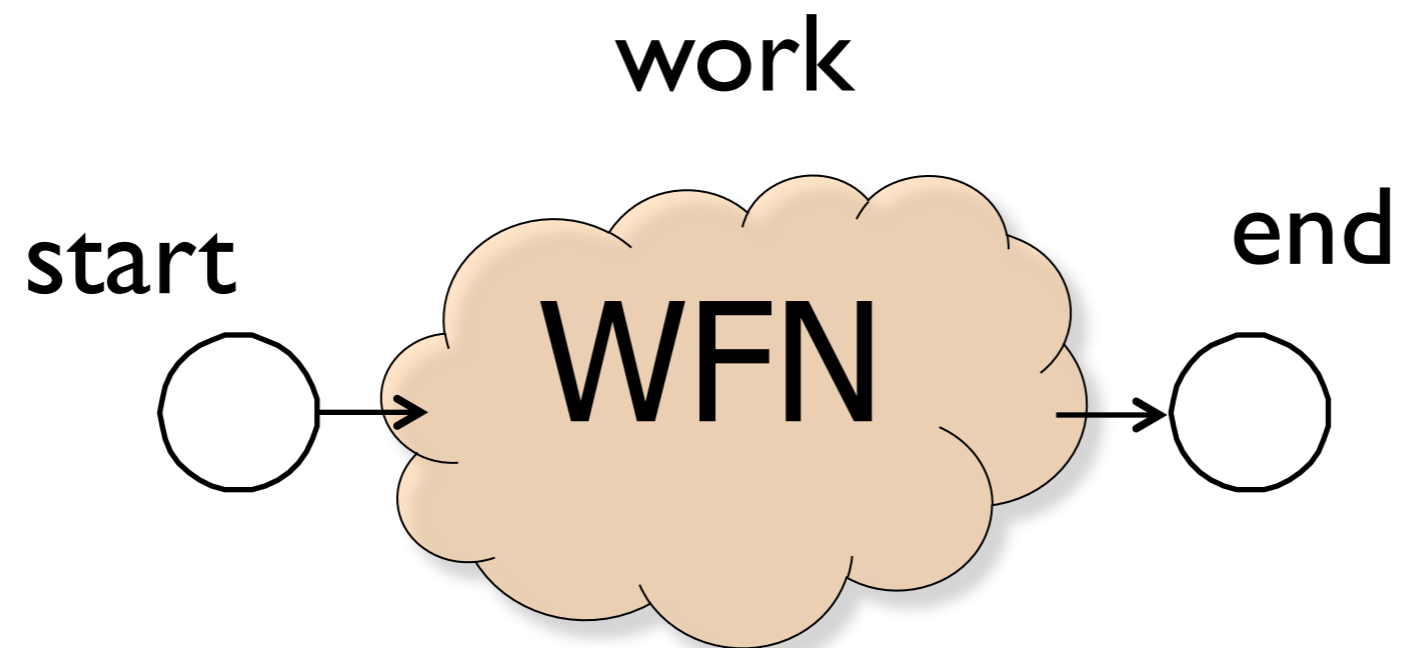
Formal (unambiguous) semantics

Decorated graphical representation

Structural restrictions

Efficient analysis of process properties

Tool independence (.pnml standard)

Workflow net: idea

Workflow net

Definition:
A Petri net (P, T, F) is called **workflow net** if:

1. there is a distinguished *initial place* $i \in P$ with $\bullet i = \emptyset$

2. there is a distinguished *final place* $o \in P$ with $o \bullet = \emptyset$

3. every other place and transition belongs to a path from i to o

Workflow net: Rationale

1. a token in i represents a process instance not yet started

2. a token in o represents a finished case

3. each place and each transition can participate in a case

Definition:
A Petri net (P, T, F) is called **workflow net** if:

1. there is a distinguished *initial place* $i \in P$ with $\bullet i = \emptyset$

