

## EX 2.1

A = 1, 2, 4, 9, 10, 11, 15, 19, 20, 24  
 B = 3, 20

- ① 3 is compared with 1, 2, 9 and then Binary Search is performed on the block [4]
- ② 20 is compared with 4, 9, 11, 24 and then Binary Search is performed on the block [15, 19, 20]

## EX 2.2

Let us assume that  $\pi(x) = 2x \pmod{29}$

A = 1 2 4 9 10 11 15 19 20 24  
 $\pi(A)$  = 2 4 8 18 20 22 1 9 11 19

B = 3 20  $\rightarrow$   $\pi(B)$  = 6 11

$\frac{n}{L} = \frac{10}{2} = 5$ , assuming  $L = 2$

So  $U = [1, 29]$  is partitioned in 5 buckets  $\rightarrow$  size =  $\lceil \frac{29}{5} \rceil = 6$   
 $B_1 = [1, 5]$   $B_2 = [6, 11]$   $B_3 = [12, 17]$   $B_4 = [18, 23]$   $B_5 = [24, 29]$

Therefore all elements of B end up in  $B_2$ , which is the only bucket to look at in A  $\Rightarrow \{4, 19, 20\} \subseteq B_2$   
 $\pi \begin{matrix} 4 & 19 & 20 \\ \hline 8 & 9 & 11 \end{matrix}$

the algorithm then intersect  $\underbrace{(4, 19, 20)}_A \cap \underbrace{(3, 20)}_B = 20$

The intersection could have been done over  $\pi: (8, 9, 11) \cap (6, 11)$   
 and then compute  $\pi^{-1}(11) = 20$ .