



# (Indoor) Localization of Sensors

# Motivation

- Astonishing growth of wireless systems in last years
  - Wireless system used in large number of applications
- Wireless information access has become ubiquitous
- Gave rise to location-based services
  - Navigation systems, location-aware social networks, ...
- High demand of location information
  - both in outdoor and indoor environments
  - Outdoor mostly solved with GPS or Galileo
  - Indoor localization is still an open issue

# Types of location information

- *Physical* vs *Symbolic* location
  - Physical location: 2D or 3D coordinates referring to a map (e.g. latitude and longitude)
  - Symbolic location: natural language information (e.g. near the fridge, in the bedroom, etc.)
- *Absolute* vs *Relative* location
  - Absolute: uses a shared reference system
  - Relative: each object has its own frame of reference (e.g. proximity to an access point or position with respect to a destination)

# Types of location information

- It is always possible to convert absolute location in relative location
- A relative location can be converted into an absolute one if:
  - The absolute position of the reference points is known
  - Multiple relative readings are available
  - ...but there's a need for a triangulation algorithm

# Indoor localization systems

- Localization achieved by exchange of radio signals
- Three components :
  - Signal transmitter and receiver (HW)
  - Measuring unit (HW)
    - that uses received signals to make measurements of distances, angles etc. (also called ranging)
  - Localization algorithm (SW)
    - That uses the above information to determine the positioning of an object

# Indoor localization systems

- Two main topologies:
  - *Remote positioning*: the unit to be localized is mobile and acts as transmitter. The measuring units (*anchors*) are fixed. A fixed location manager (may be an anchor) executes the localization algorithm
  - *Self-positioning*: the unit to be localized is mobile, makes the measurements and runs the localization algorithm
    - This unit receives the signal from fixed anchors (whose position is known) that are only transmitters
- Two derived topologies:
  - *Indirect remote positioning*: similar to self-positioning, but the mobile sends its location to a remote location manager
  - *Indirect self-positioning*: similar to remote positioning, but the location manager sends the position to the mobile

# Measuring principles and positioning algorithm

## Triangulation

### Lateralation (*range-based*)

- Time of Arrival (ToA)
- Time Difference of Arrival (TDoA)
- Received Signal Strength (RSS)
- Roundtrip Time of Flight (RTofF)
- Received Signal Phase (RSP)

### Angulation

- Angle of Arrival (AoA)

## Scene analysis (fingerprinting)

Probabilistic methods

K-Nearest Neighbors (kNN)

Neural Networks

Radio Tomography

## Proximity

Radio Frequency Identifier (RFID)

Passive Infrared (PIR)

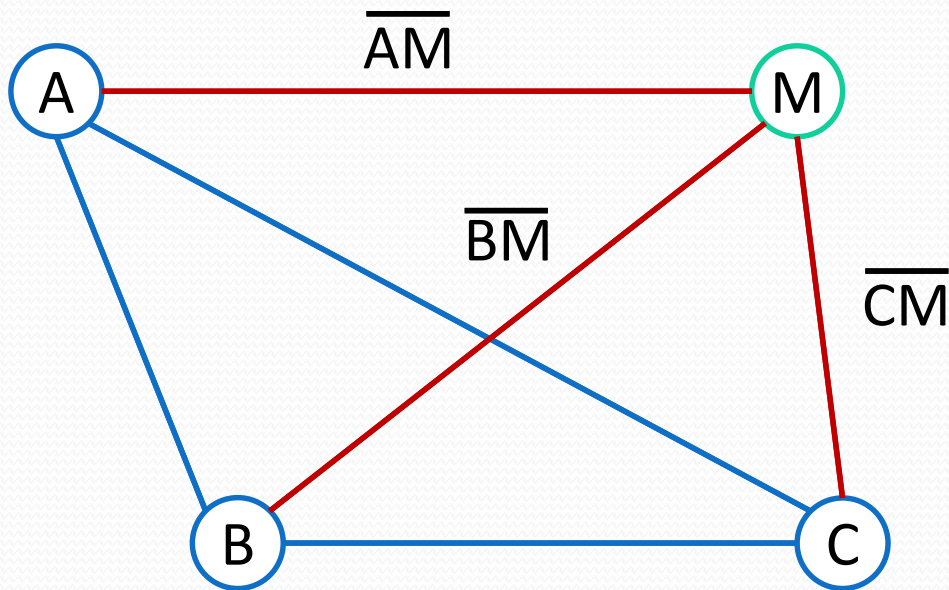
WSN Multihop proximity

# Triangulation

- Uses geometric properties of triangles to estimate target location
- Two approaches:
  - *Lateration*: estimates position of an object based on its distance from reference points (also called *range-based localization*)
  - *Angulation*: estimates position based on the angles between the lines connecting the object and the reference points