2. there is a distinguished *final place* $o \in P$ with $o \bullet = \emptyset$

3. every other place and transition belongs to a path from i to o

WF net: Example
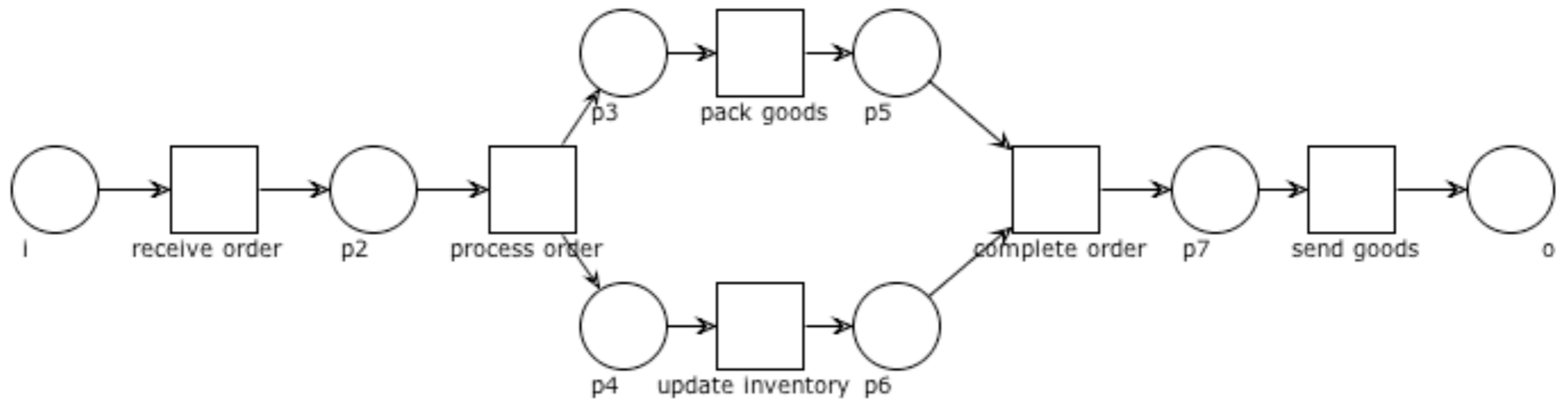
Basic properties

Lemma: In a workflow net there is a **unique** node
with no incoming arc

Lemma: In a workflow net there is a **unique** node
with no outgoing arc

Exercise: Guess which nodes are those

Exercise: Prove the above lemmas
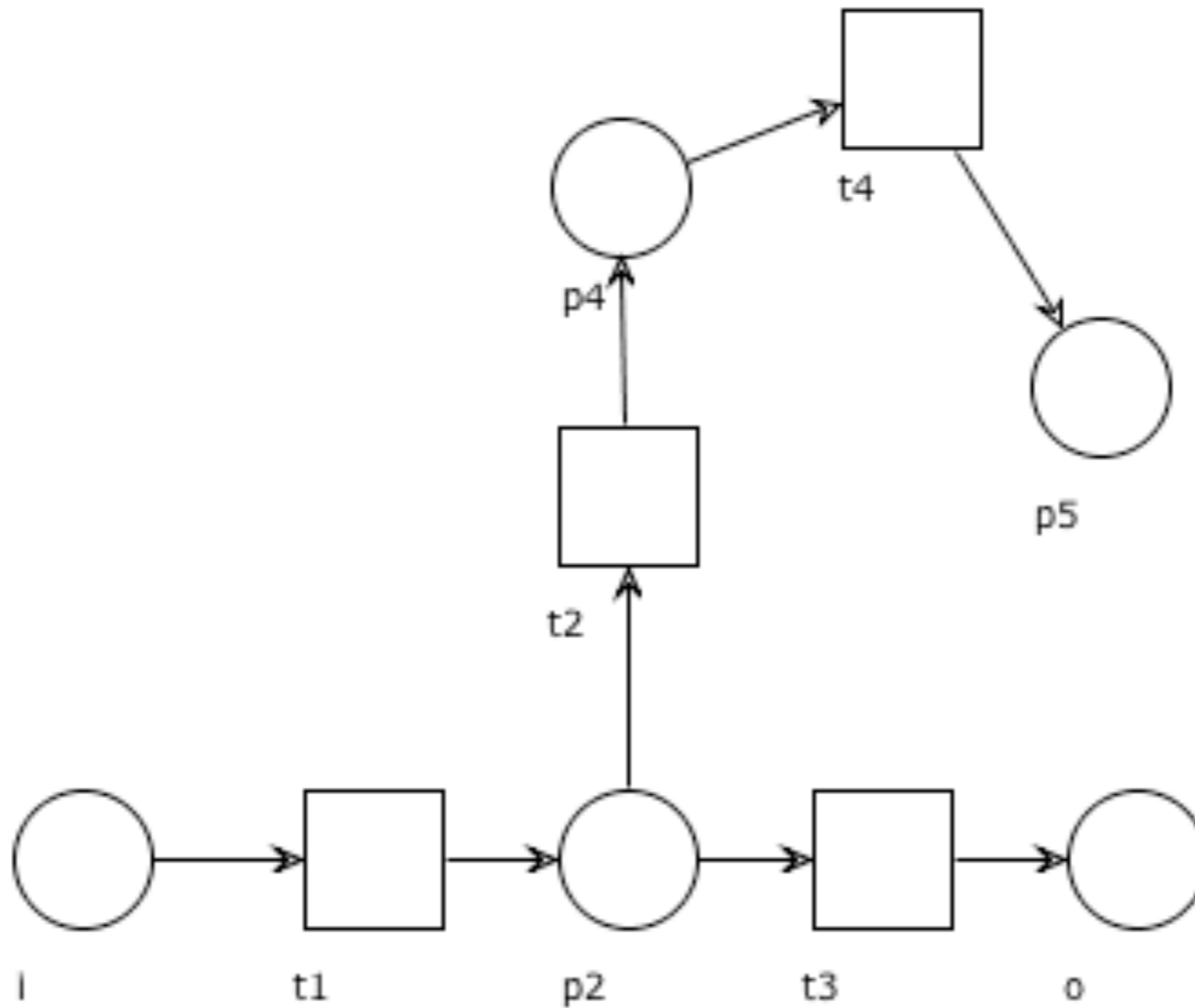(hint: suppose the nodes are not unique reach a contradiction)
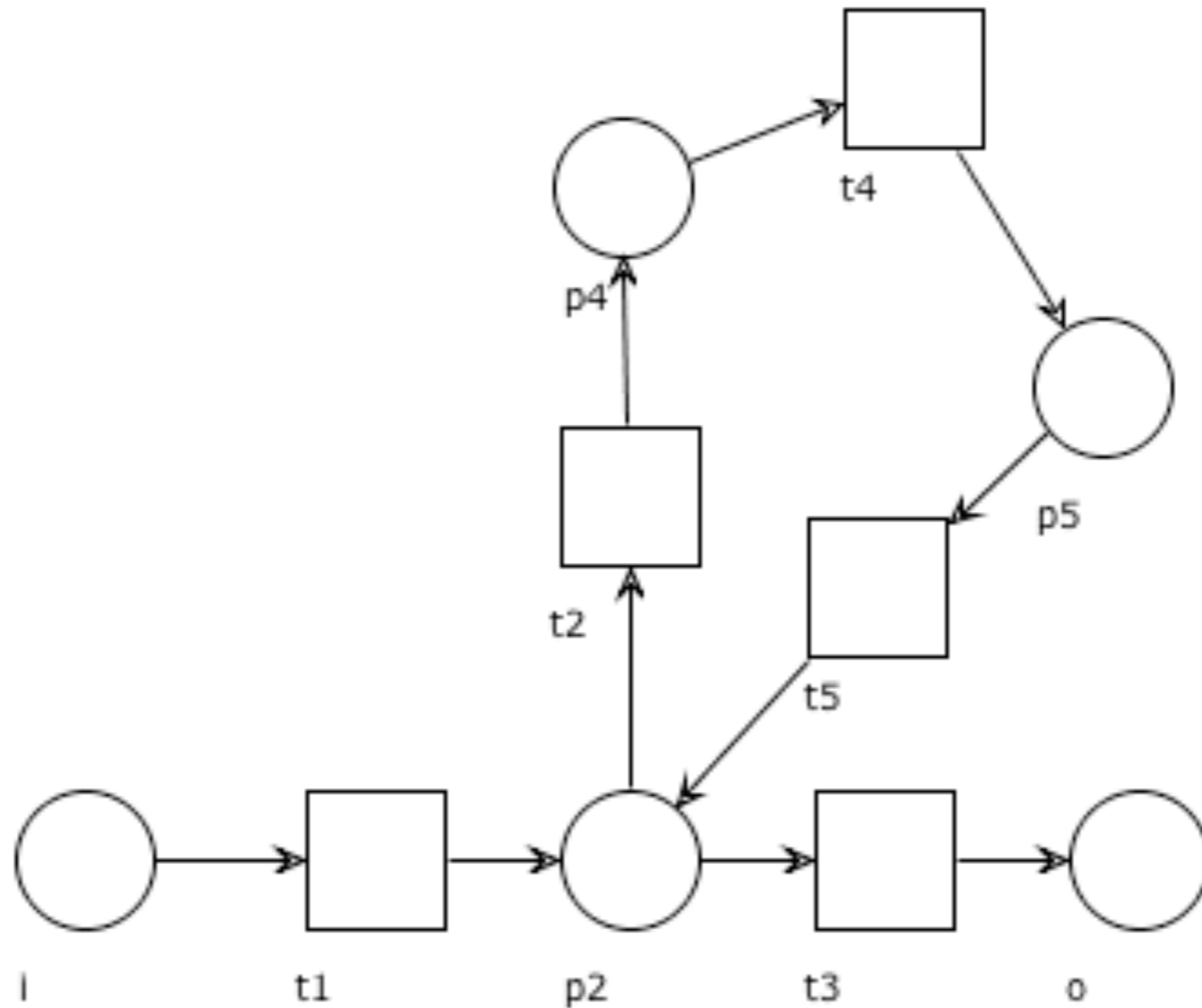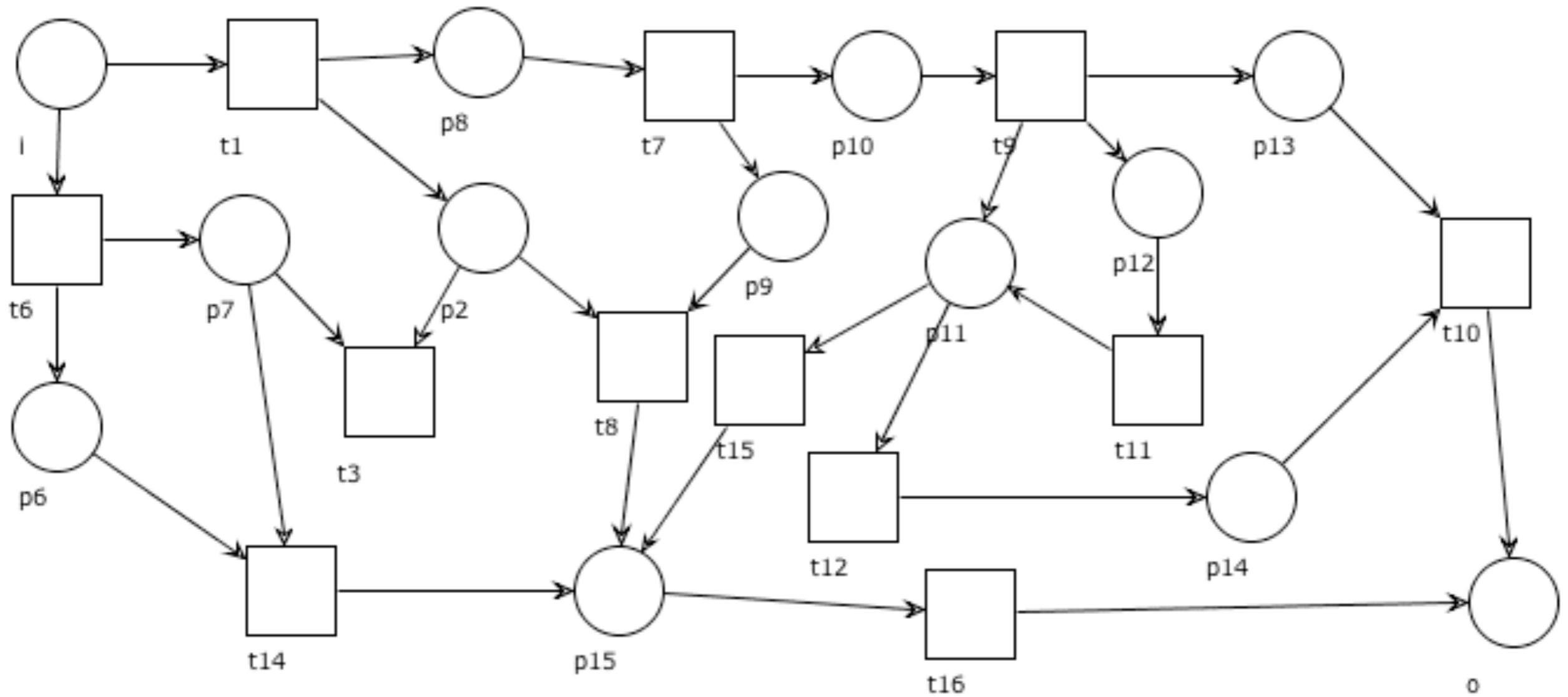
Question time: WF net?
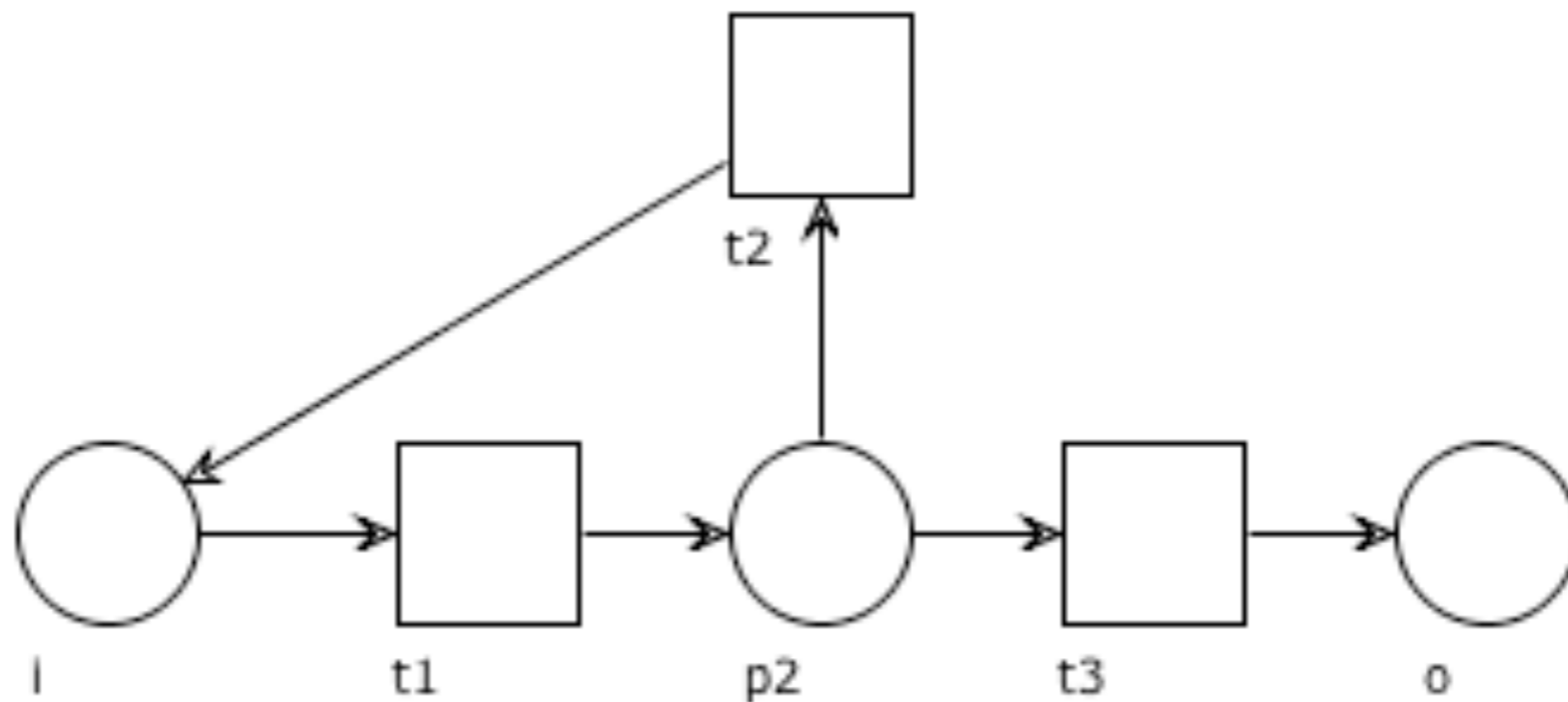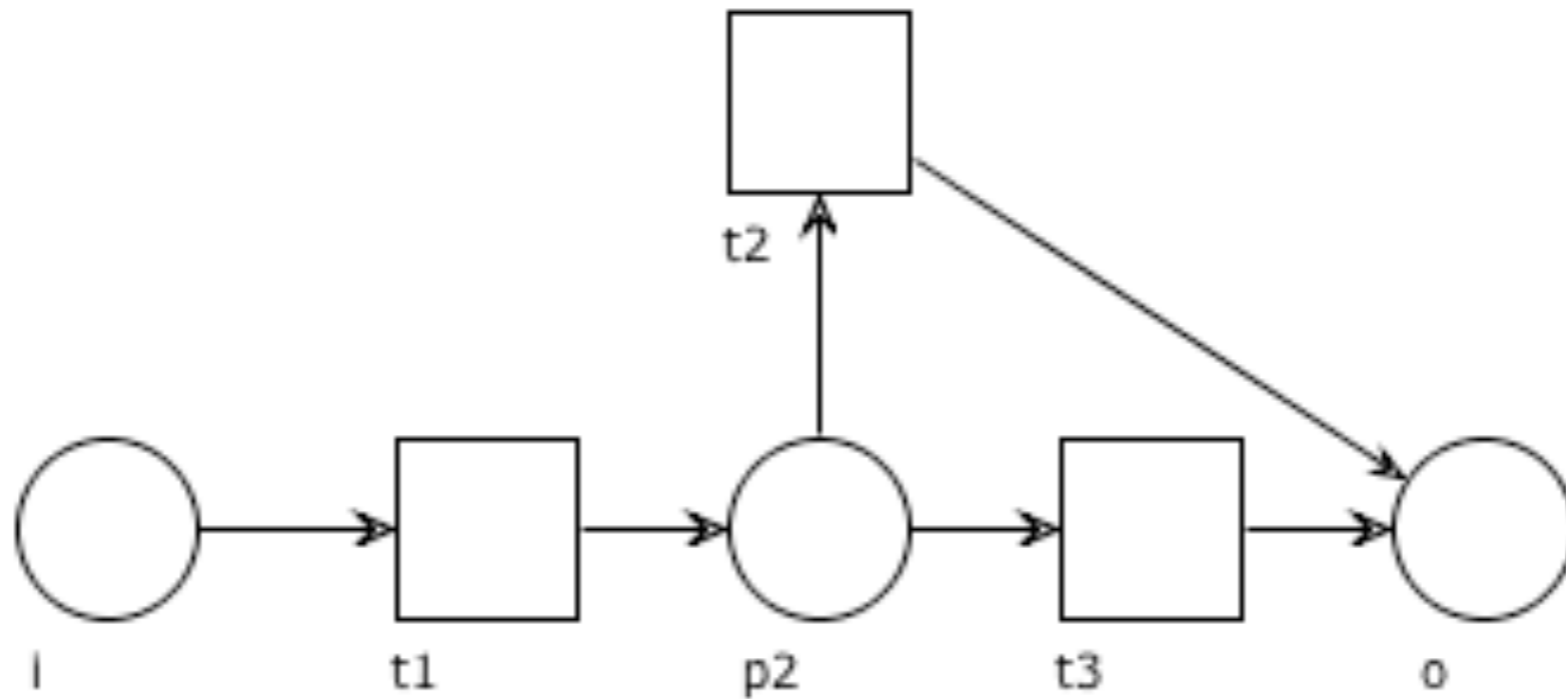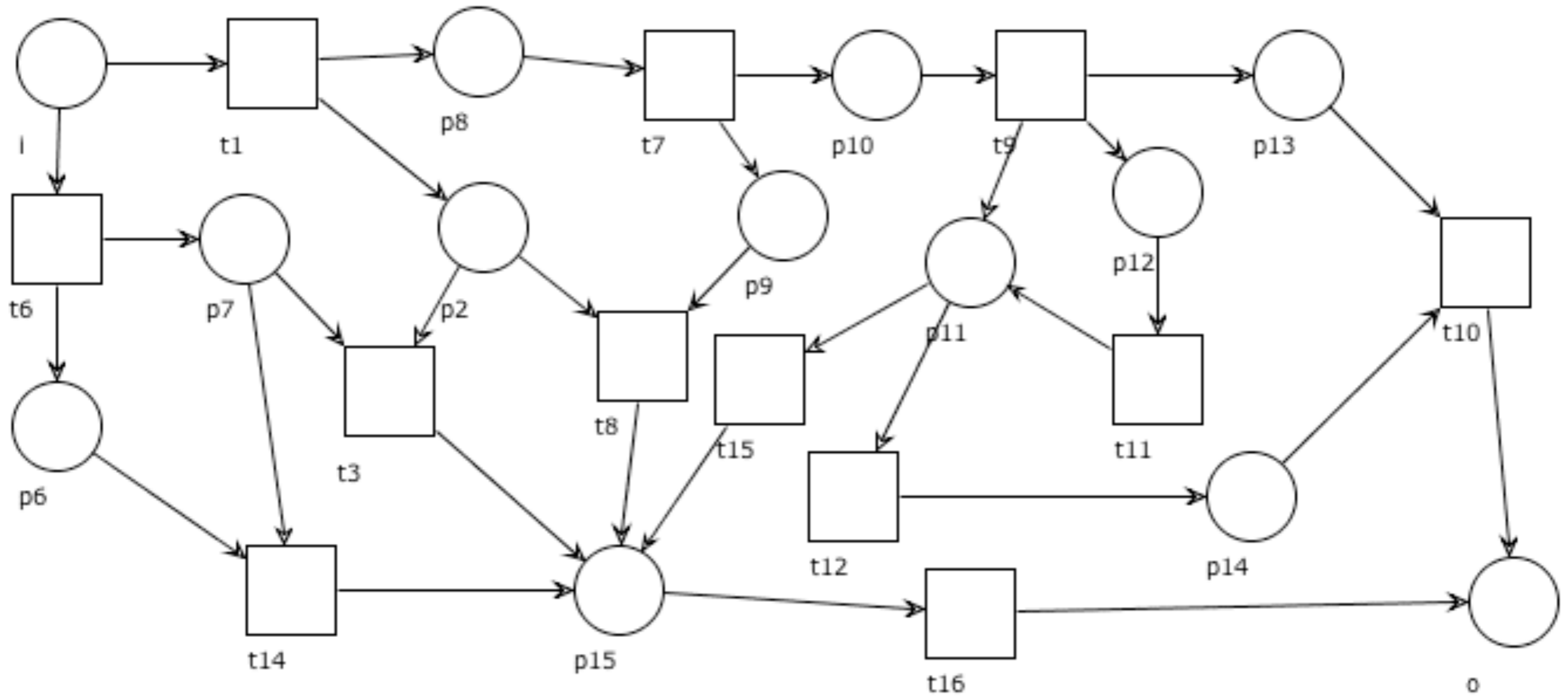
Question time: WF net?

Question time: WF net?
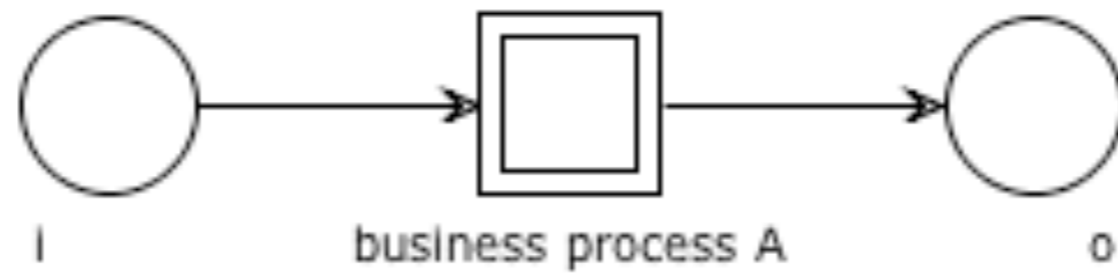
Question time: WF net?

Question time: WF net?

Question time: WF net?

