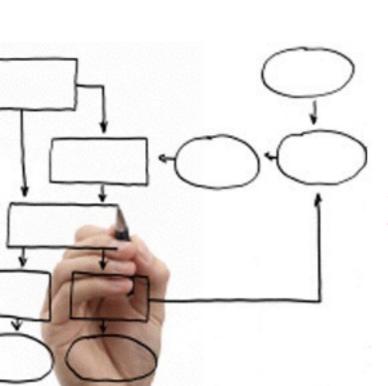
# Methods for the specification and verification of business processes MPB (6 cfu, 295AA)



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http://www.di.unipi.it/~bruni

14 - Sound by construction

### Object



We show a technique to build sound Workflow nets

# Soundness proof by construction

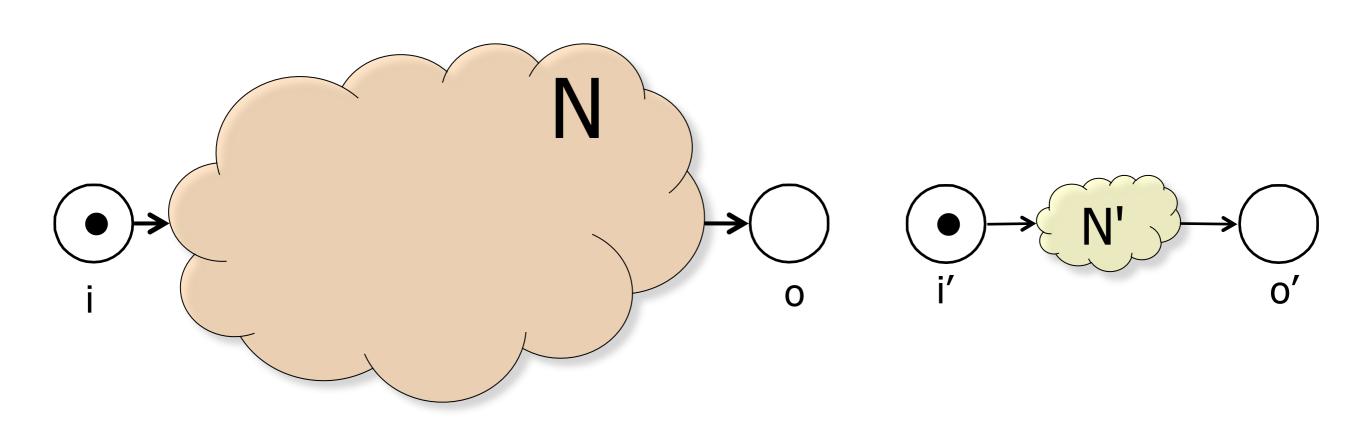
#### Idea

1. Find a suitable set of "building blocks"

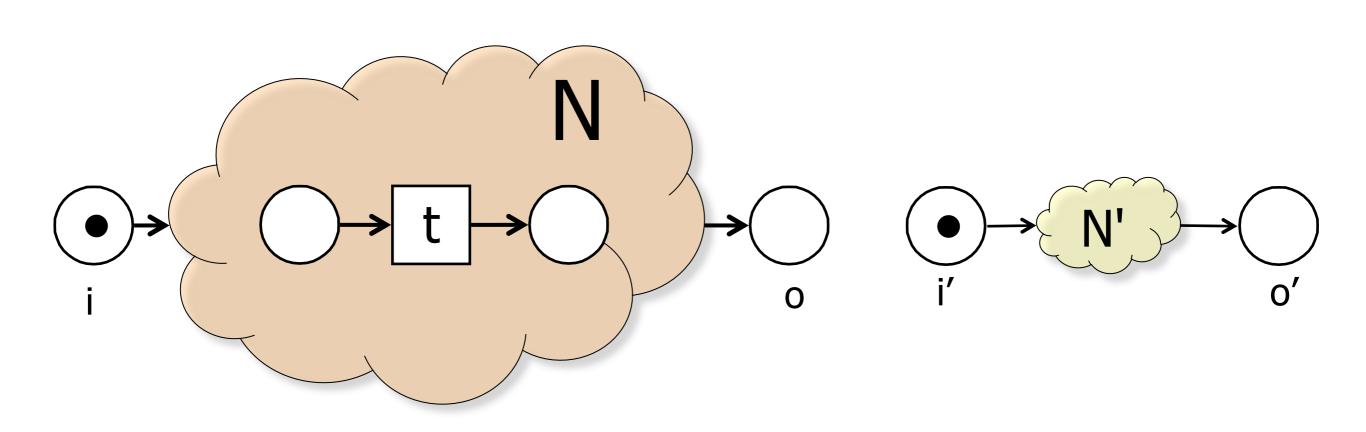
they are (small) workflow nets that can be (easily) proved to be **sound** and to be **safe** (1-bounded)