# Triangulation – Lateration

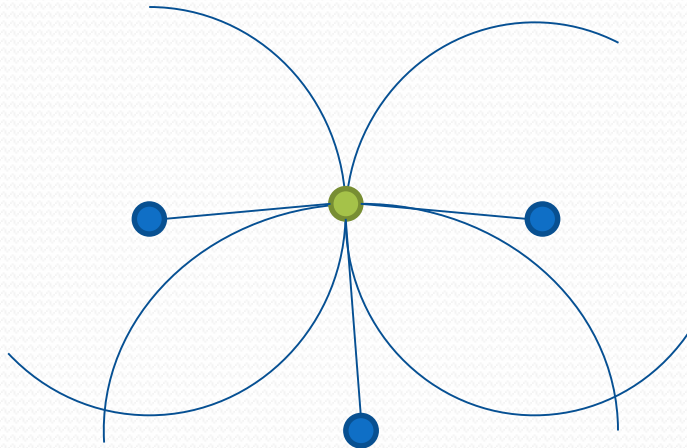


# Time of Arrival (ToA)

- The distance between a measuring unit and a mobile target is directly proportional to propagation time
- How it works
  - The mobile target emits a radio signal at time  $t$
  - The measuring unit receives the radio signal at time  $t'$
  - The measuring unit estimates the distance as  $(t'-t)/p$ 
    - Where  $p$  is the propagation speed of the signal
- Issues:
  - Requires tight synchronization of transmitter and receiver
  - The signal must encode the transmission time ( $t$ )

# Time of Arrival (ToA)

- To compute the position of the mobile target in 2D are required at least 3 measurements from 3 different anchors
- The position can be computed with different methods:
  - Intersection of circles centered in the anchors



# Time of Arrival (ToA)

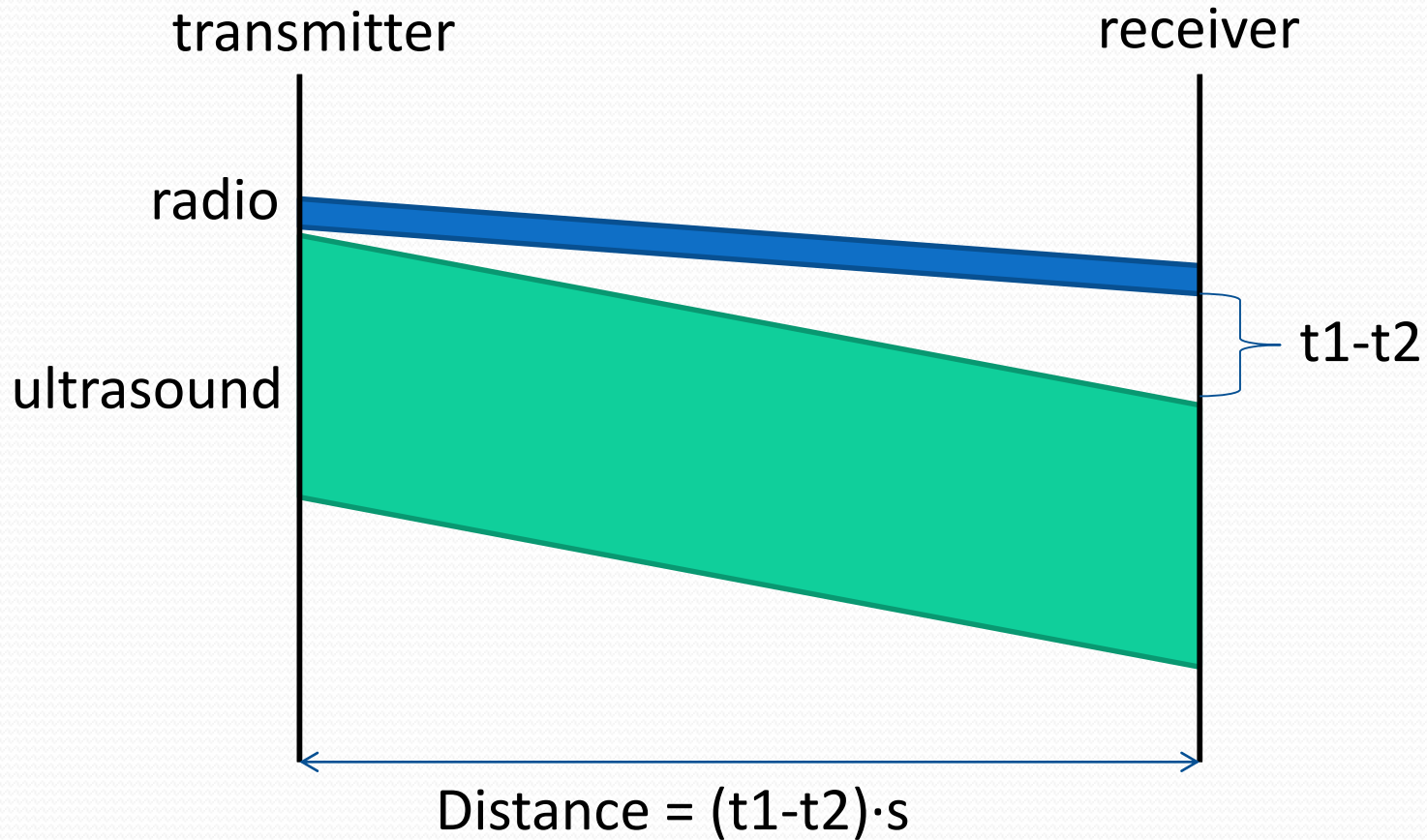
- Other positioning method:
  - Solving a non-linear optimization problem (least squares)
    - the unknown are  $t$ , the coordinates  $(x,y)$  of the mobile target
    - The coordinates of anchors  $(x_1,y_1), \dots, (x_n,y_n)$  are known
    - The time of arrival of the signal at the anchors  $t_1, \dots, t_n$  are known
    - $c$  is the light speed

