

Algorithm Engineering – FINAL TERM

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Name and Surname:

#matricola:

Question #1 [score 4] Given the set of strings $S = \{abab, abca, abma, baa, bbb\}$, build a Patricia trie and show the steps for the lexicographic search of the strings $P1 = aaa$, and $P2 = abb$.

Question #2 [score 4+4]. Given the sequence of integers $S = (2, 3, 4, 5, 6, 10, 11)$, compress it via:

- (2,6)-dense code [showing the first 12 codewords of the integers from 0 to 11]
- Interpolative Coding [compressing the integers 5, 3, 10]

Question #3 [rank 4]. Given the tree of root labeled “a”, show its succinct encoding:

$T = \{ a \rightarrow b \text{ (right child)}; b \rightarrow c \text{ (left child)}; b \rightarrow e \text{ (right child)}; c \rightarrow d \text{ (right child)} \}$

Question #4 [score 4]. Decompress the 6th integer encoded via Elias-Fano in the two arrays:

$L = 01\ 11\ 00\ 01\ 01\ 00\ 11\ 11\ 00\ 11\ 00$ and

$H = 110\ 110\ 10\ 0\ 10\ 10\ 10\ 110\ 0\ 0\ 10\ 0\ 0\ 0\ 0\ 0$

(*hint*: derive first the number of keys, and then the length of the low and high part)

Question #5 [scores 4] Given the text $T = bababac$, apply the pipeline BWT+MTF+RLE0 (with Wheeler’s code) and finally apply Arithmetic coding on the first 3 numbers of the output of this pipeline.

Question #6 [score 4+4] Two theoretical questions:

- Prove the upper-bound in bits of Arithmetic coding, as a function of the Entropy and the input text length.
- Show and prove the space bound in bits of the **succinct** data structure built to support a Rank operation in constant time over a binary array $B[1,n]$.