2. Define composition patterns so that by composing **safe and sound** WF nets we get **safe and sound** WF nets

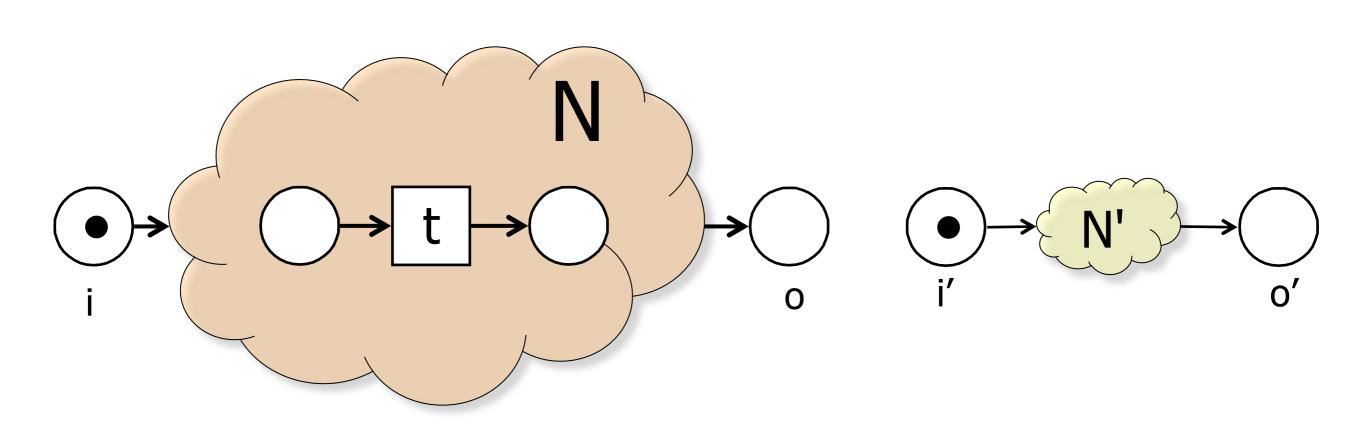
Let N, N' be two safe and sound workflow nets



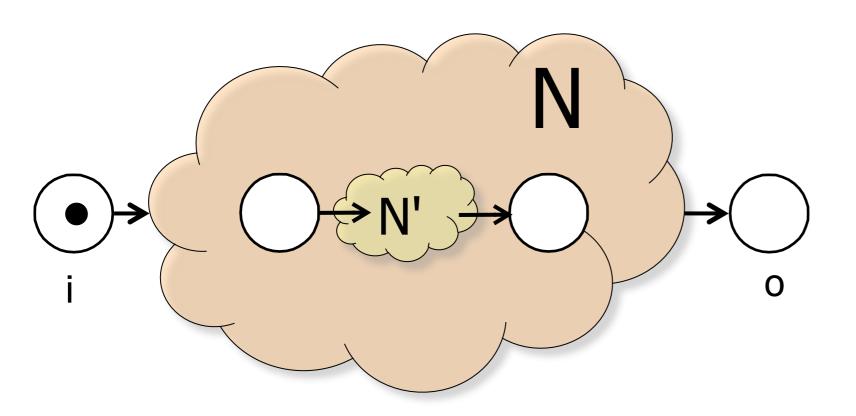
Let t be a task of N with exactly one input and one output place



Let N[N'/t] denote the net obtained by replacing the task t in N by N'



The net N[N'/t] is a sound and safe workflow net (proof omitted)



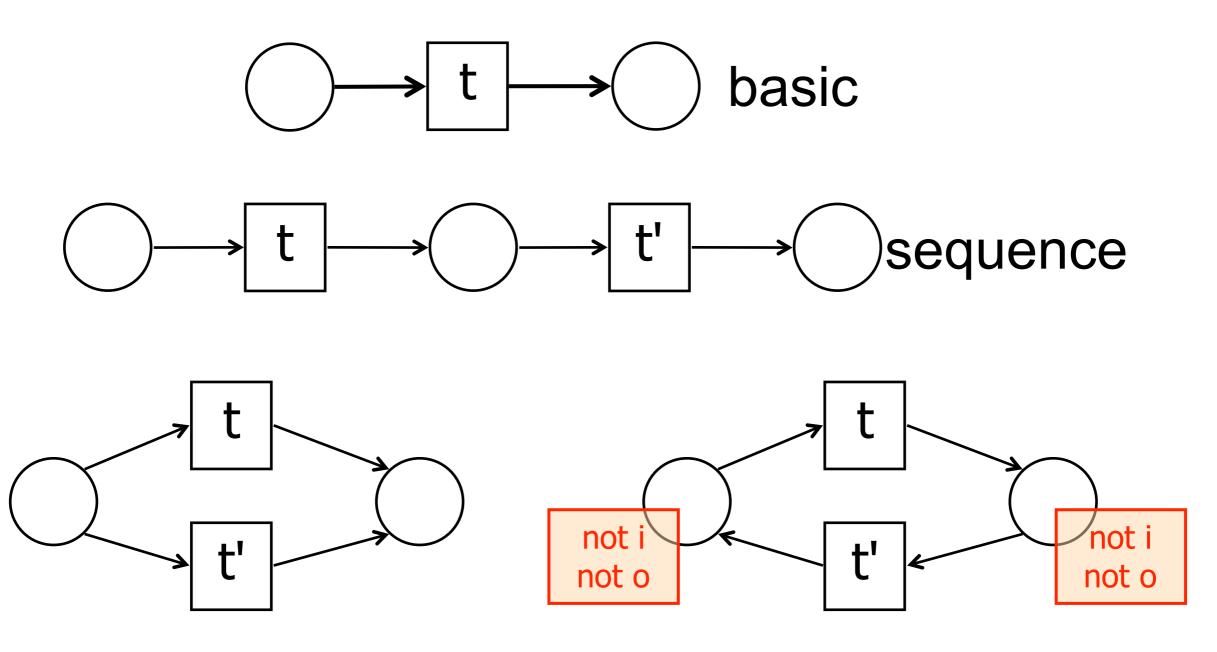
#### Proof sketch

#### Intuitively

a sound workflow net behaves as a transition: it takes one token from its input place and it produces one token to its output place (but not atomically)