Process activity

Process instance, case

Place can hold tokens that represent cases

Transition realised by another workflow net

Abstract view

i   business process A   o

A

29
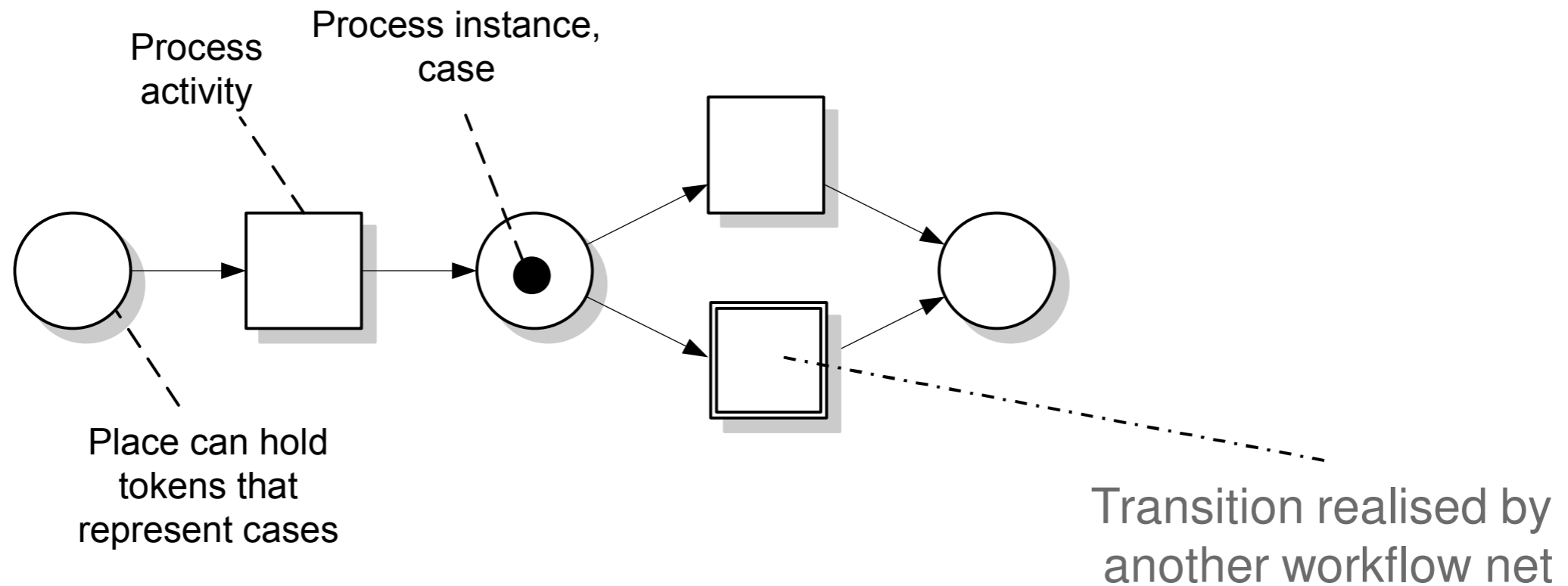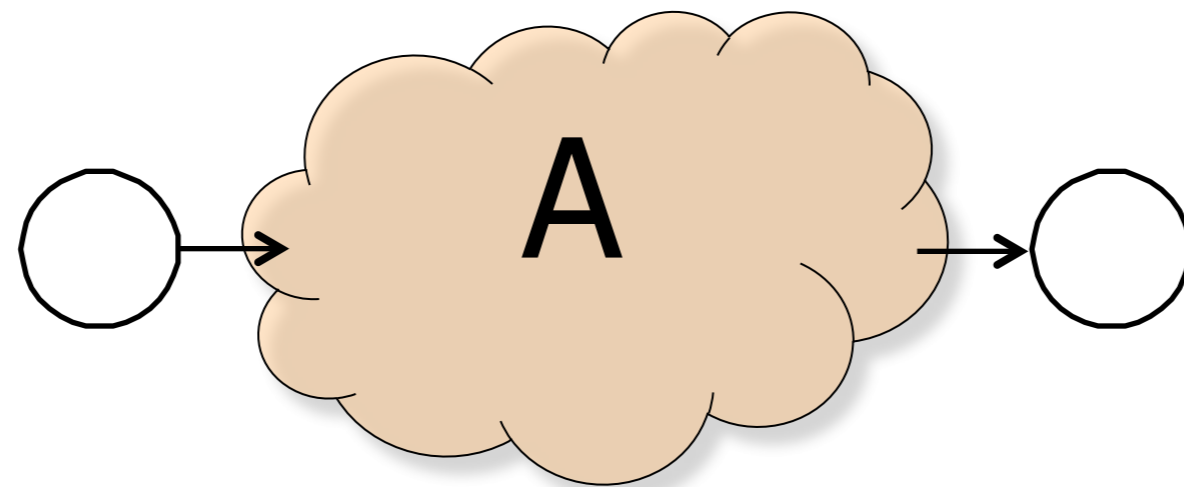
Typical control flow aspects

Sequencing

Parallelism (AND-split + AND-join)

Selection (XOR-split + XOR-join)

Iteration (XOR-join + XOR-split)

Capacity constraints:
Feedback loop
Mutual exclusion
Alternating
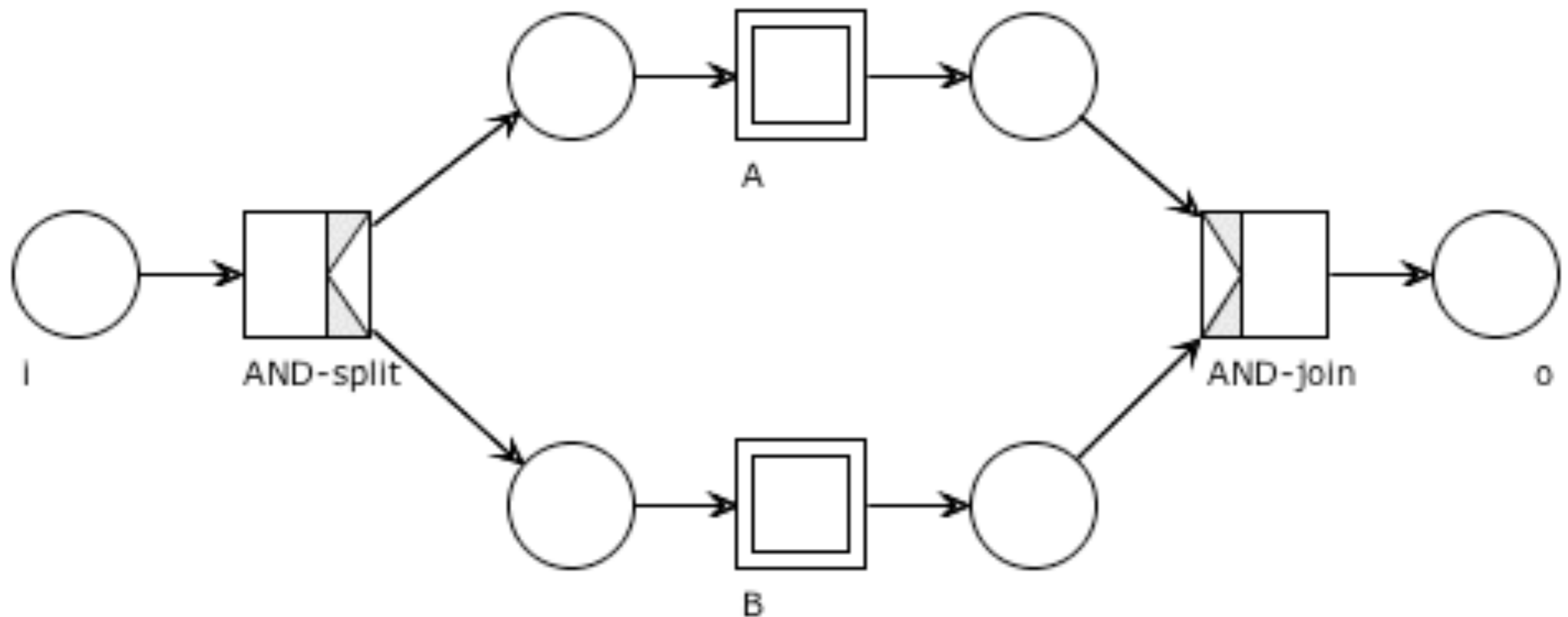
Sequencing

B is executed after A
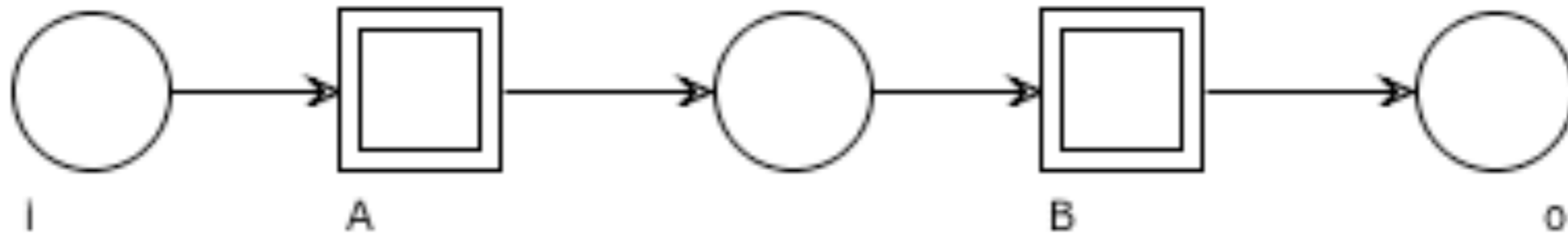
Parallelism (AND-split + AND-join)

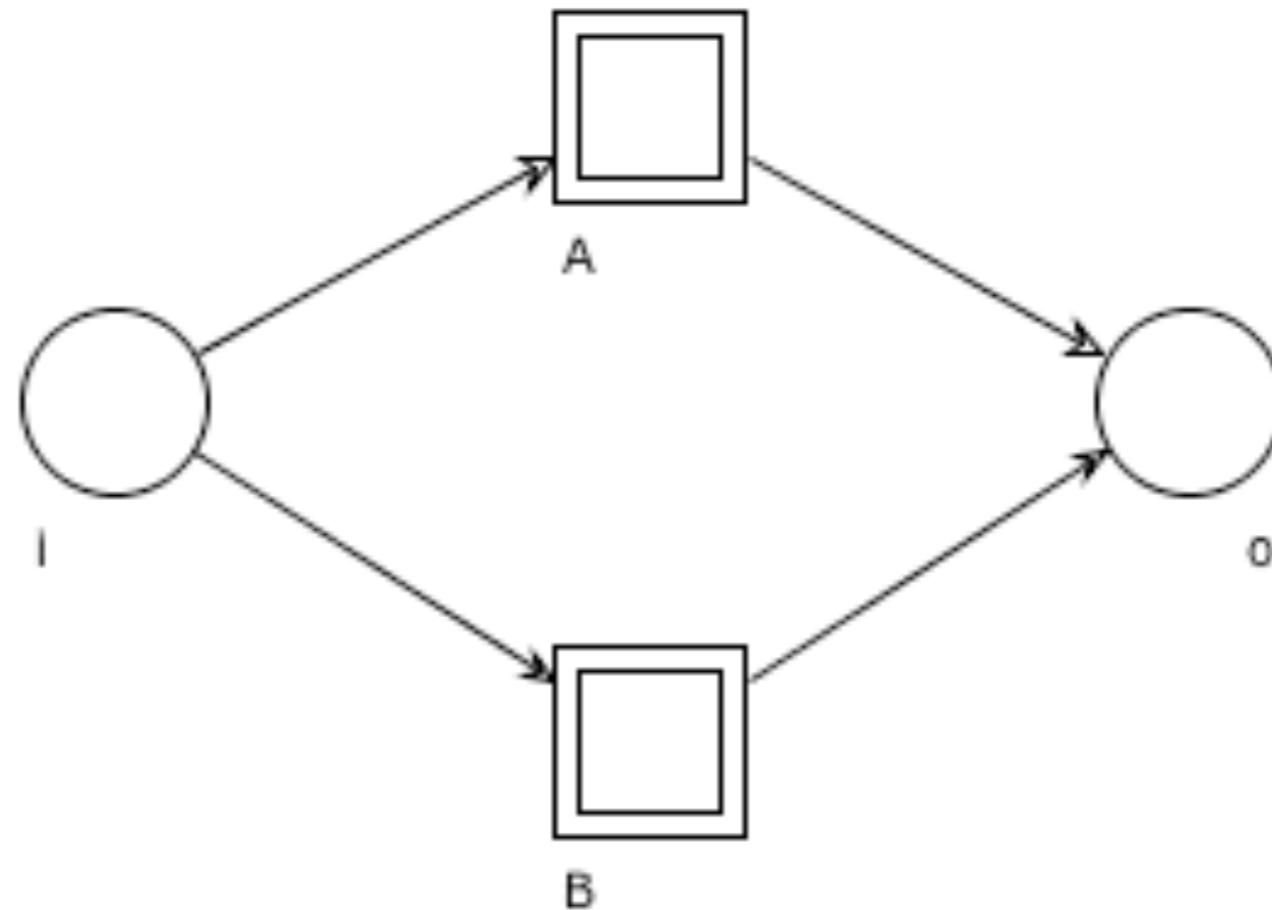A and B are both executed in no particular order
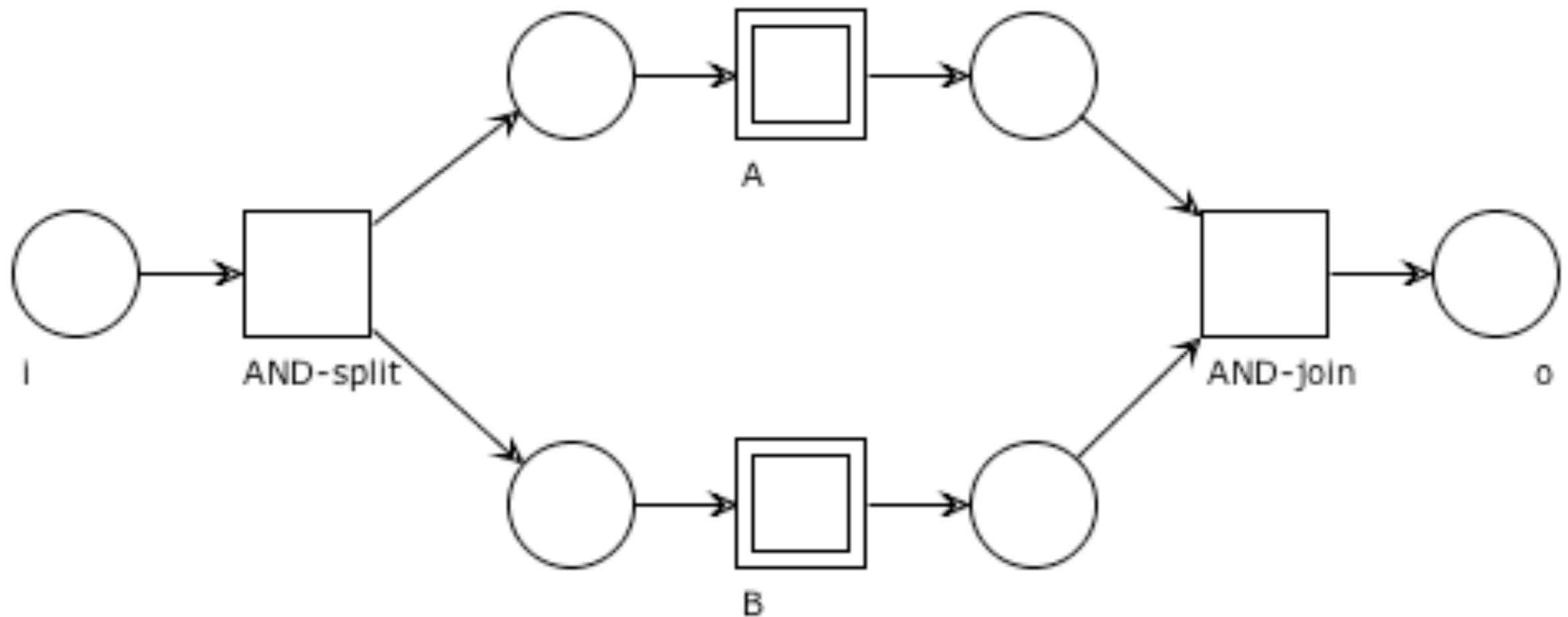
Parallelism ("sugared" version)