$$\min \sum_{i=1}^n \left| c \cdot (t_i - t) - \sqrt{(x_i - x)^2 + (y_i - y)^2} \right|$$

# Time of Arrival (ToA)

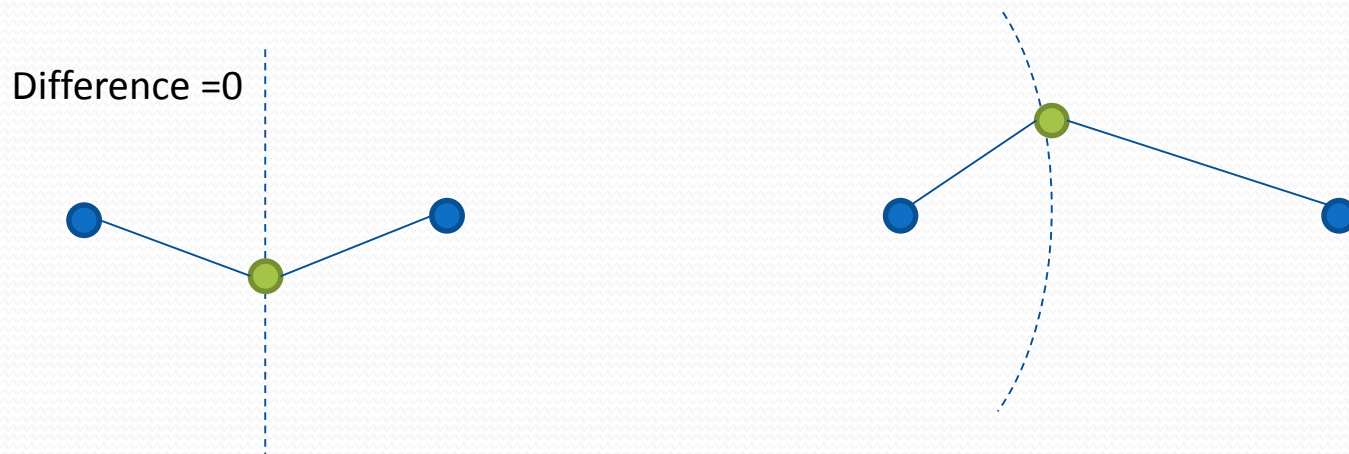
- In some applications, the ToA is implemented by using signals of different nature, e.g. radio and acoustic:
  - The radio signal is used to synchronize the measuring units
- The difference in time between the arrival of the two signals is (almost) proportional to the distance
  - Because the radio signal is order of magnitudes faster than the acoustic signal
- Some systems use ultrasound
  - Cricket motes, Active Bat, etc.