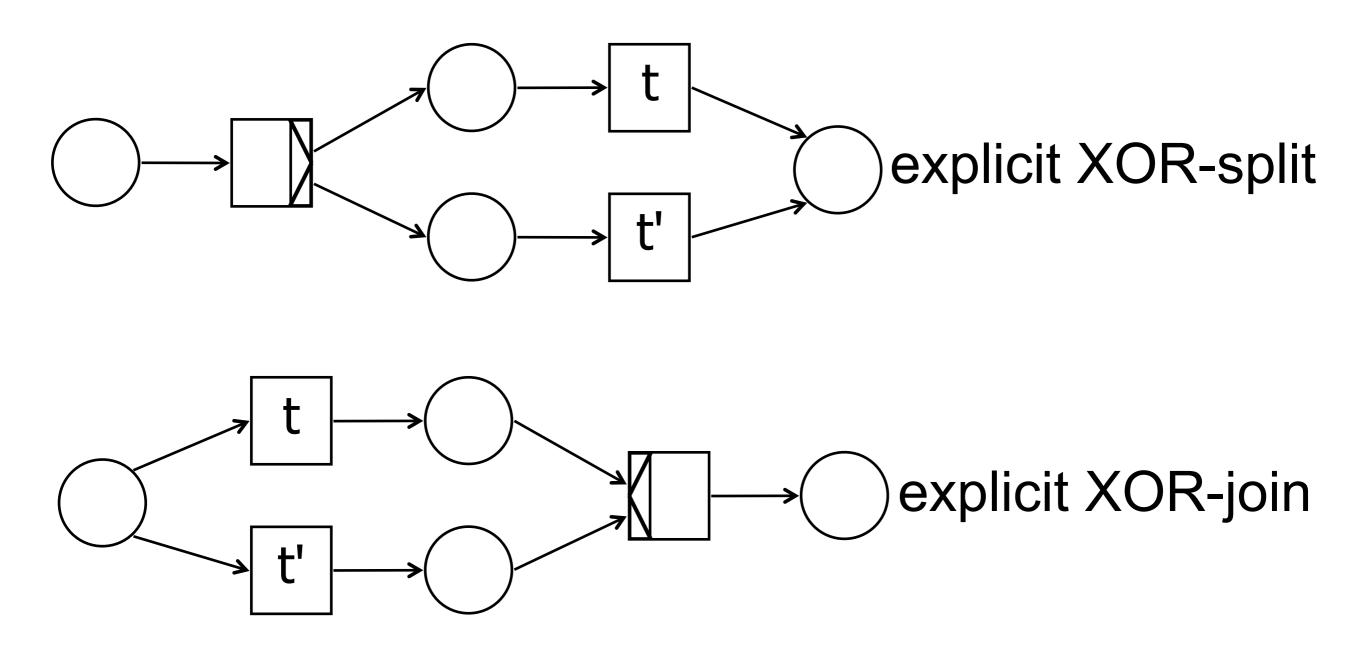
#### **Formally**

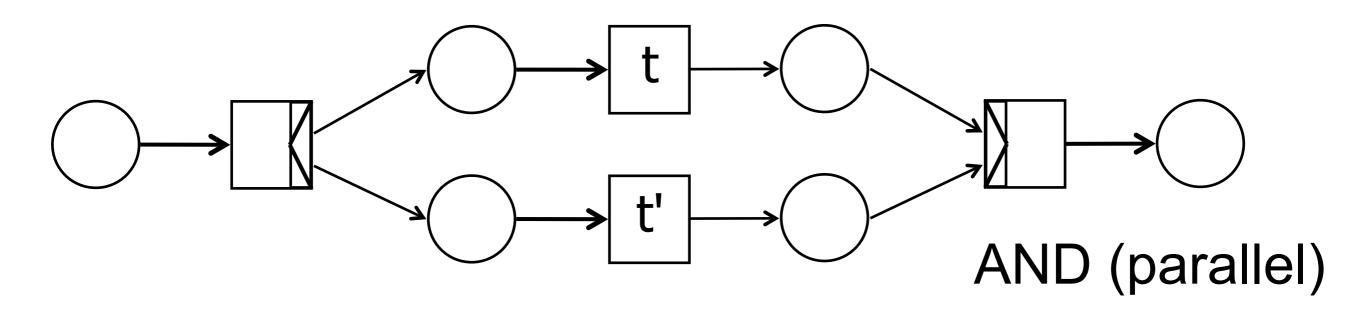
the crux of the proof is showing a bijective correspondence between markings of the composed net N[N'/t] and the pairs of markings in N and N'