Decorated version for business process stakeholders
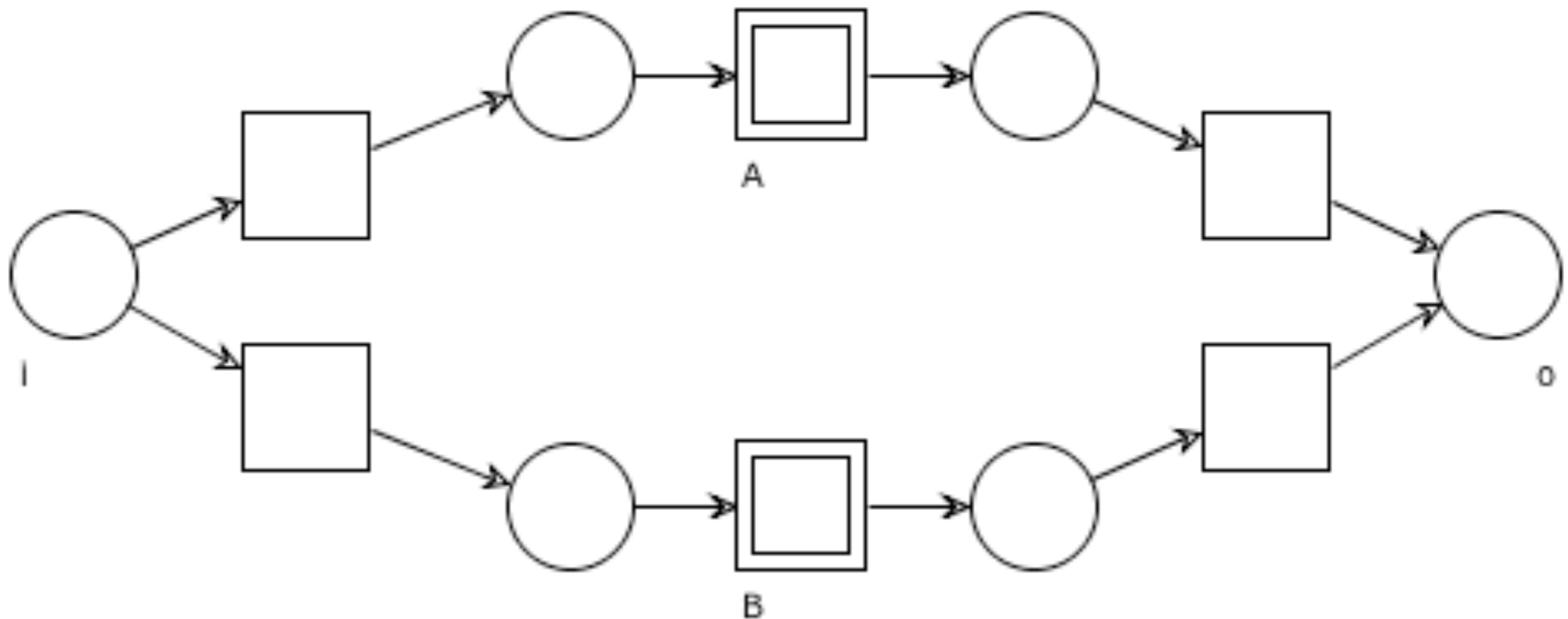
Deferred choice (XOR-split + XOR-join)

Either A or B is executed (choice is **implicit**)
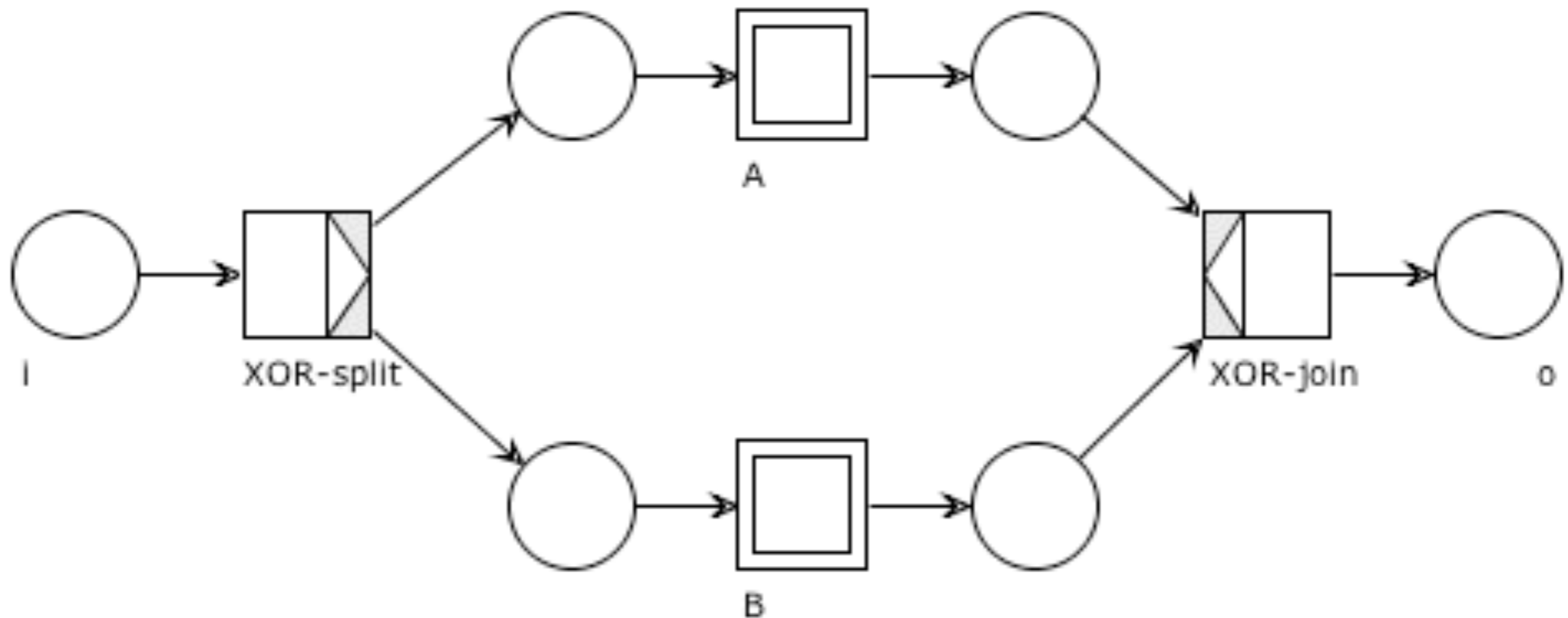
Explicit choice
(XOR-split + XOR-join)

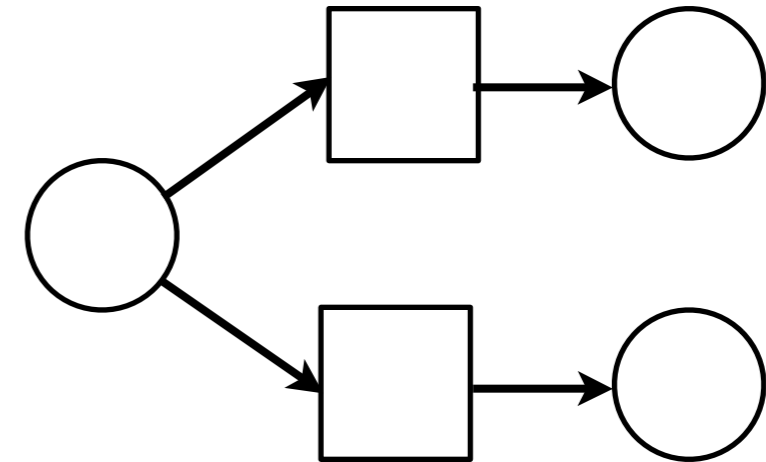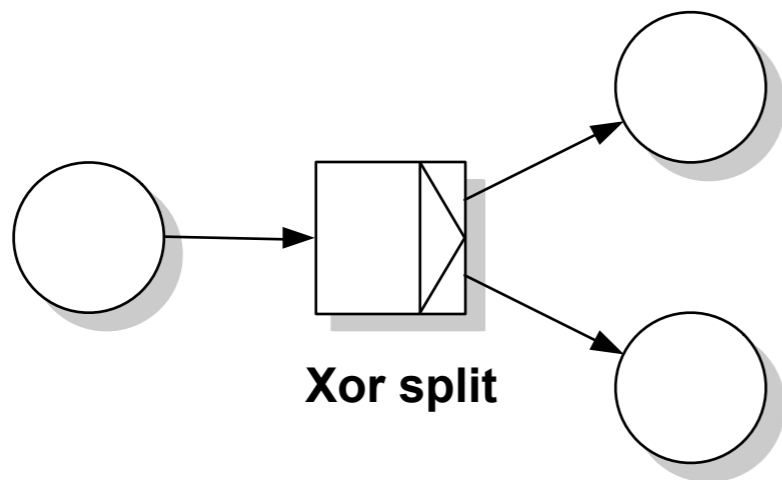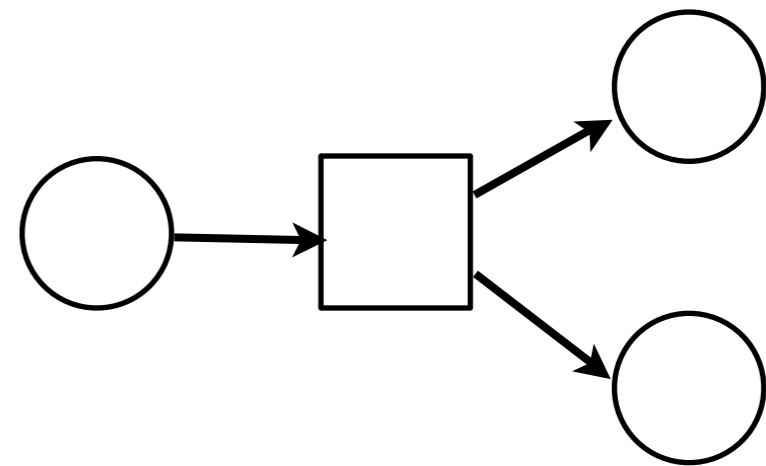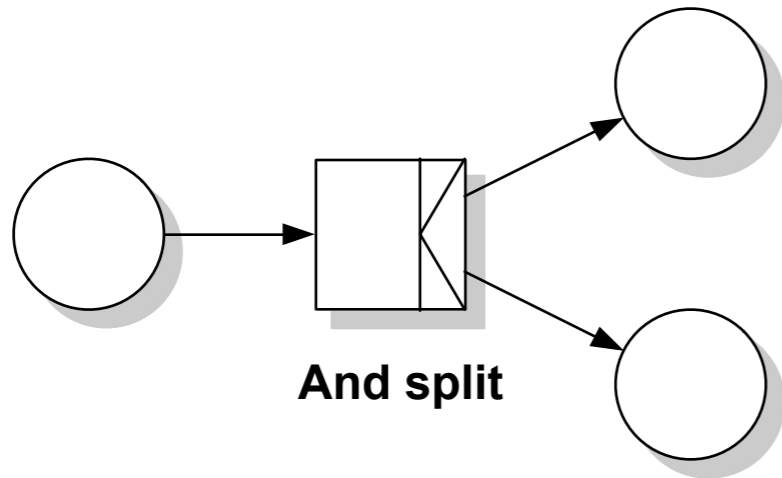Either A or B is executed (choice is **explicit**)

Choice ("sugared" version)
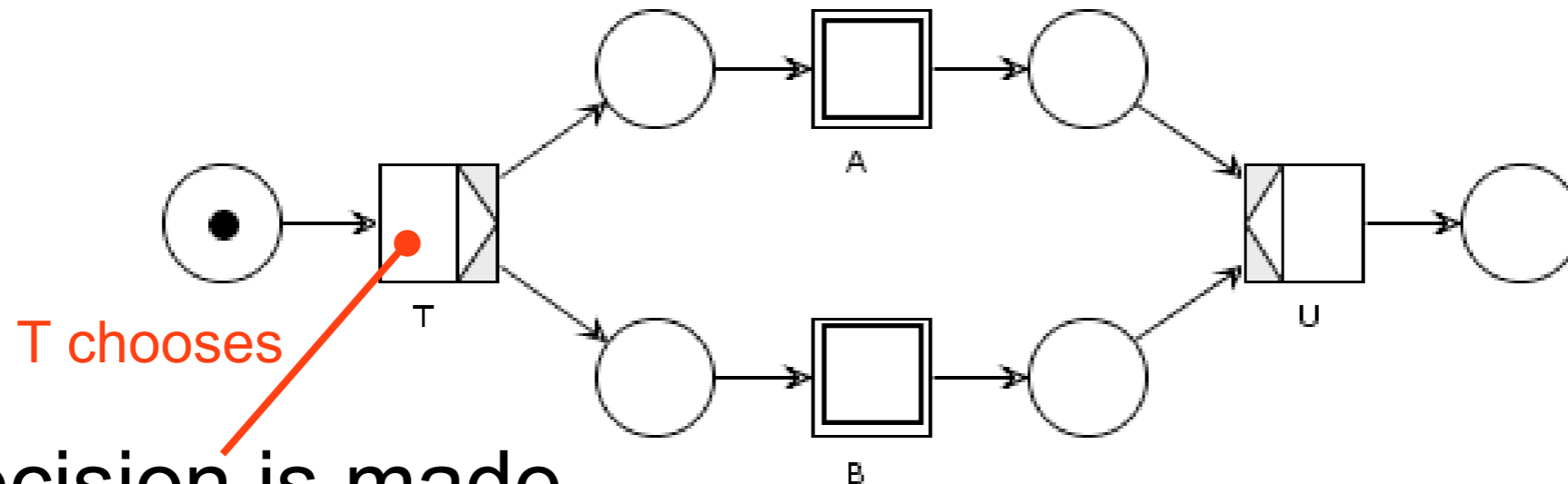
Decorated version for business process stakeholders