# Time of Arrival (ToA)



# Time Difference of Arrival (TDoA)

- Uses the difference between the arrival times at the measuring units (rather than the absolute time)
- For each TDOA measurement, the transmitter must lie in a hyperboloid with a constant range difference between any two measuring units
- For example, in 2D:



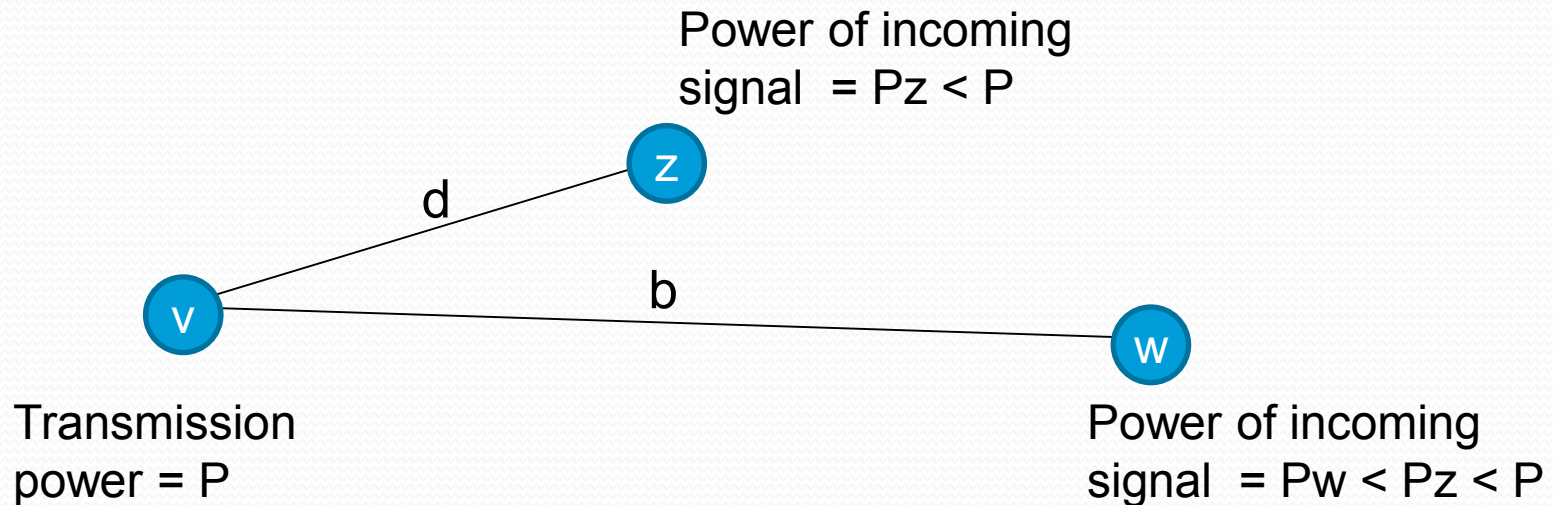
# TOA and TDoA

- Both system work well if transmitter and measuring units are in Line Of Sight (LOS)
- If not, the signal is affected by multipath that affects time of arrival and angle



# Received Signal Strength (RSS)

- Radio signal attenuates with distance
  - Power of the signal decays with an exponential rule
- There is a relationship between signal attenuation and distance



# Received Signal Strength (RSS)

- Friis equation: establish a relationship between transmission power and distance between transmitter and receiver