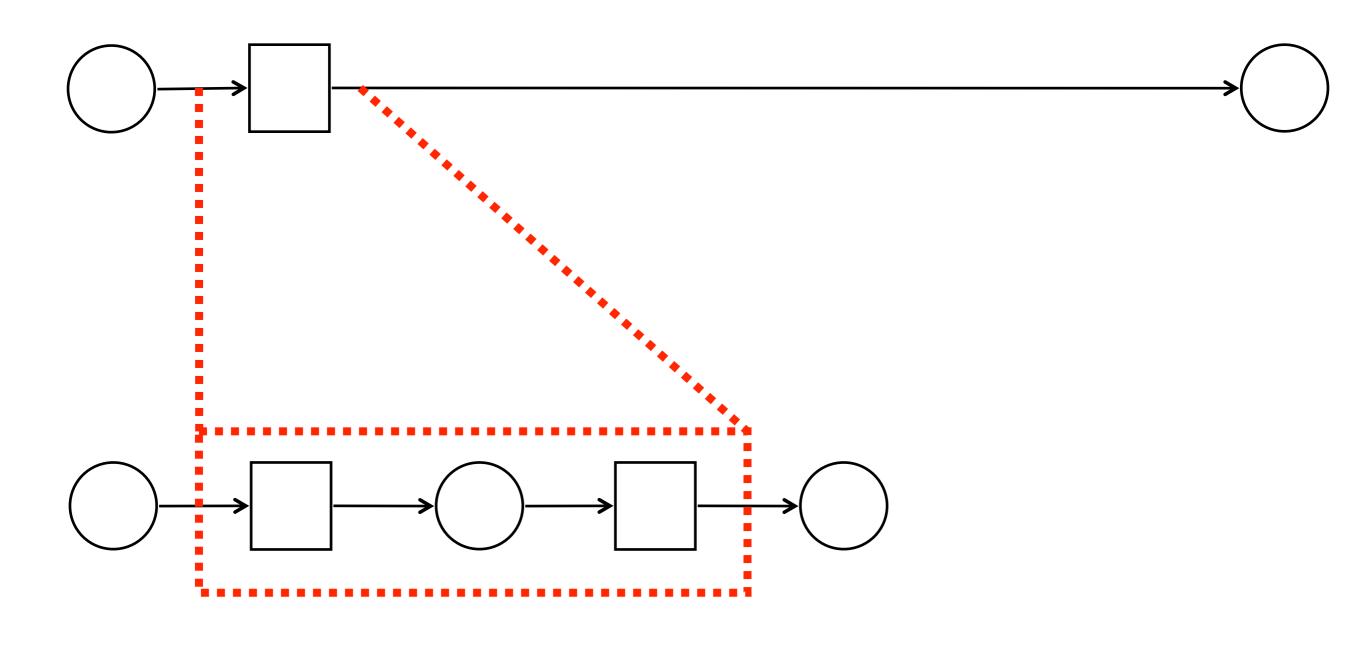
implicit XOR

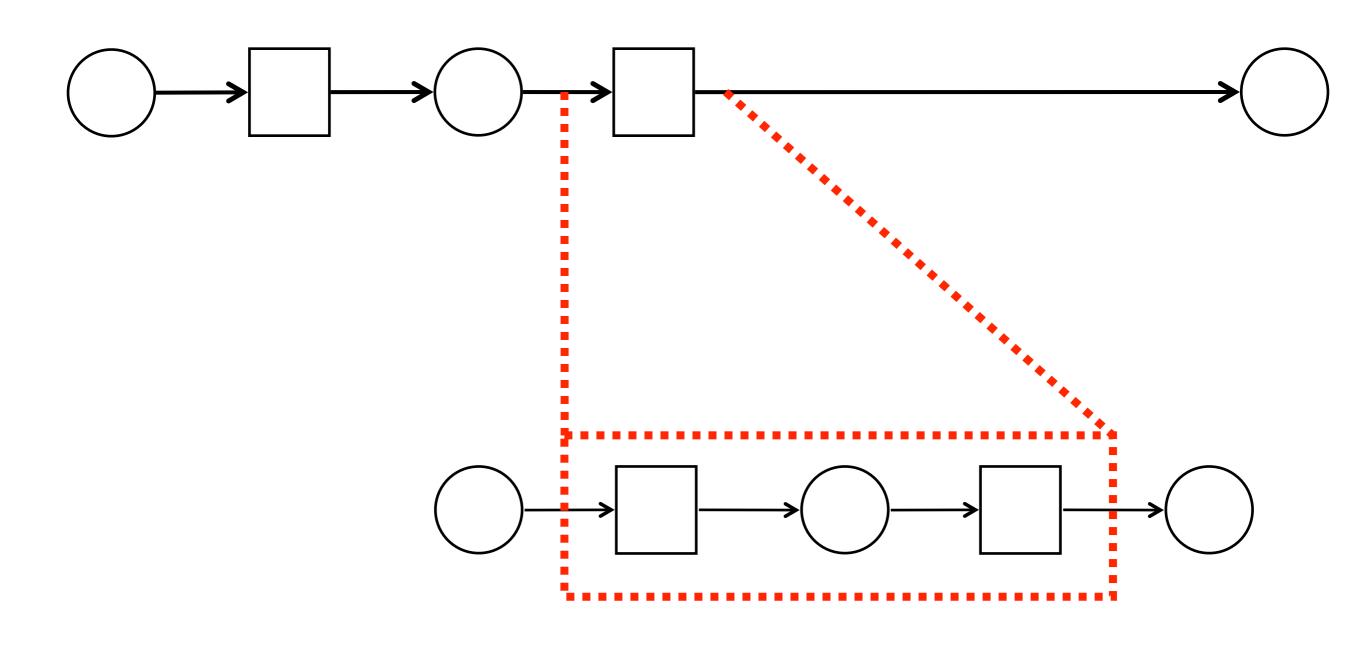
