### Business Processes Modelling MPB (6 cfu, 295AA)



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13 - Workflow nets



#### We study some special kind of Petri nets, that are suitable models of workflows

Ch.4.4 of Business Process Management: Concepts, Languages, Architectures

# There are many, many variants of Petri nets

# Example: Coloured nets (also called High-Level)

A coloured net is a Petri net whose tokens can carry data and whose transitions can check data (see exact definition in Weske's book)



M. Weske: Business Process Management © Springer-Verlag Berlin Heidelberg 2007

# Workflow nets

# Workflow nets features

Tailored to the representation of business processes

Formal (unambiguous) semantics

Structural restrictions

Decorated graphical representation

# Workflow net: idea



# Workflow net

#### **Definition:**

A Petri net (P, T, F) is called **workflow net** if:

- 1. there is a distinguished *initial place*  $i \in P$  with  $\bullet i = \emptyset$
- 2. there is a distinguished final place  $o \in P$  with  $o \bullet = \emptyset$
- 3. every other place and transition belongs to a path from i to o

# Workflow net: Rationale

- 1. a token in i represents a process instance not yet started
- 2. a token in *o* represents a finished case
- 3. each place and each transition can participate in a case

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# Basic properties

Lemma: In a workflow net there is a unique node with no incoming arc

Lemma: In a workflow net there is a unique node with no outgoing arc

Exercise: Guess which nodes are those

**Exercise**: Prove the above lemmas (hint: suppose the nodes are not unique, reach a contradiction)





Yes





No (no initial place)

















Yes

### Syntax sugar: split



### Syntax sugar: join



# Syntax sugar: any combination is also possible



# Syntax sugar: any combination is also possible



## Syntax sugar: a personal note







Chosen decorations are too similar!

Different meanings if differently placed!



Unnecessary for AND (redundant)!

### Syntax sugar: a personal note

Why there? Because of gateways





# Hierarchical structuring

Uniqueness of entry / exit point facilitate the hierarchical structuring of WF nets



#### http://woped.dhbw-karlsruhe.de/woped/

WoPeD

WoPeD Workflow Petri Net Designer Download WoPeD at Sourceforge!





# Language of a workflow net



The language of a workflow net is the set of firing sequences that go from i to o

$$L(N) = \{ \sigma \mid i \xrightarrow{\sigma} o \}$$

L(N) defines the admissible traces of the workflow

# Typical control flow aspects

Sequencing

Parallelism (AND-split + AND-join)

Selection (XOR-split + XOR-join)

Iteration (XOR-join + XOR-split)

Capacity constraints: Feedback loop Mutual exclusion Alternating

# Sequencing

B is executed after A



# Parallelism (AND-split + AND-join)

A and B are both executed in no particular order



# Explicit choice (XOR-split + XOR-join)

Either A or B is executed (choice is **explicit**)





# Deferred choice

Either A or B is executed (choice is **implicit**)



### Remember

Explicit choice *≠* Implicit choice



# Iteration (one or more times)

A is executed 1 or more times



# One-or-more iteration ("sugared" version)

**Decorated version** 





# Zero-or-more iteration ("sugared" version)

**Decorated version** 



# One serve per time

Multiple activations are handled one by one



# Mutual exclusion

A and B cannot execute concurrently



### Alternation

A and B execute one time each (A first)



# Question time

Consider the workflow net below

![](_page_47_Figure_2.jpeg)

How many times can A be executed? How many times can B be executed? Can a firing sequence contain two As in a row? Can a firing sequence contain two Bs in a row? Can a firing sequence contain more Bs than As?

# Question time

Consider the workflow net below

![](_page_48_Figure_2.jpeg)

How many times can A be executed? 1 or more How many times can B be executed? 0 or more Can a firing sequence contain two As in a row? yes Can a firing sequence contain two Bs in a row? no Can a firing sequence contain more Bs than As? no

- Which "patterns" can be found in the workflow net below?
- Draw the corresponding Reachability Graph
- What is its language?

![](_page_49_Figure_4.jpeg)

- Which "patterns" can be found in the workflow net below?
- "Sugarize" the net (where it makes sense)
- Name all places and draw the Reachability Graph
- What is its language?

![](_page_50_Figure_5.jpeg)

- "Desugarize" the workflow net below
- Name all nodes and draw the Reachability Graph
- What is its language?

![](_page_51_Figure_4.jpeg)

- "Desugarize" the workflow nets below
- Name all nodes and draw the Reachability Graphs
- What are their languages?

![](_page_52_Figure_4.jpeg)

# Triggers

Execution constraints can depend on the environment in which processes are enacted.

In workflow nets, transitions can be decorated with the information on who (or what) is responsible for the "firing" of that task.

Such annotations are called **triggers** 

# Triggers

Triggers can be:

a human interaction

the receipt of a message

the expiration of a time-out

Transitions with no trigger can fire automatically

# Symbols for triggers

![](_page_55_Figure_1.jpeg)

Automatic Trigger: Task enacted automatically

![](_page_55_Picture_3.jpeg)

User Trigger: A human user takes initiative and starts activity

![](_page_55_Picture_5.jpeg)

External Trigger: External event required to start activity

![](_page_55_Picture_7.jpeg)

Time Trigger: Activity started when timer elapses

# Triggers: example

![](_page_56_Figure_1.jpeg)

# Triggers: example

![](_page_57_Figure_1.jpeg)

![](_page_58_Picture_0.jpeg)

(a) *Explicit xor split* does not enable A and B concurrently

(b) Implicit xor split enables A and B concurrently

# Motivation for the analysis

L(N) shows the correct ways to run the process if it is empty there is clearly some problem

Are we guaranteed that nothing can go wrong? Are we guaranteed that once a case is started it will reach an end?

BPs are large, with increasing complexity flawed situations are frequent

# Is this WF net ok?

![](_page_60_Figure_1.jpeg)