$$P_R = P_T \frac{G_T G_R \lambda^2}{(4\pi)^2 d^n}$$

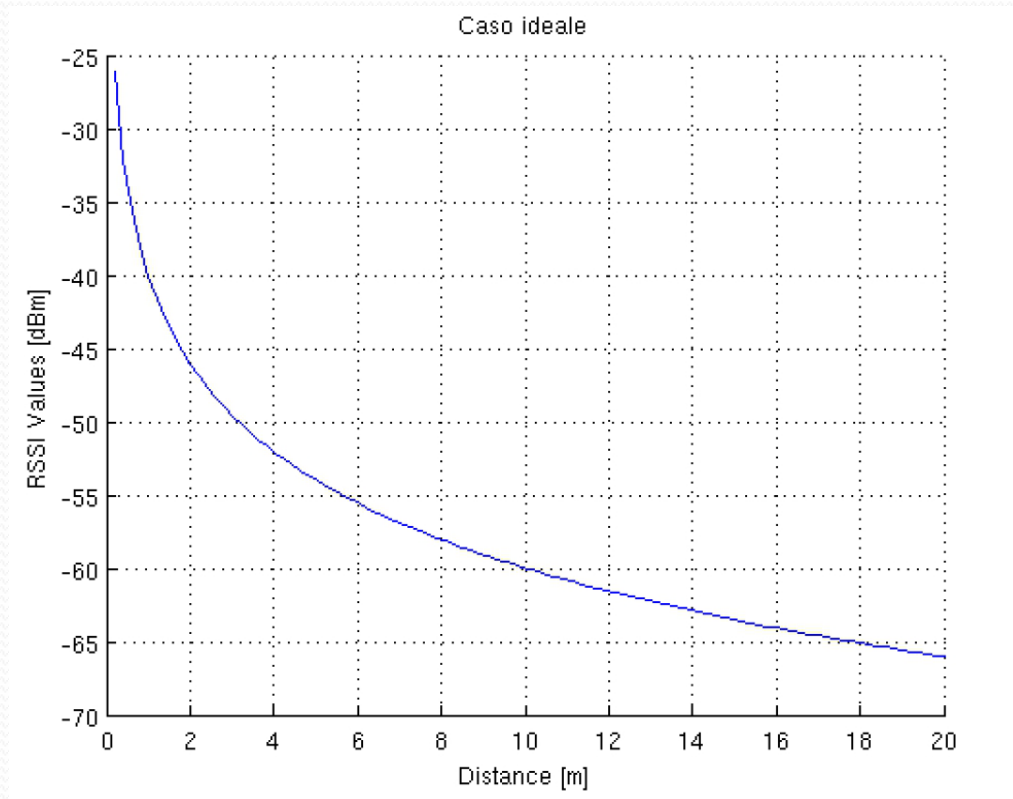
- $P_T$  e  $P_R$ : signal power at transmitter and receiver (in Watt)
- $G_T$  e  $G_R$ : antennas gain (at transmitter and receiver)
- $\lambda$ : wave length
- $d$ : distance between the transmitter and receiver
- $n$ : path loss (usually between 2 and 4)

# Received Signal Strength (RSS)

- Signal attenuation depends on the environment.
- There are many models that relate distance with transmission and received power.
- Converting Watt in dBm:
  - $P[\text{dBm}] = 10 \log_{10} (10^3 P[\text{W}])$
- and combining with Friis equation we obtain:
  - $\text{RSS} = - (10 n \log_{10} d - A)$
- where
  - $A$  is attenuation of the signal at a reference distance (typically 1 m)
  - $n$  is the path loss (typically in the range [2,4])