iteration

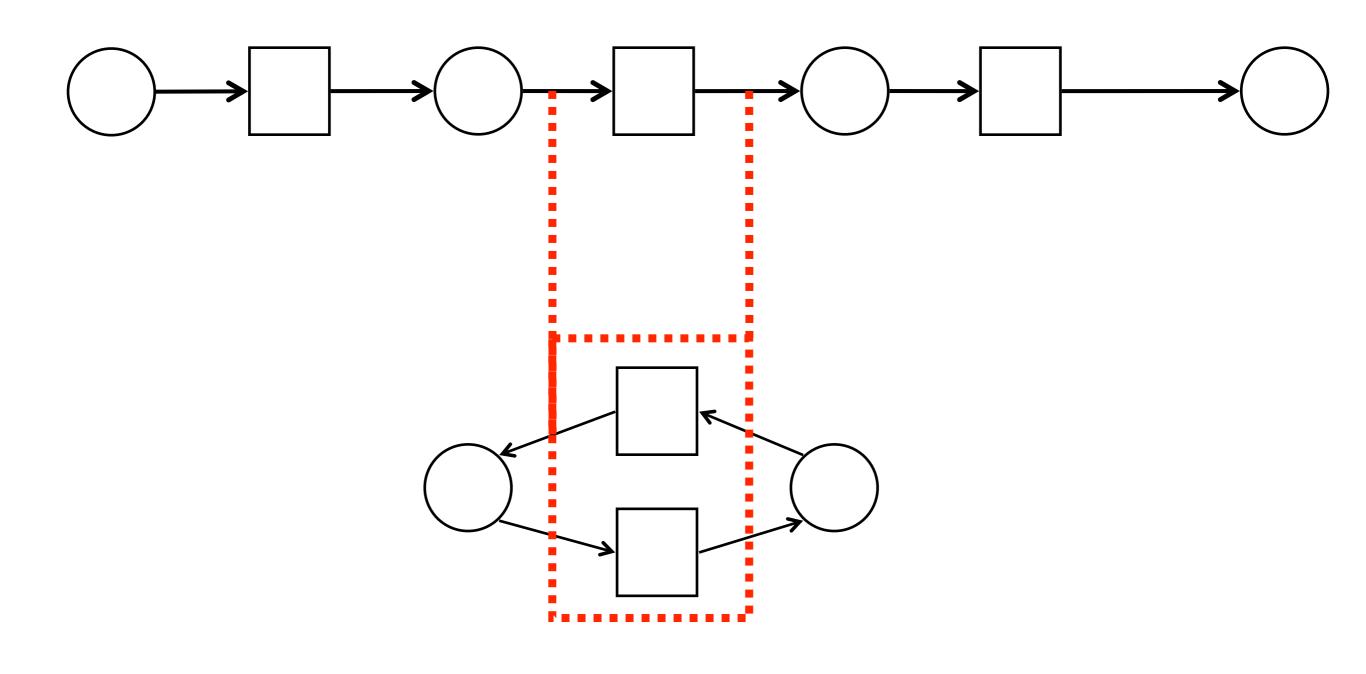


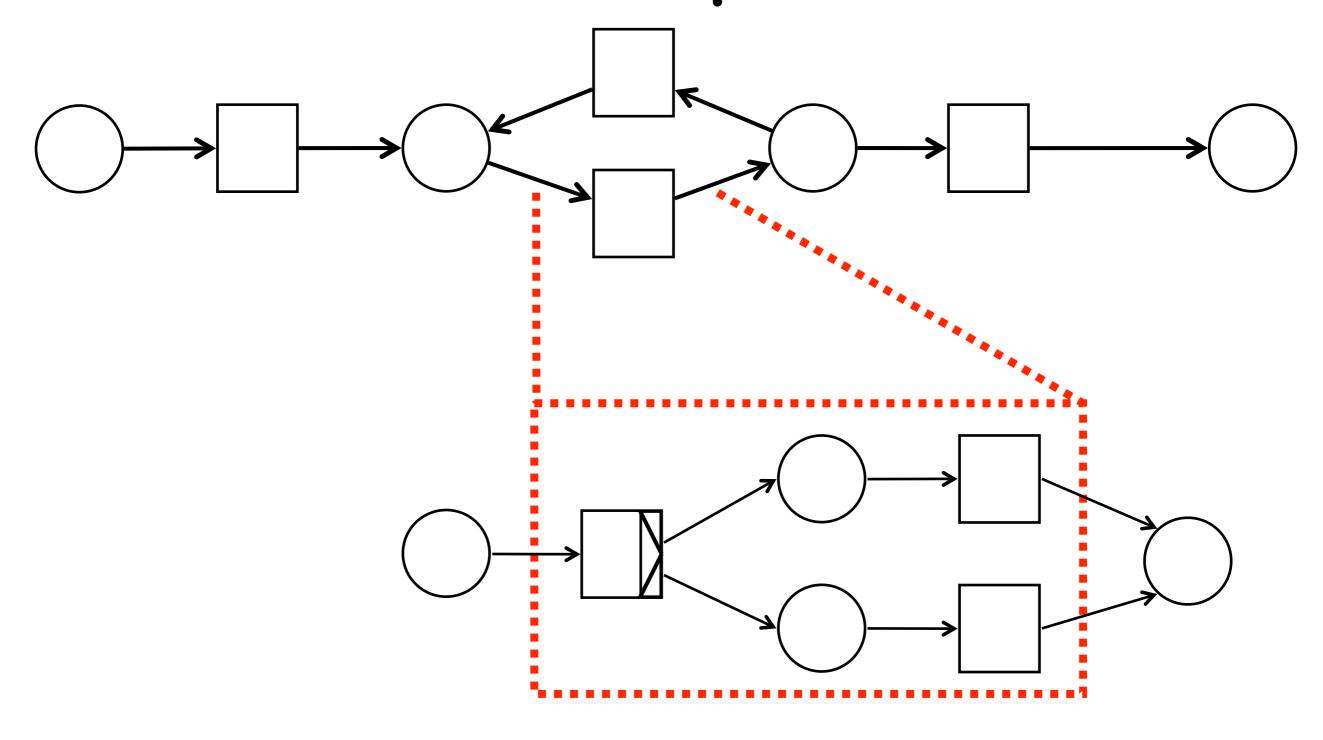