Syntax Sugar

And split

Xor split

Remember

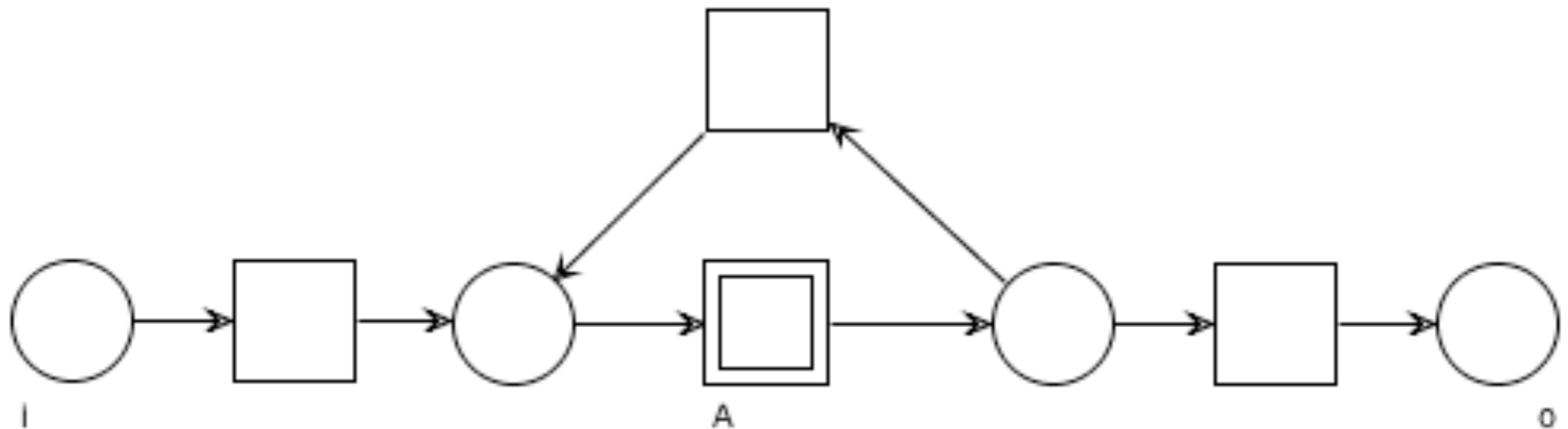Explicit choice ≠ Implicit choice

T chooses

The decision is made
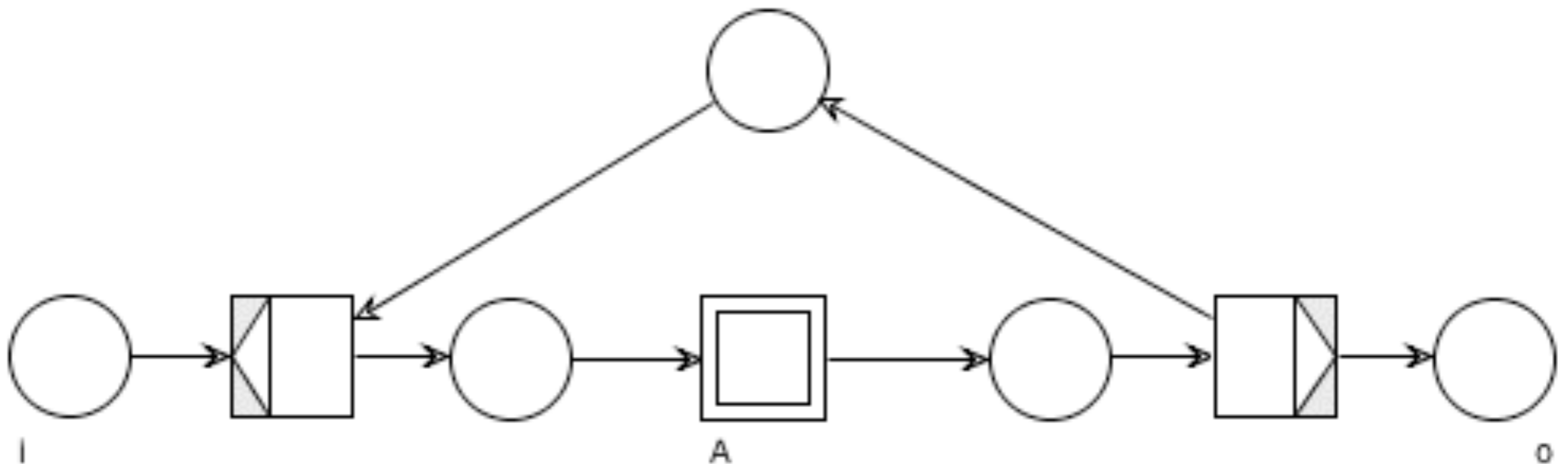at different points in time

A or B
chooses
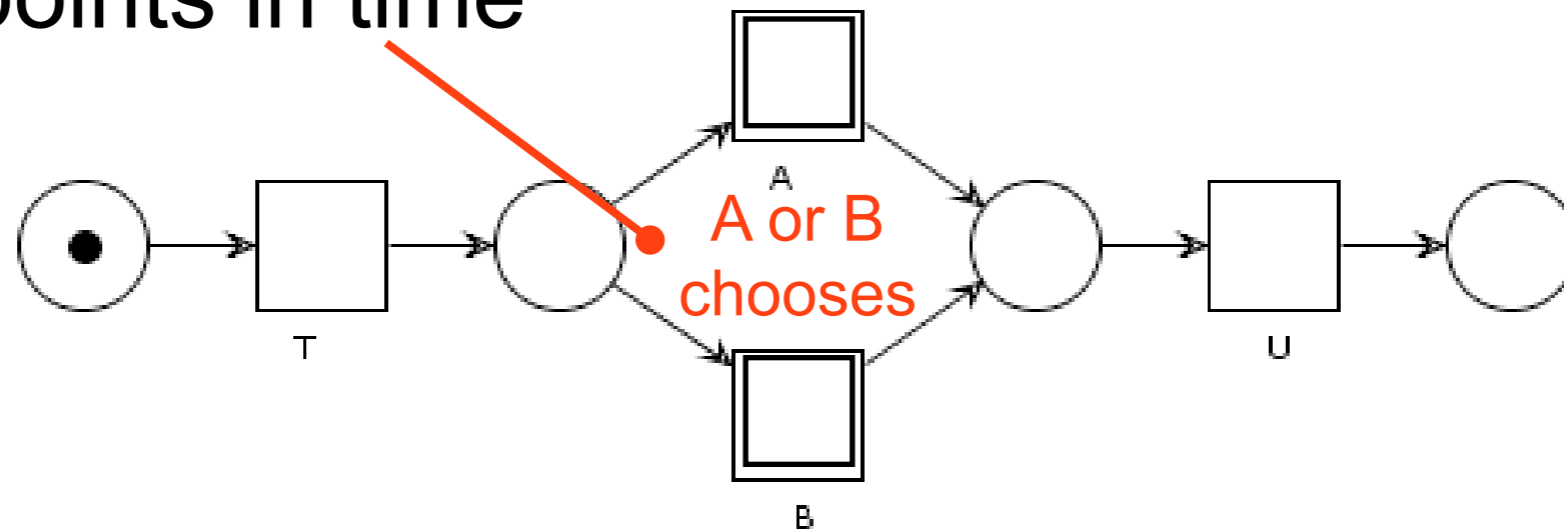
Iteration
(one or more time)
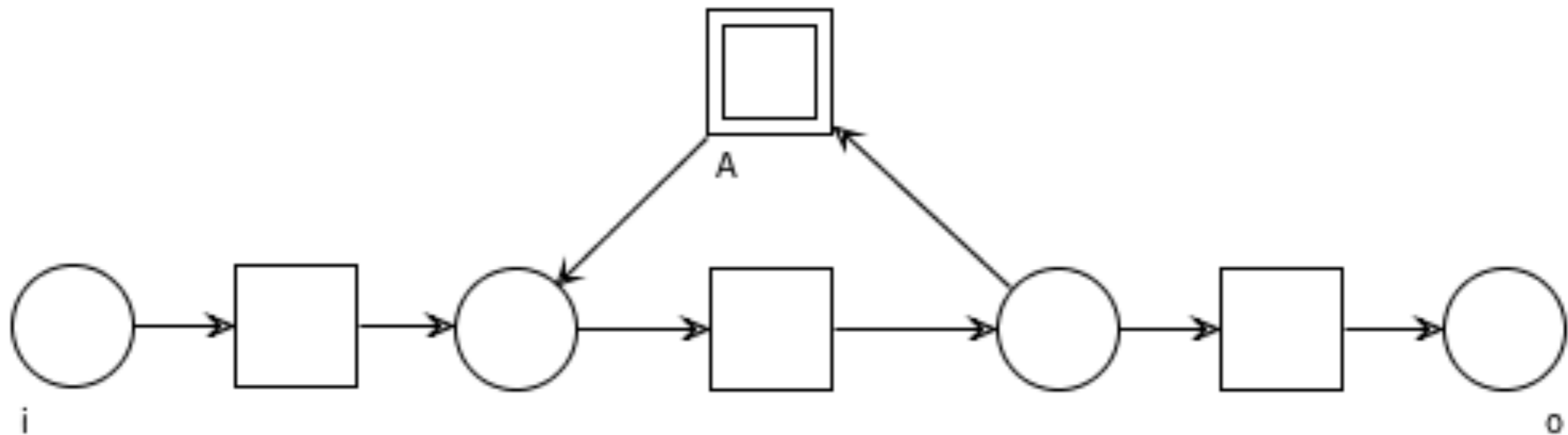
A is executed 1 or more time

One-or-more iteration ("sugared" version)
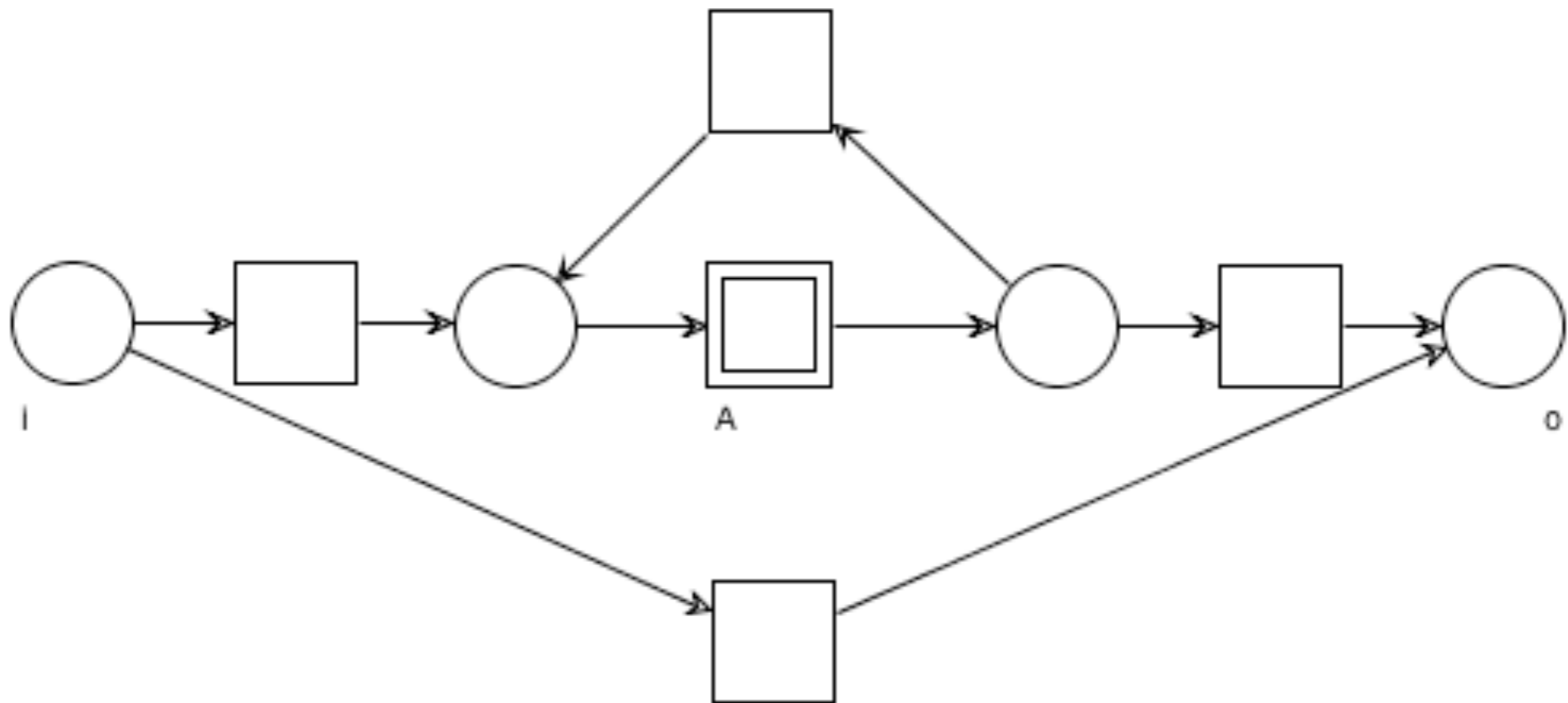
Decorated version for business process stakeholders

Iteration
(zero or more time)
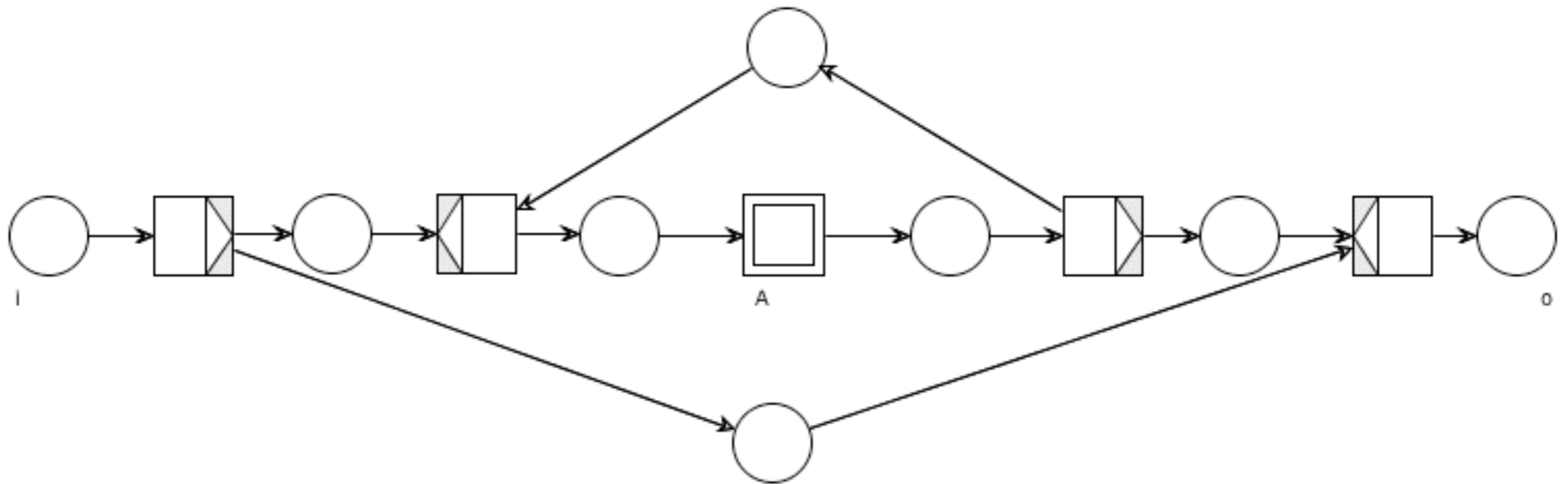
A is executed 0 or more time

Iteration
(zero or more time)