# Received Signal Strength (RSS)

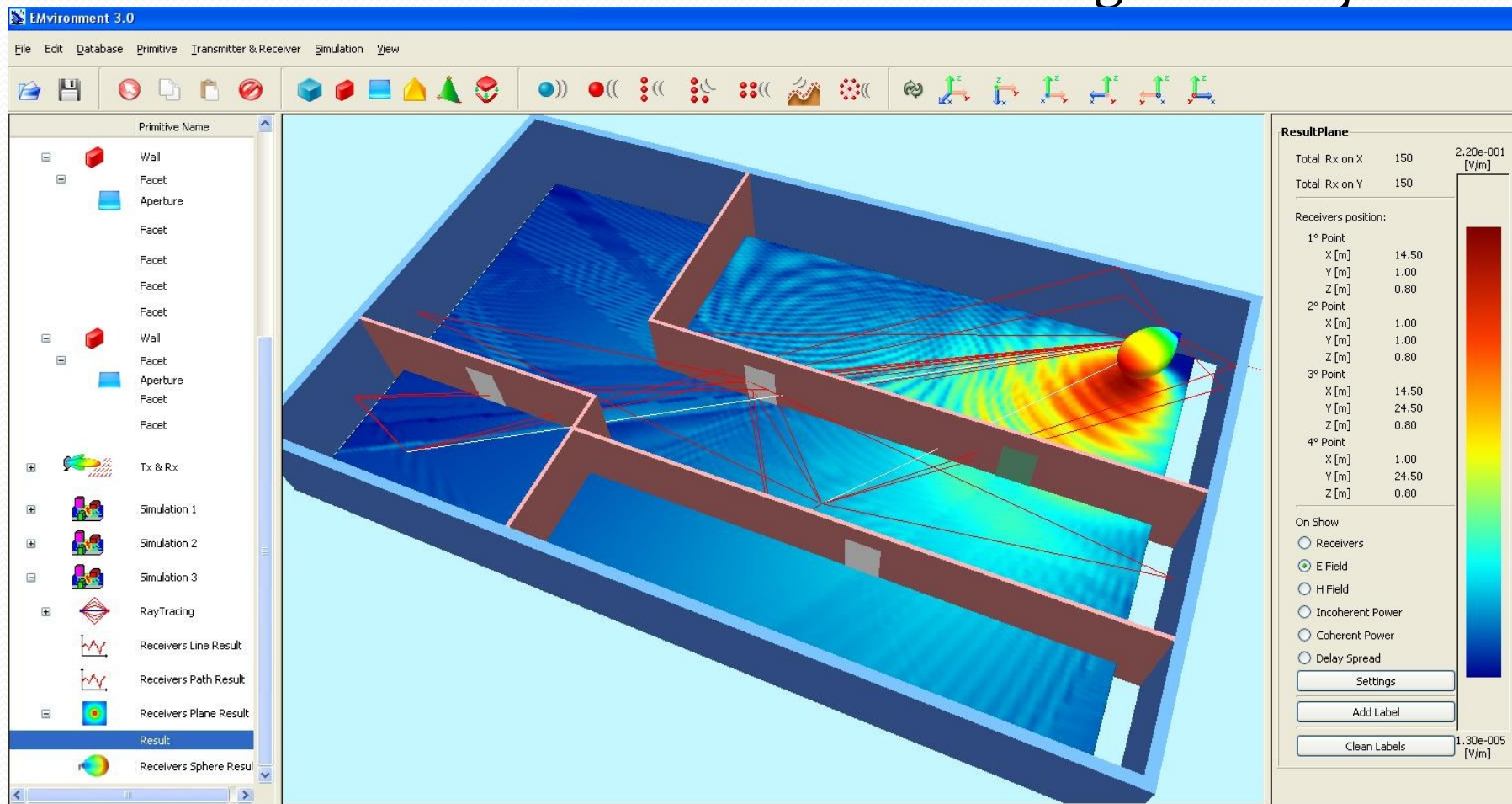
- Power vs distance



Triangulation - lateration

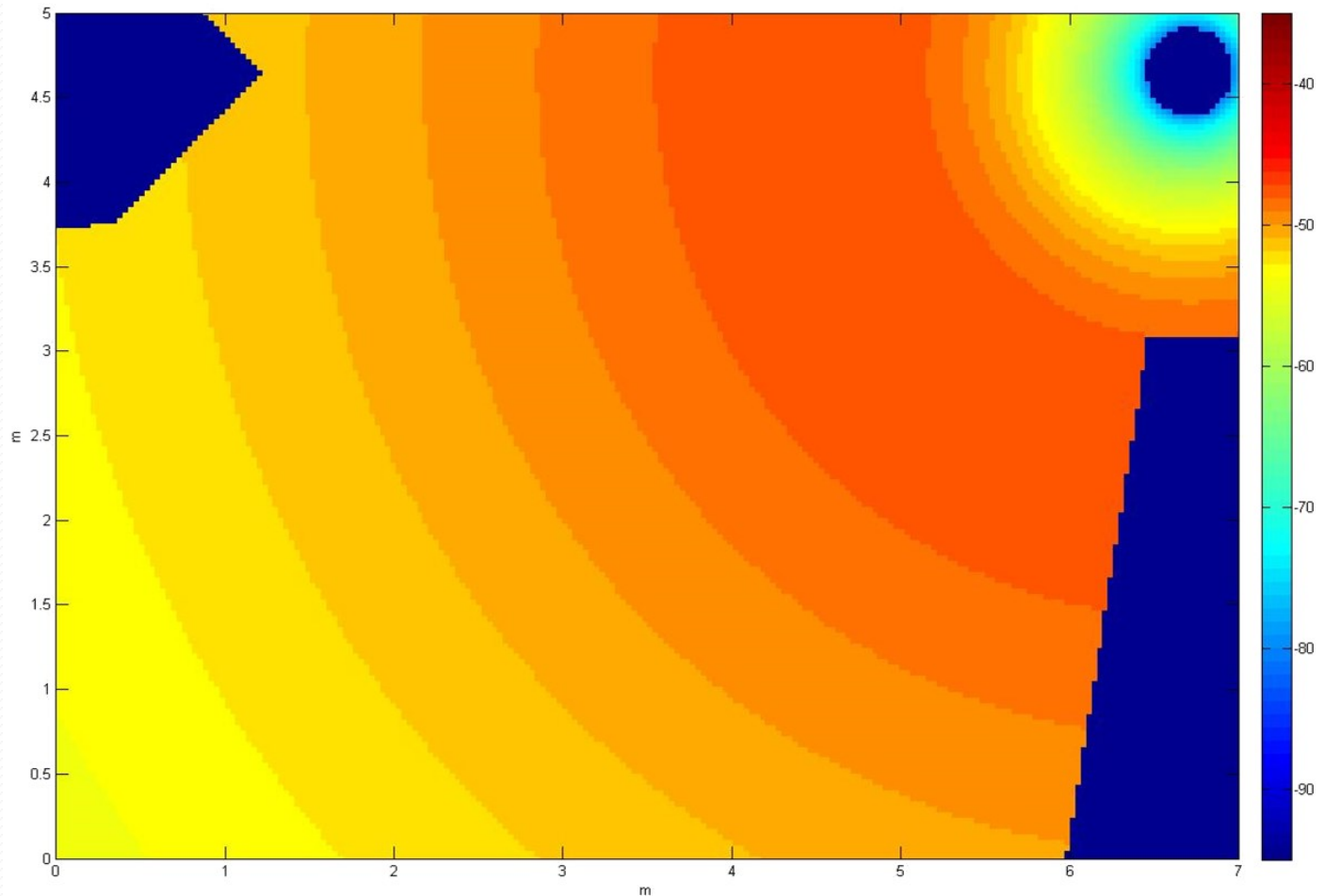
# Received Signal Strength (RSS)