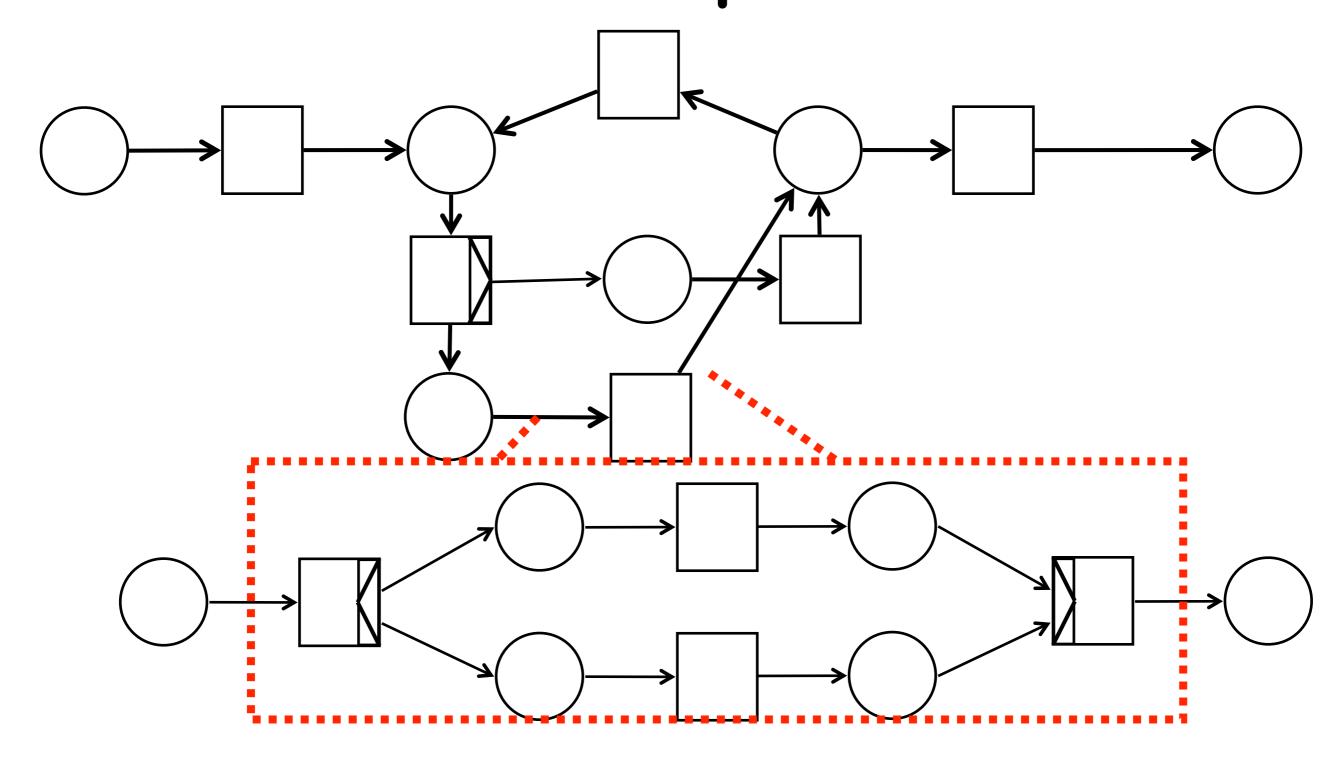
But you can define more blocks on your own