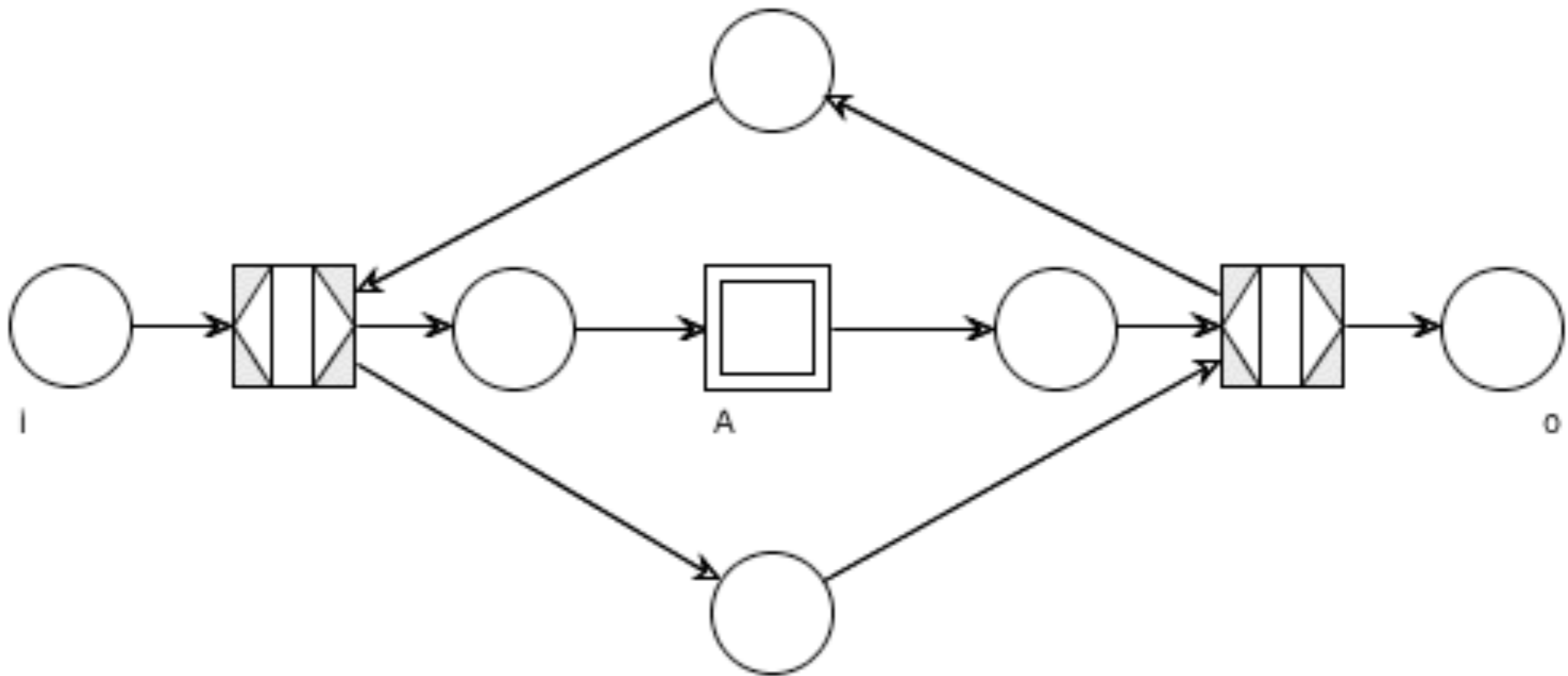A is executed 0 or more time

Zero-or-more iteration ("sugared" version)

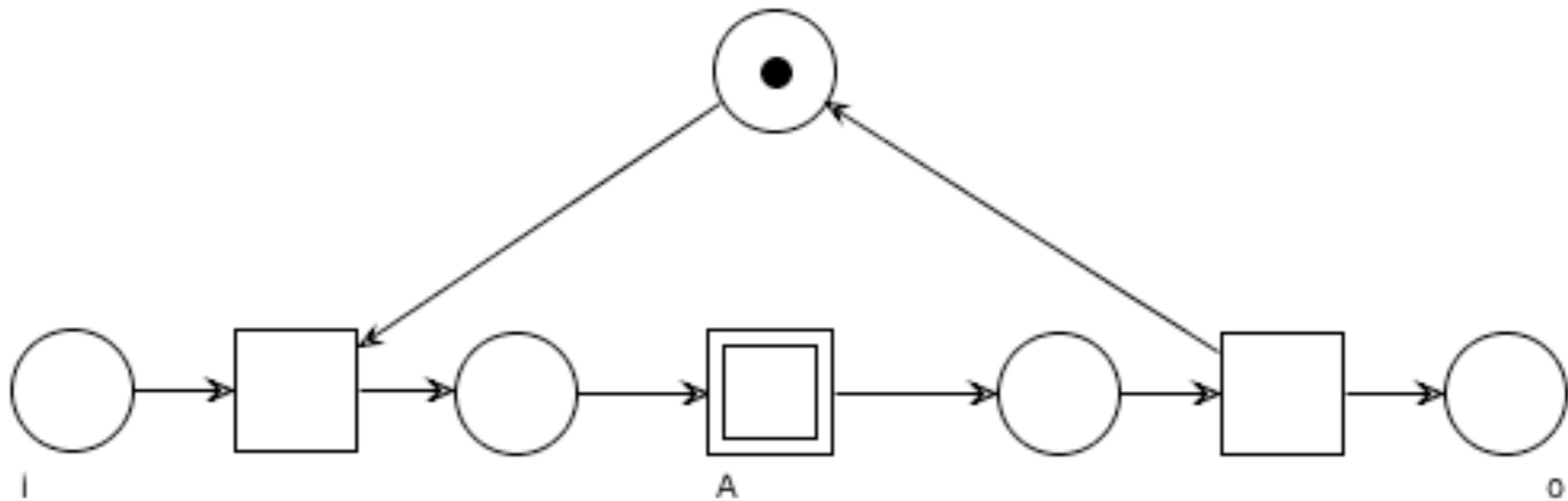Decorated version for business process stakeholders

Zero-or-more iteration (simplified version)

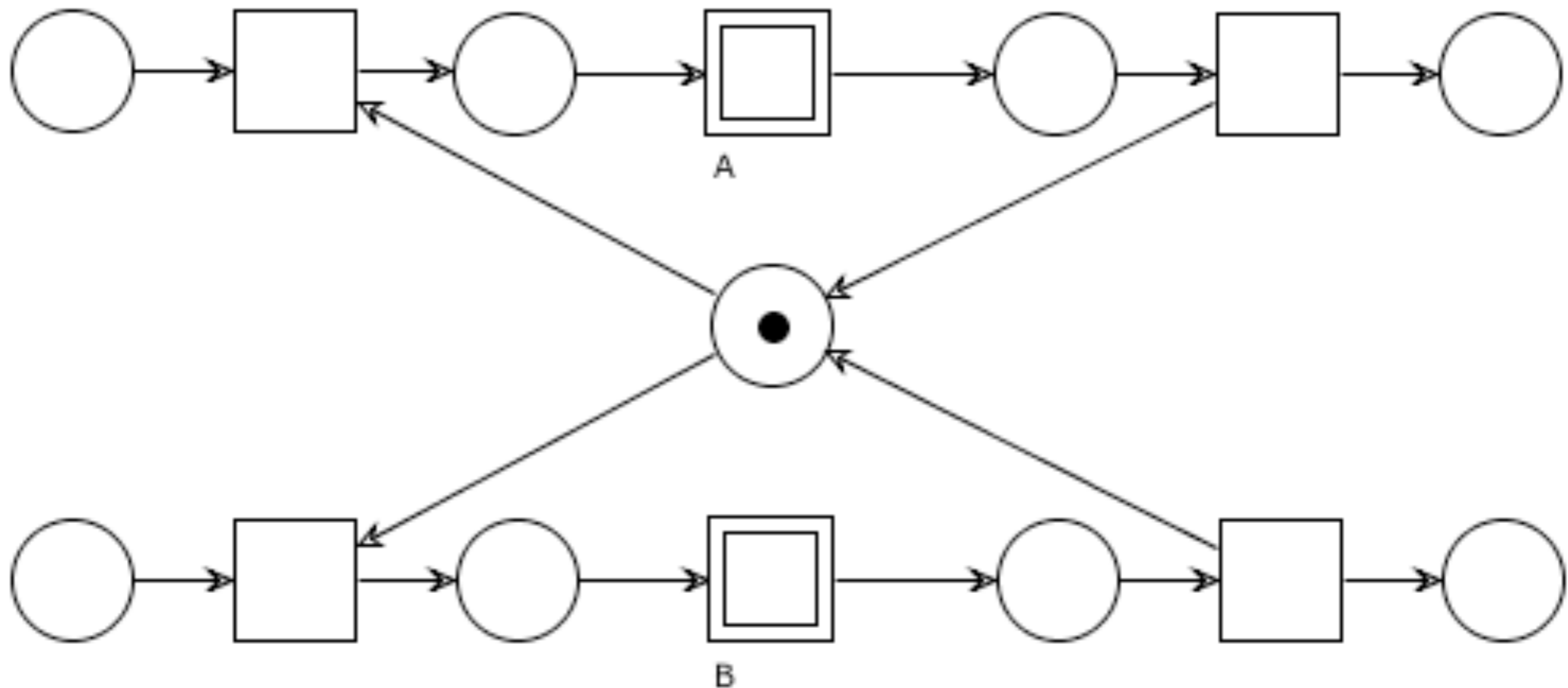Decorated version for business process stakeholders

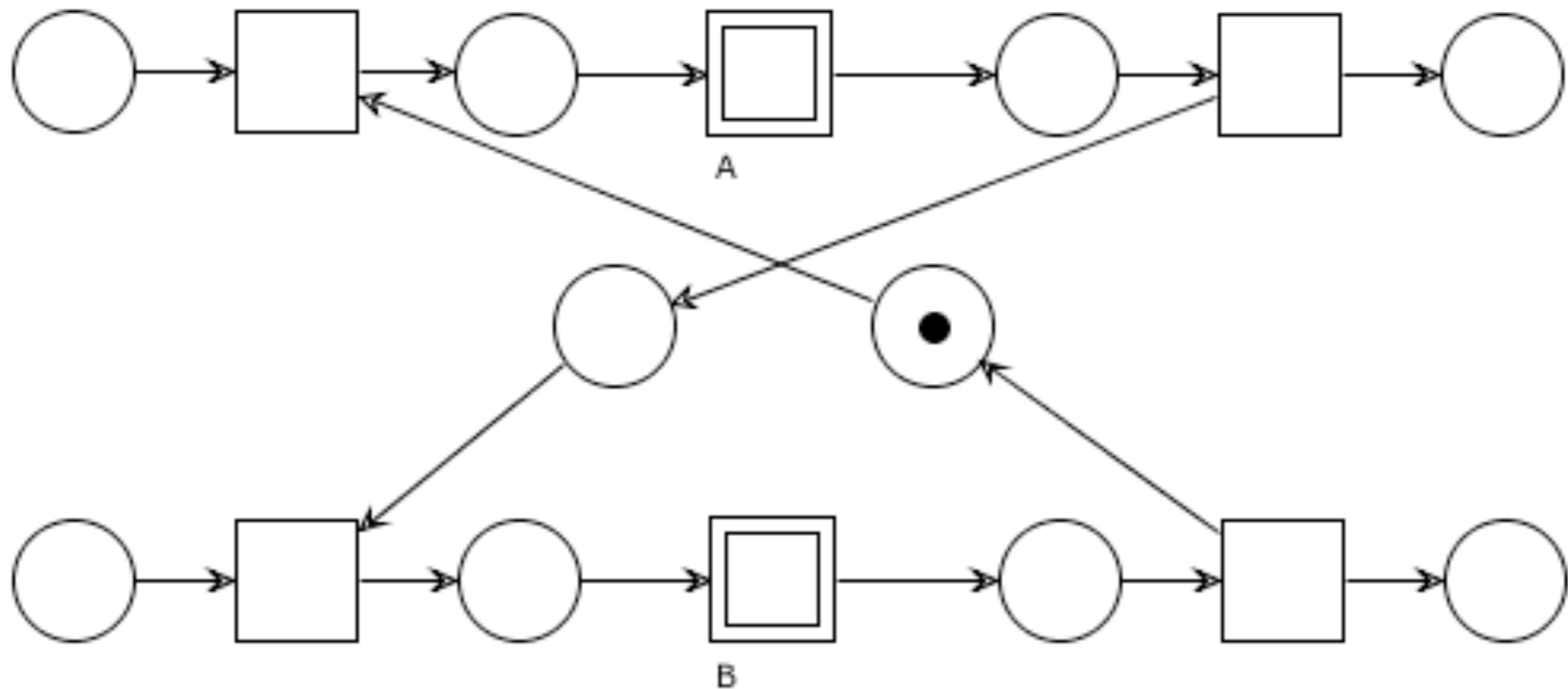# One serve per time

Multiple activations are handled one by one

Mutual exclusion

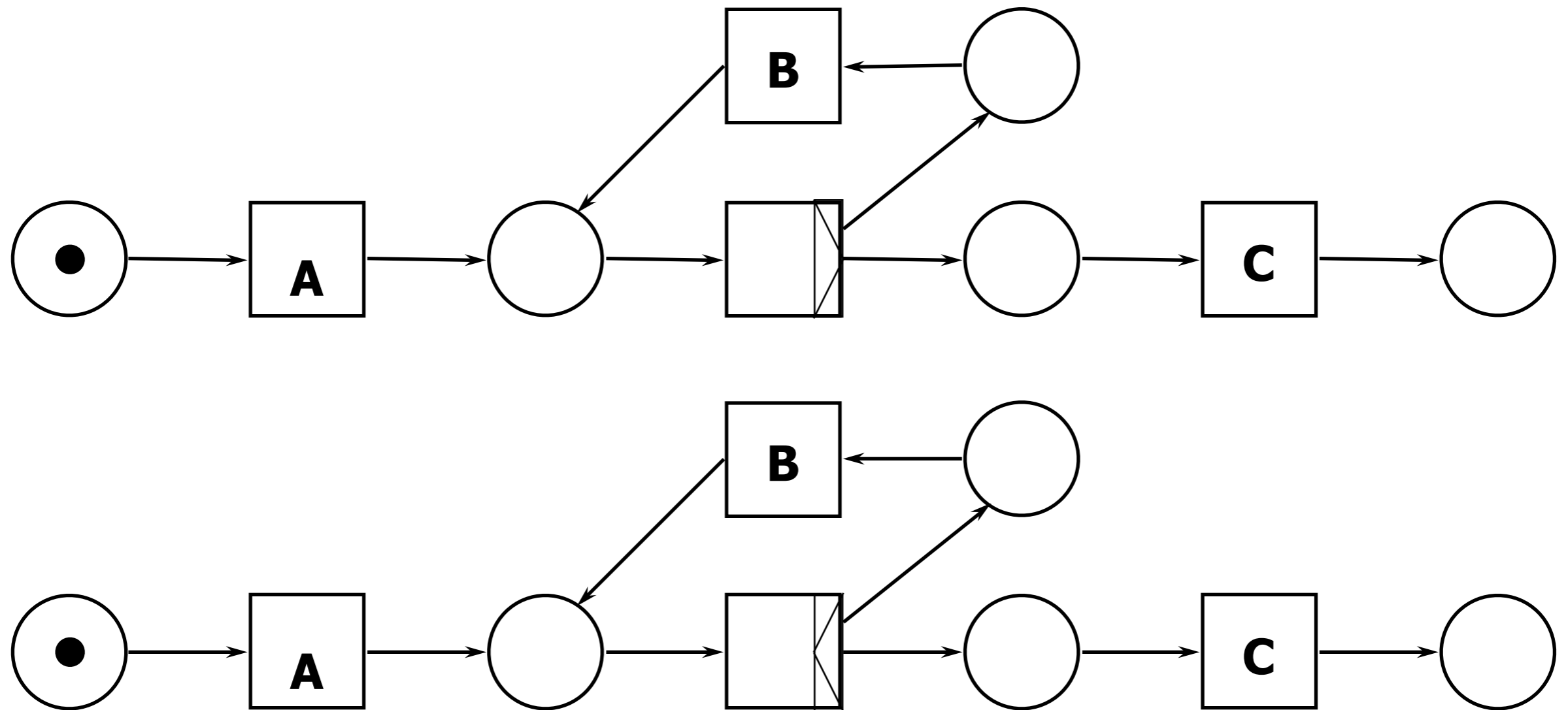A and B cannot execute concurrently

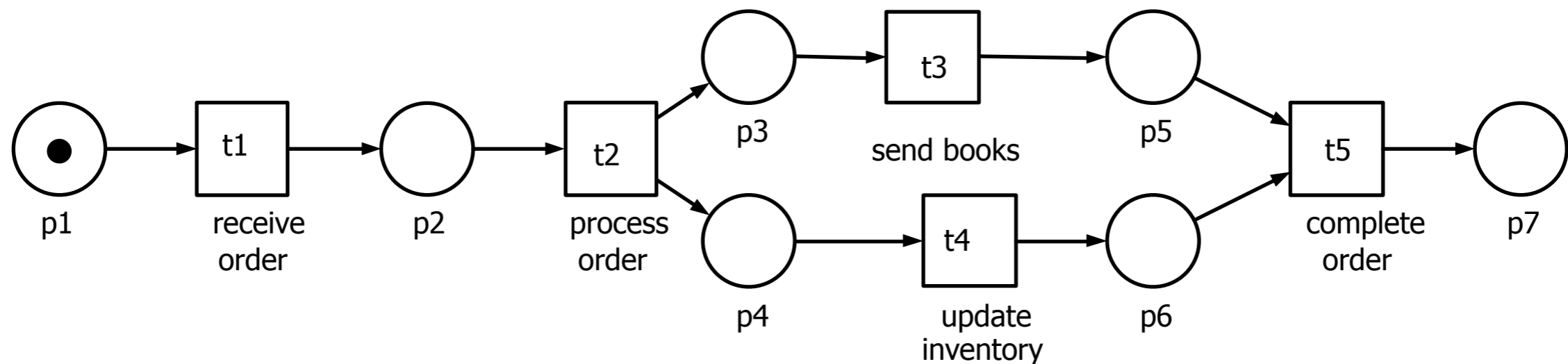# Alternation

A and B execute one time each (A first)

Question time

What's the difference (also in terms of firing sequences)?

