

(E5)

ELIAS-FANO

ENCODE $S = 11, 14, 16, 19, 20, 21, 22$ WITH ELIAS-FANO AND SHOW HOW TO ANSWER

- ① ACCESS(5)
- ② NEXT SEQ(17)

HINT REDUCE THE UNIVERSE ~~TO 17~~ TO ~~17~~ $u=12$

SUBTRACT $S[1]$ TO OBTAIN $S' = (0, 3, 5, 8, 9, 10, 11)$

$$u=12 \quad m=7 \quad b=\lceil \log u \rceil = 4 \quad l=\lceil \log \frac{u}{m} \rceil = \lceil \log \frac{12}{7} \rceil = 1 \quad h=b-l=3$$

	$\overbrace{\quad\quad\quad}^{h=3 \text{ bits}}$	$\overbrace{\quad\quad\quad}^{l=1 \text{ bit}}$
0	000	0
3	001	1
5	010	1
8	100	0
9	100	1
10	101	0
11	101	1

$$L = 0110101$$

FOR M WE HAVE $2^h = 8$ BUCKETS

$$M = \underbrace{\frac{10}{0}}_{1} \underbrace{\frac{10}{1}}_{2} \underbrace{\frac{10}{2}}_{3} \underbrace{\frac{0}{3}}_{4} \underbrace{\frac{110}{4}}_{5} \underbrace{\frac{110}{5}}_{6} \underbrace{\frac{0}{6}}_{7} \underbrace{\frac{0}{7}}$$

① ACCESS(5) \rightarrow LOW PART $L[5] = 1$

$$\downarrow \text{HIGH PART} = \text{SELECT}_1(5)-5 = 9-5 = 4 = (100)_2$$

$\underbrace{\hspace{1cm}}_{h \text{ bits}}$

$$\text{RETURN } S[1] + (100)_2 = 11 + 8 = 20$$

② NEXT SEQ(17-5[1]) = NEXT SEQ(6) = NEXT SEQ(~~1000110~~
 $\overbrace{110}^{H(6)}$)

$$t = \text{SELECT}_0(3)+1 = 6+1 = 7$$

$$\begin{aligned} H[7] &= 0 \quad \text{so we return } S[1] + \text{ACCESS}(t-H(6)) \\ &= S[1] + \text{ACCESS}(7-3) \\ &= S[4] + \text{ACCESS}(4) \\ &= 11 + 8 = 19 \end{aligned}$$