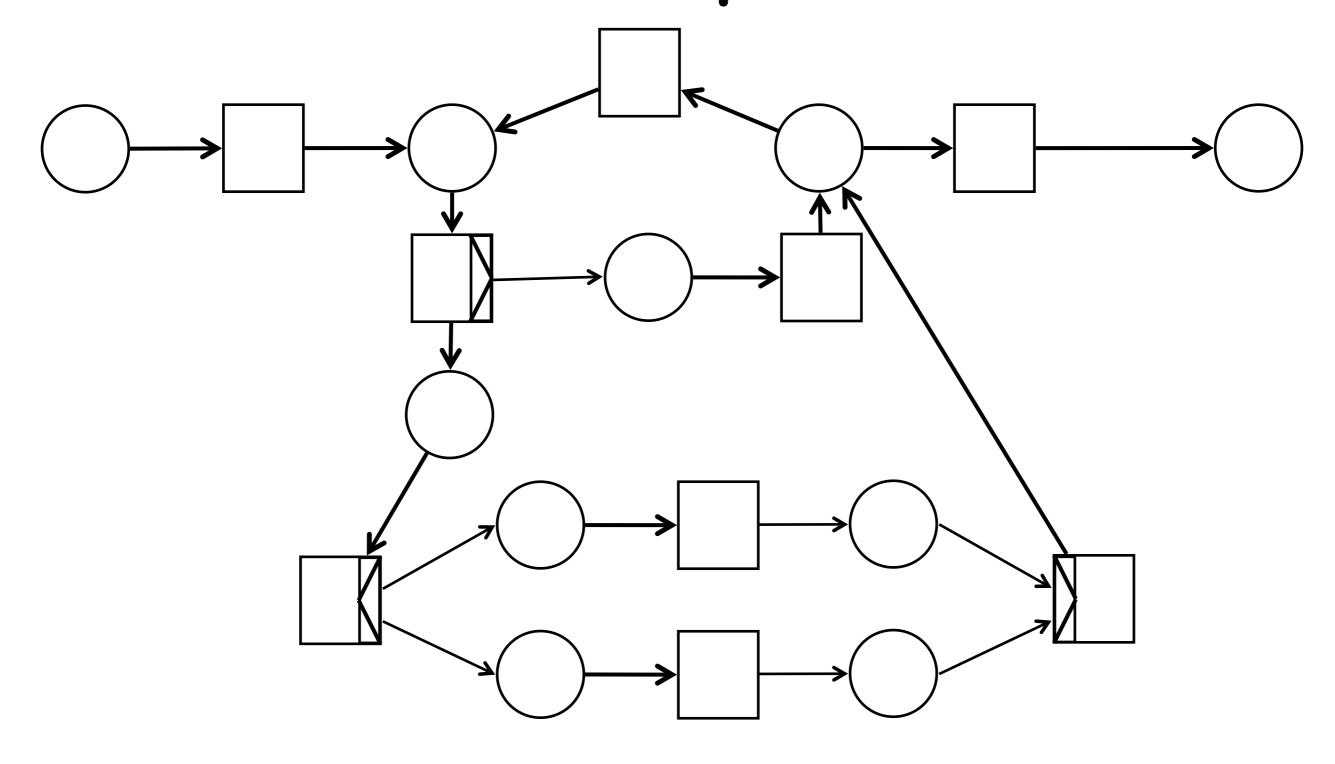






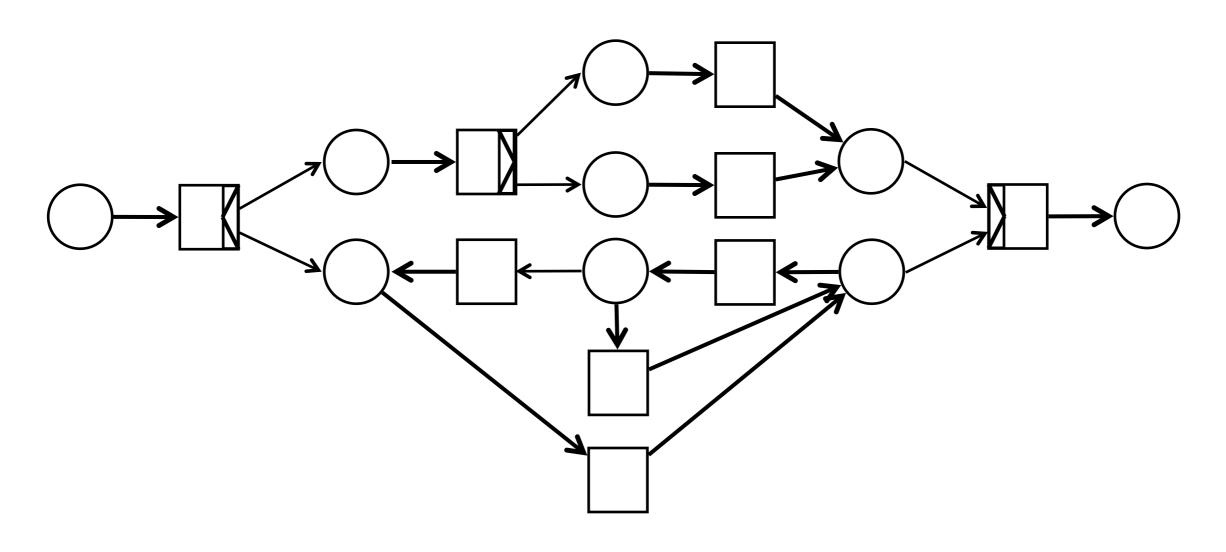






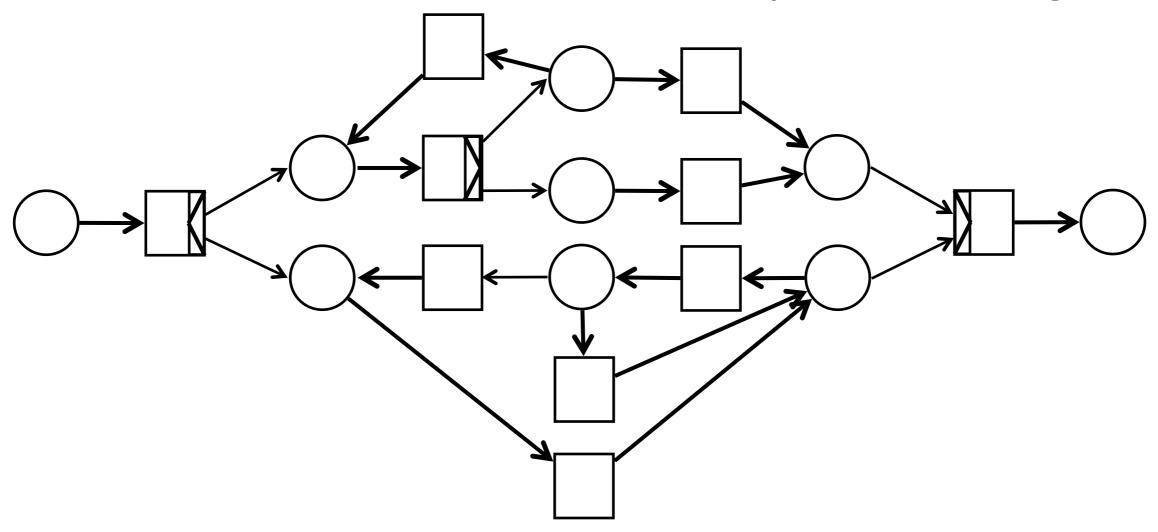
#### Exercise

Prove that the net below is a safe and sound workflow net



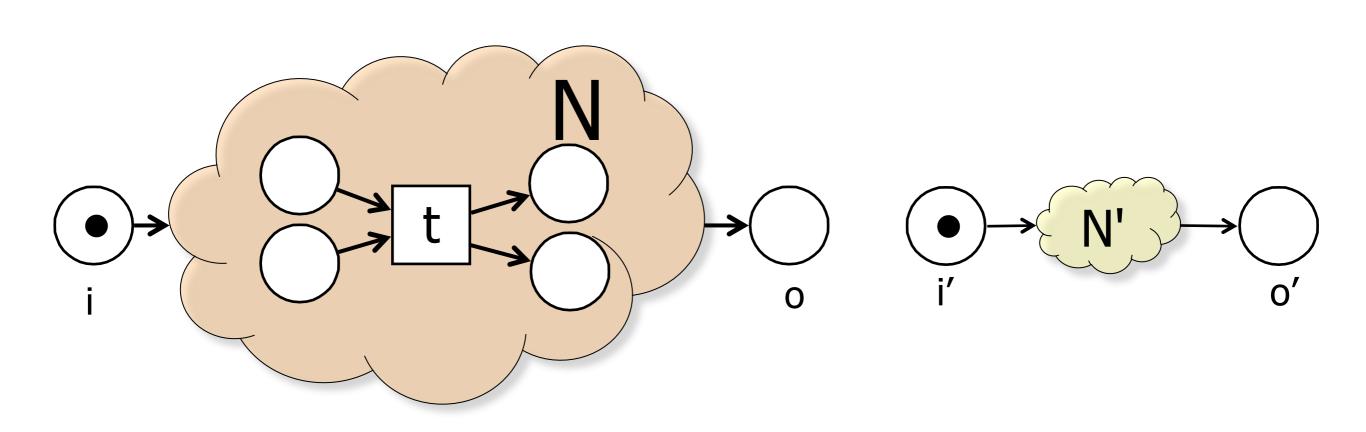
#### Exercise

Prove that the net below is a safe and sound workflow net (hint: "desugar" it)