- In indoor environments the RSS worsens significantly



# Received Signal Strength (RSS)

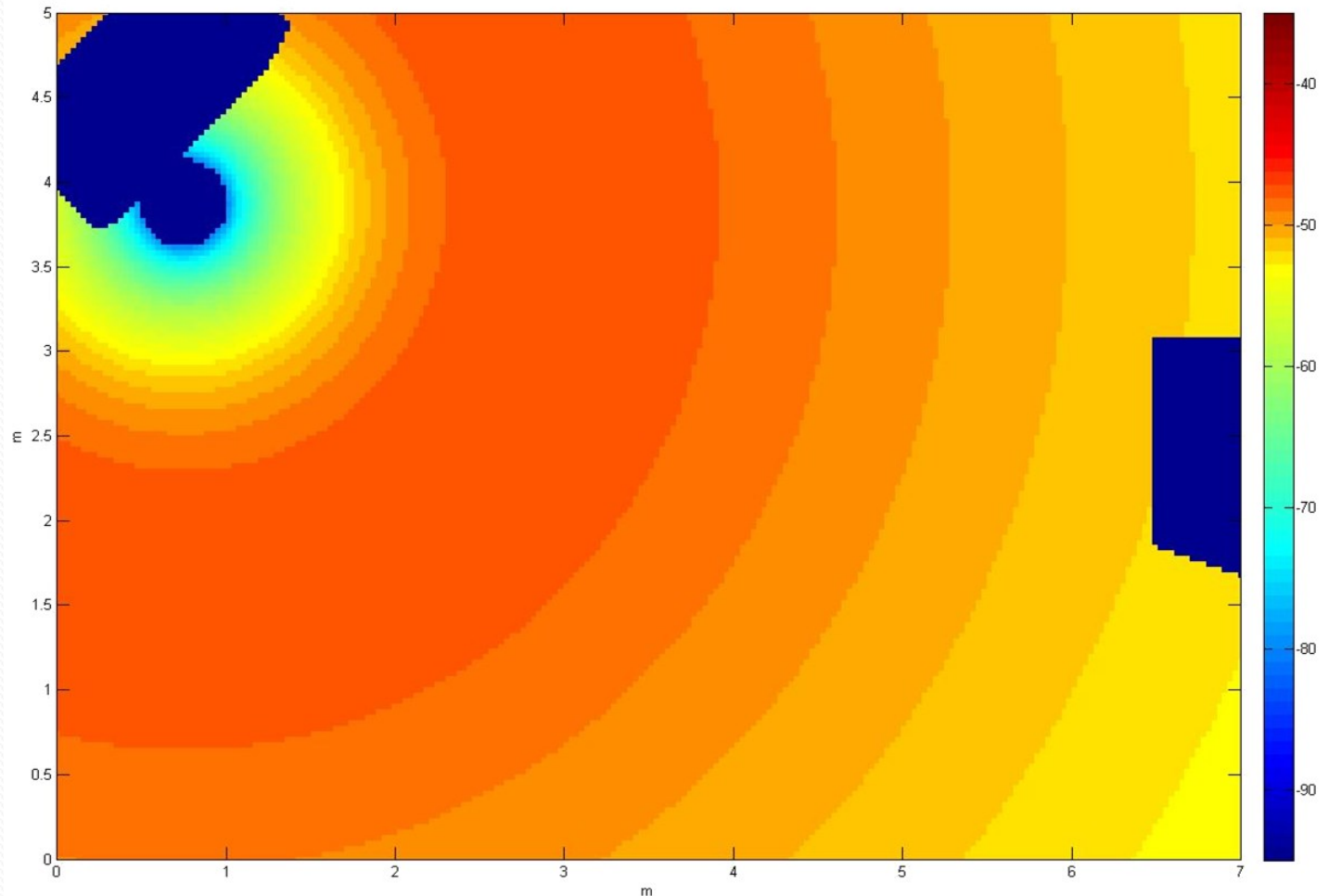
- Ideal situation



courtesy of  
F.Potortì,  