Exercises

- Which "patterns" can be found in the workflow net below?
- "Sugarize" the net
- Draw the corresponding Reachability Graph
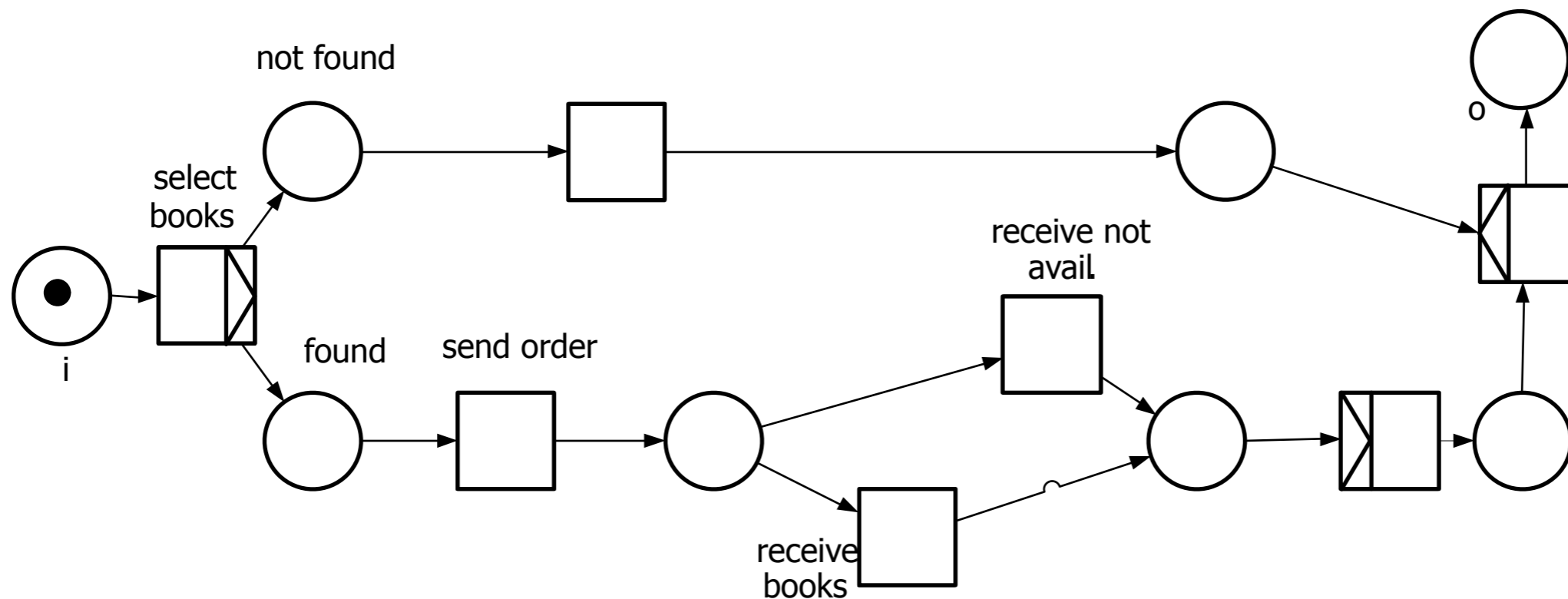- What are the possible firing sequences?

Exercises

- Which "patterns" can be found in the workflow net below?

- "Sugarize" the net (where it makes sense)

- Name all places and draw the Reachability Graph
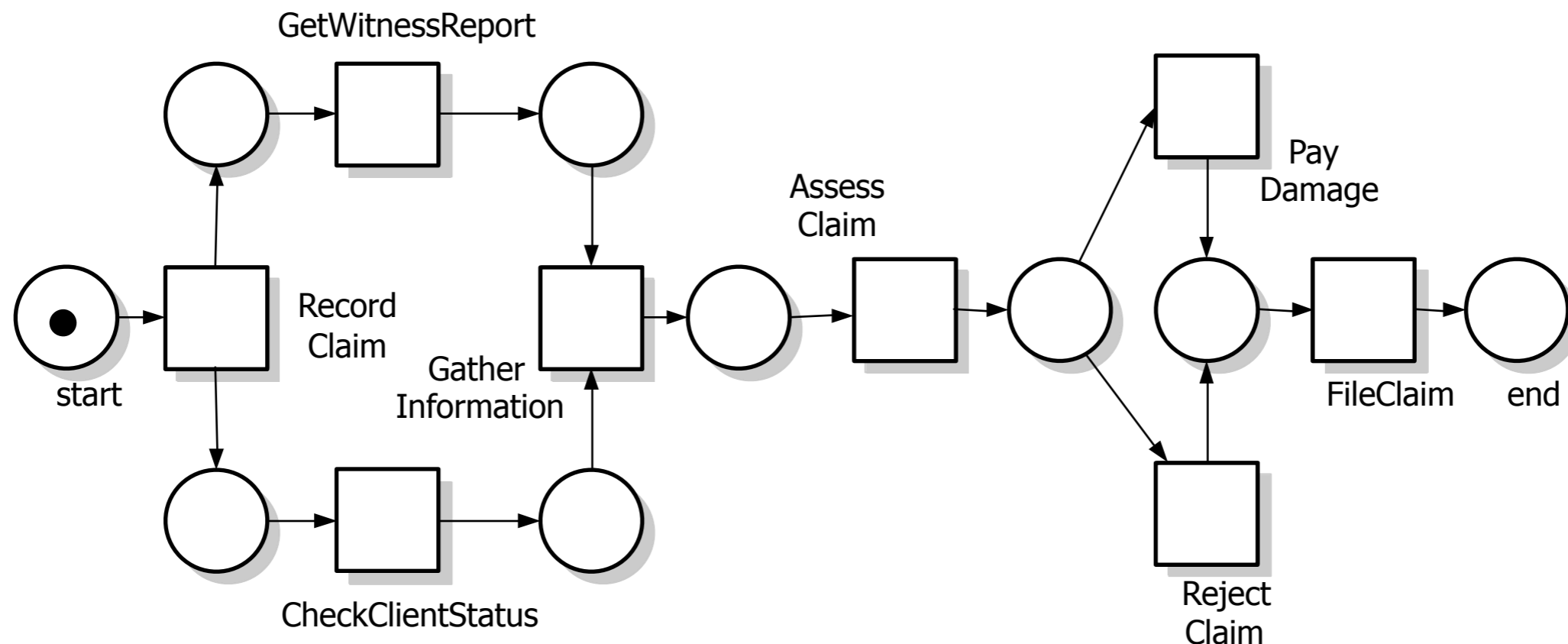
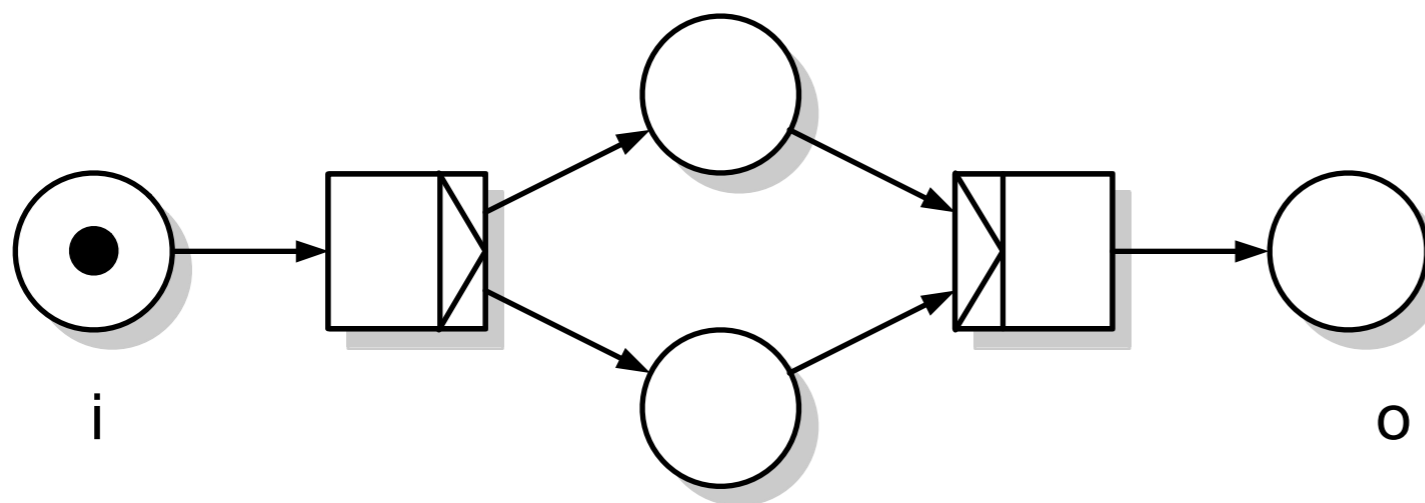# Exercises

- "Desugarize" the workflow net below, then name all places and all transitions
- Draw the corresponding Reachability Graph
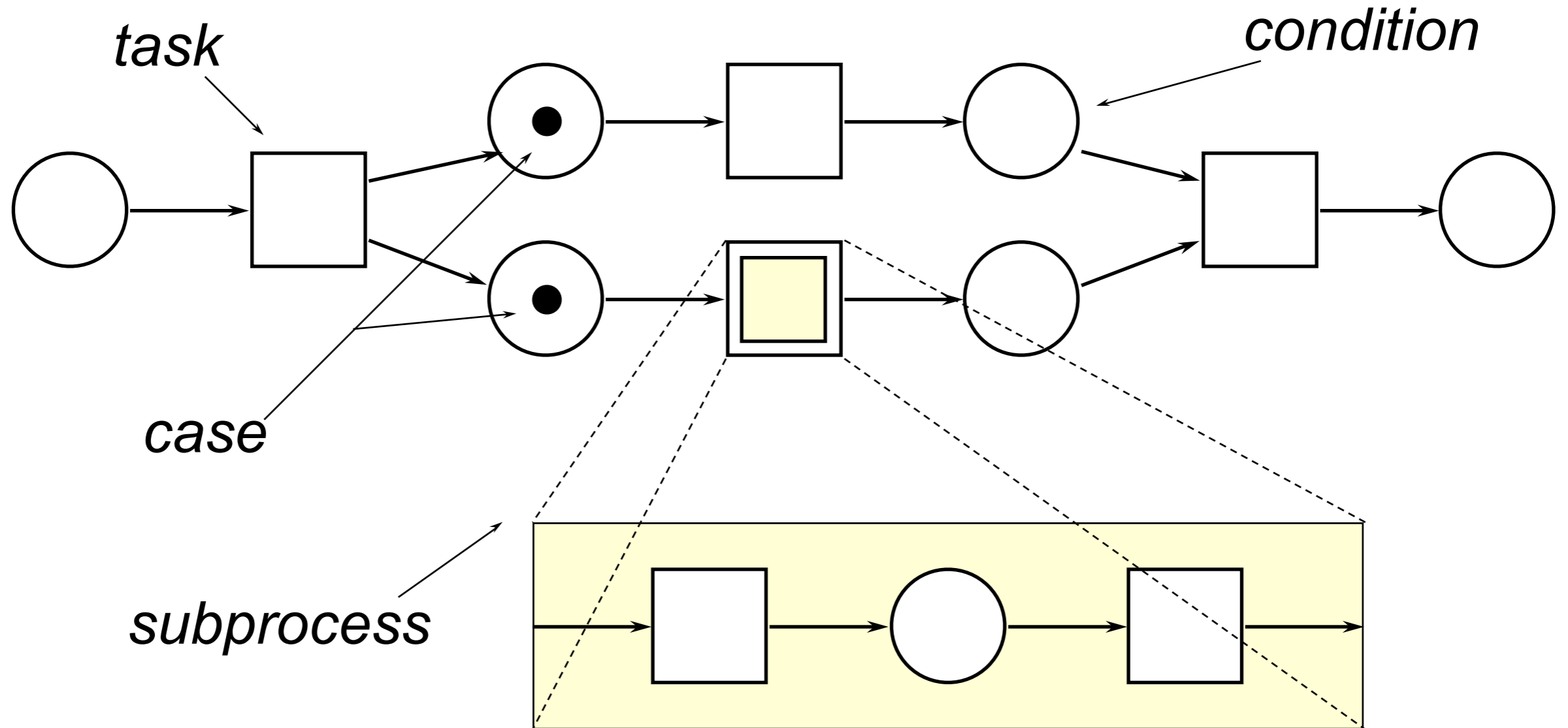- What are the possible firing sequences?

Exercises

- "Desugarize" the workflow nets below, then name all items
- Draw the corresponding Reachability Graphs
- What are their possible firing sequences?

Subprocesses

task

condition

case
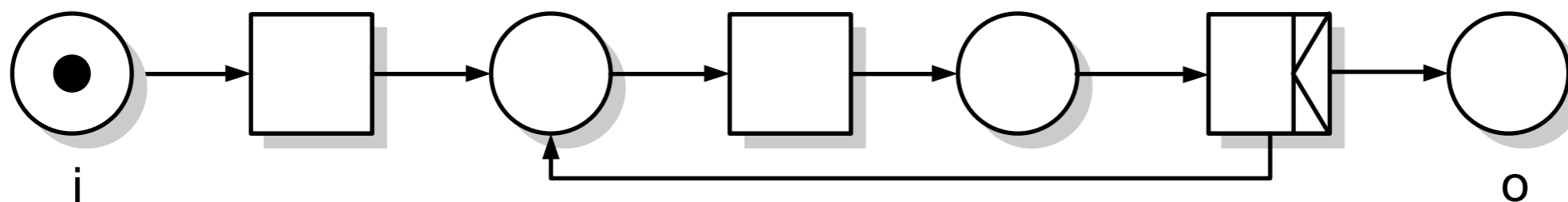
subprocess

Triggers

Execution constraints can depend on the environment in which processes are enacted.