#### Generalization

We would like to progressively refine transitions with multiple incoming and outgoing arcs



#### Two facts

**Lemma**: Let N be a sound WF net. If (i,t)∈F then the pre-set of t is {i}

(otherwise t would be a dead transition)

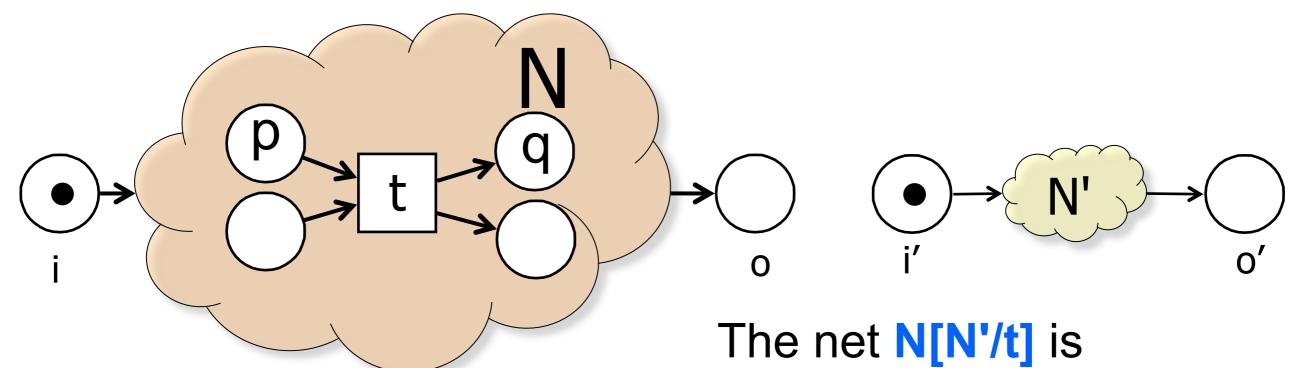
**Lemma**: Let N be a sound WF net. If (t,o)∈F then the post-set of t is {o}

(otherwise t would be dead or proper completion would not hold)

#### General replacement

Let 
$$T_{i'} = \{ u \mid \bullet u = \{i'\} \}$$
.  
Let  $T_{o'} = \{ v \mid v \bullet = \{o'\} \}$ .

If 
$$(p,t) \in F_N, u \in T_{i'}$$
 then  $(p,u) \in F_{N[N'/t]}$   
If  $(t,q) \in F_N, v \in T_{o'}$  then  $(v,q) \in F_{N[N'/t]}$ 

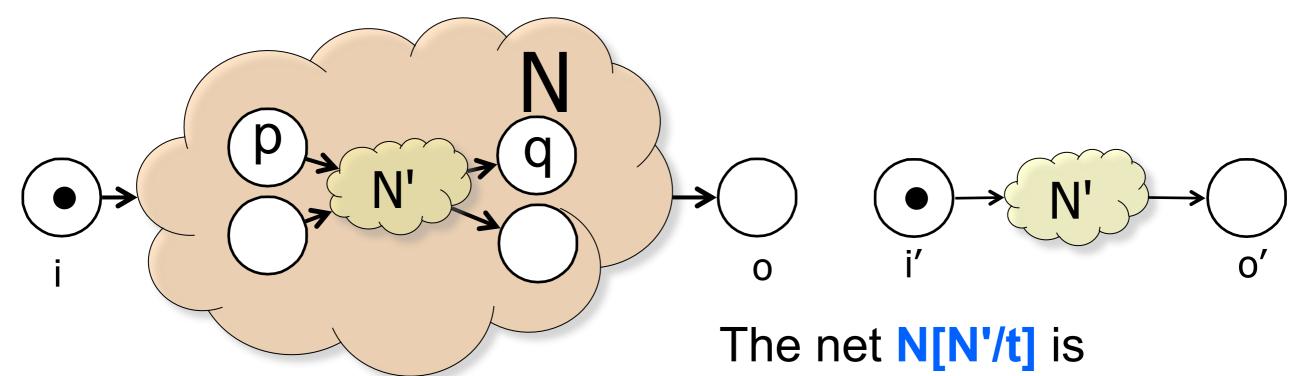


a sound and safe workflow net

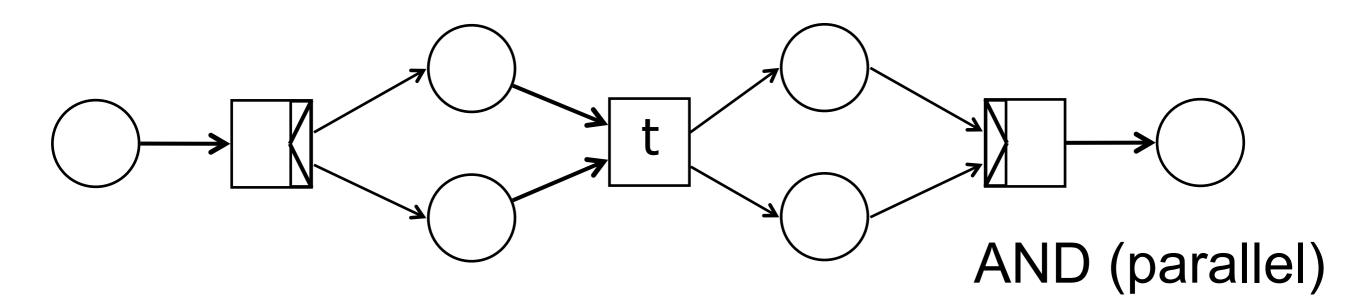
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a sound and safe workflow net



But you can define more blocks on your own

#### Exercise

Prove that the net below is a safe and sound workflow net