In the contexts of workflow nets, transitions can be annotated with the information on who (or what) is responsible for the "firing" of that task.

All transitions that are not annotated can fire automatically

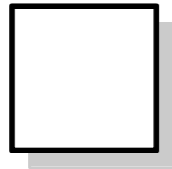Such annotations are called **triggers**

Triggers
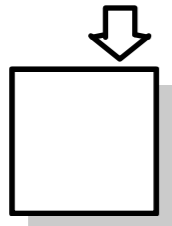
Triggers can be:

the receipt of a message

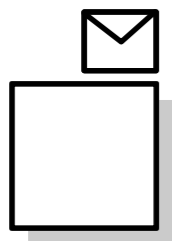the expiration of a time-out

a human interaction
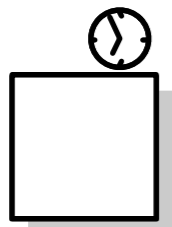
Symbols for triggers

Automatic Trigger : Task enacted automatically

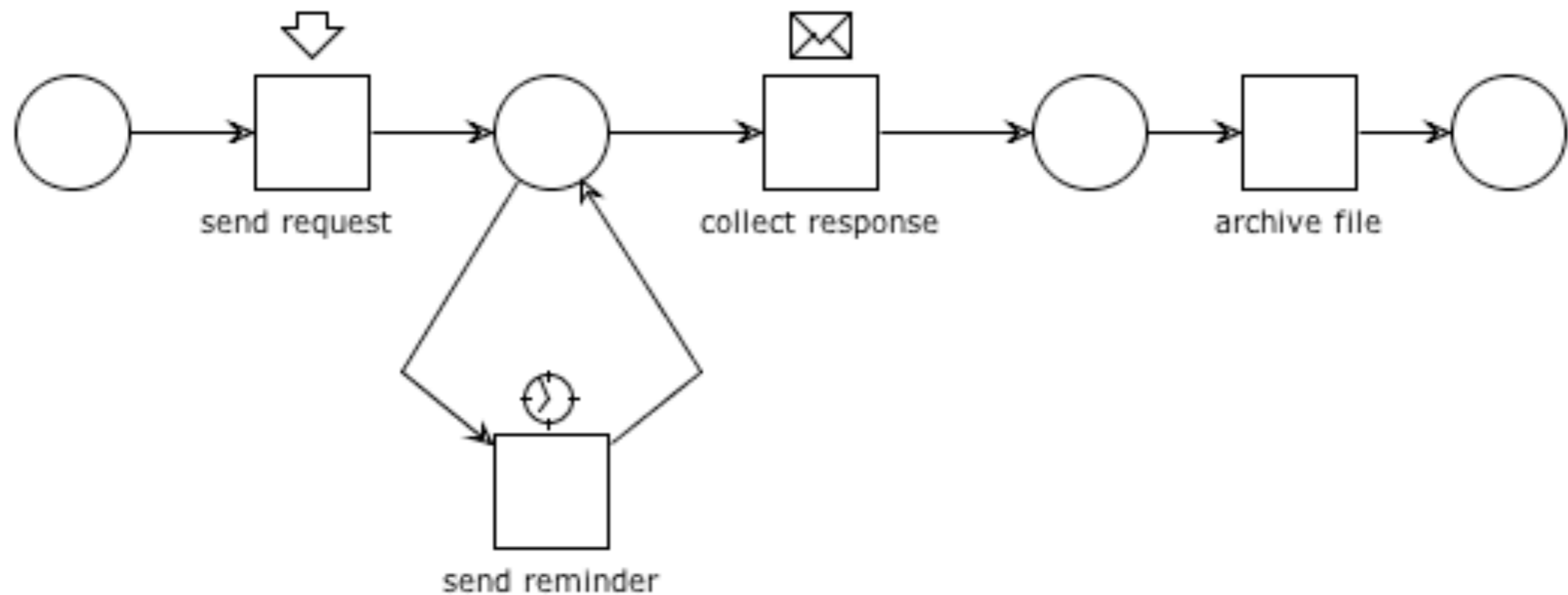User Trigger : A human user takes initiative and starts activity

External Trigger : External event required to start activity

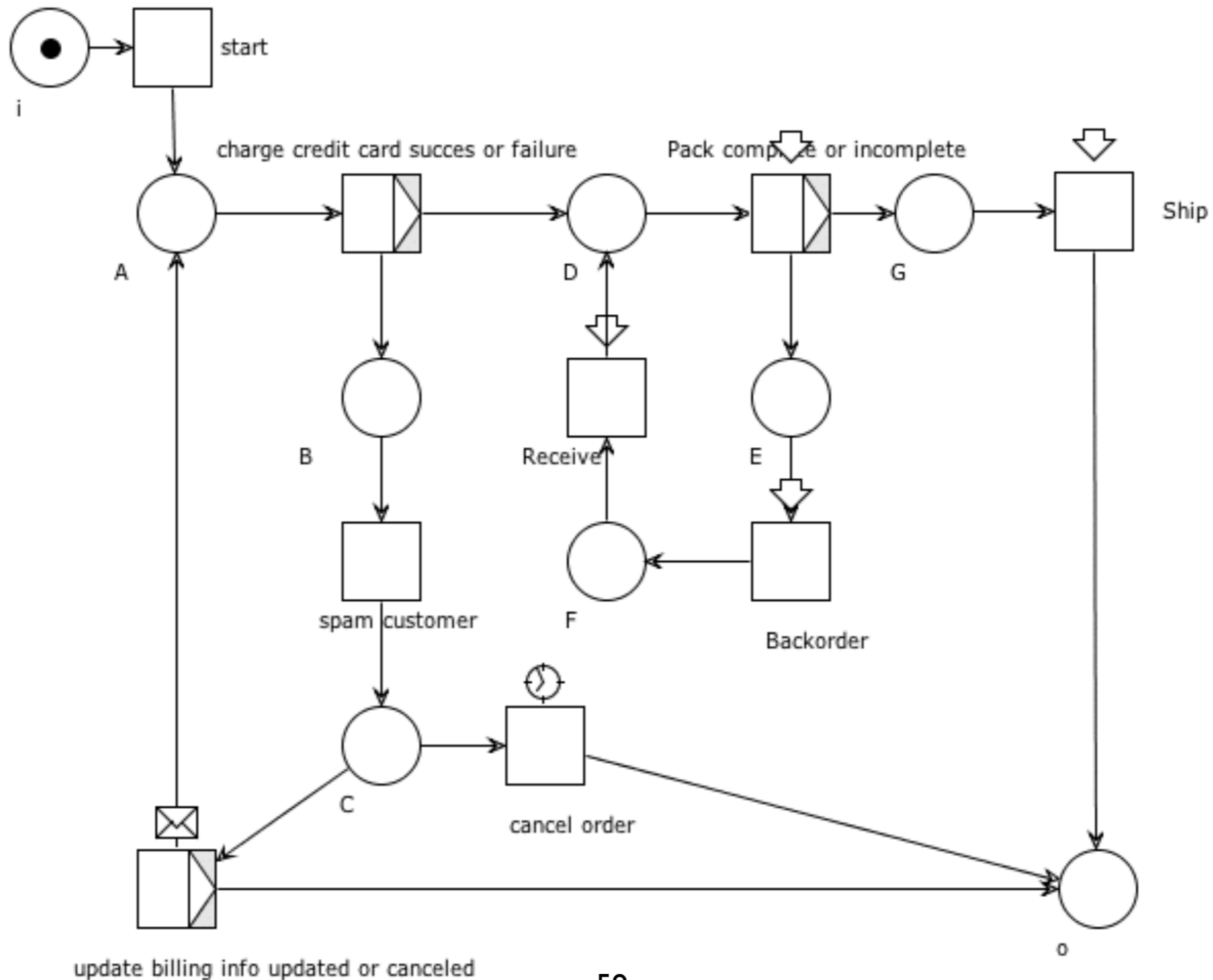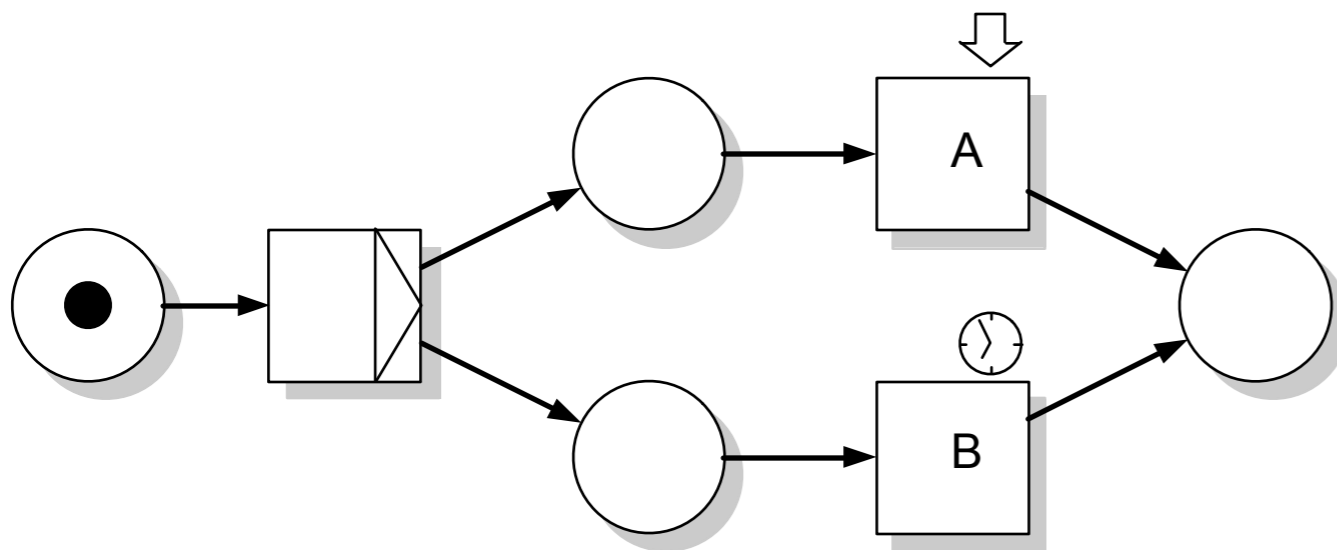Time Trigger : Activity started when timer elapses
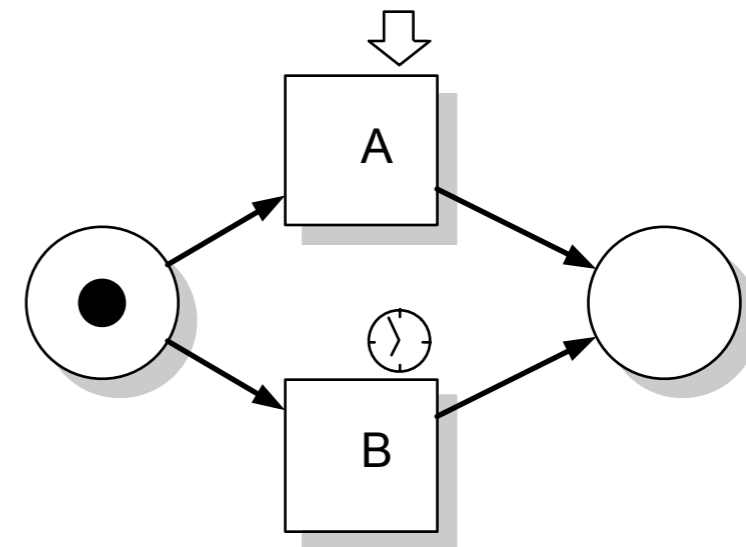
Triggers: example

Triggers: example

59

Explicit vs Implicit XOR-split

(a) *Explicit xor split* does not enable A and B concurrently

(b) *Implicit xor split* enables A and B concurrently

Encoding triggers

Trigger activities can formally be represented by places with an arc to the respective transition...
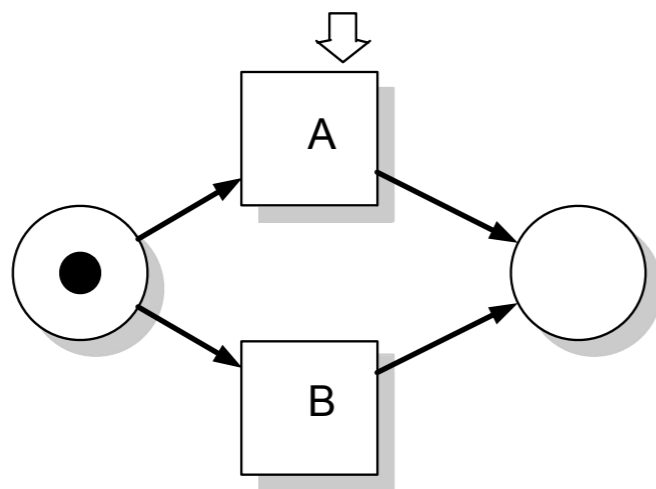
(a) Transition A started by user trigger

(b) Representation of user trigger by additional place and additional arc

but such nets would not be workflow nets!
(unless the resource is allocated at the beginning and deallocated at the end)

Terminology: revisited

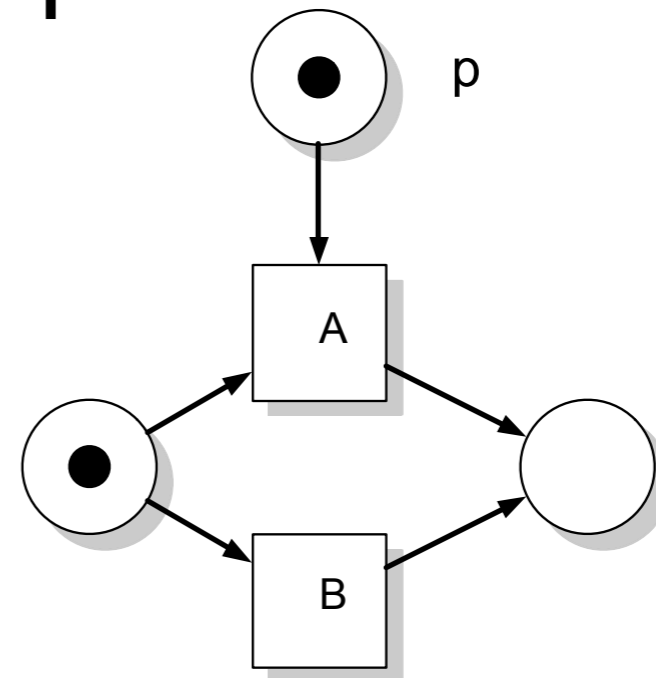**task:** A logical step which may be executed for many cases

work item = task + case
A logical step which may be executed for a specific case

activity = task + case + (trigger) + (resource)
The actual execution of a task for a specific case

(work items and activities are task instances)

Motivation for the analysis

Old BPs generally had simple structures and a physical document linked to each case (a sort of token that serializes tasks)

ICT developments (databases and networks) allowed terrific enhancements... and dangers
information is shared
parallelization is possible
completion times can be shortened
BPs are larger, with increasing complexity
flawed situations are more frequent

Is this WF net ok?