A.Corucci,  
P.Nepa,  
P.Barsocchi,  
A.Buffi

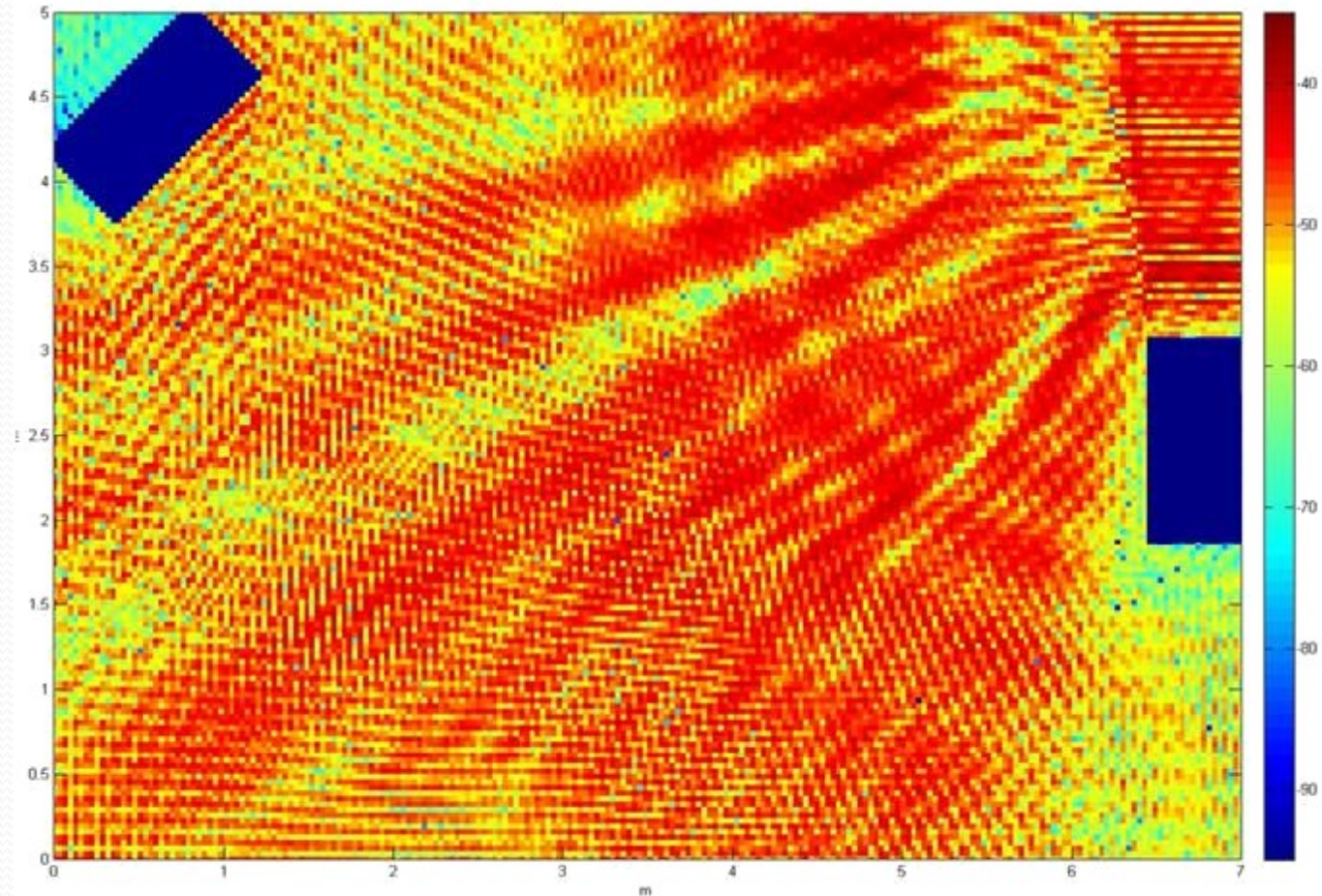
# Received Signal Strength (RSS)

- Ideal situation:



# Received Signal Strength (RSS)

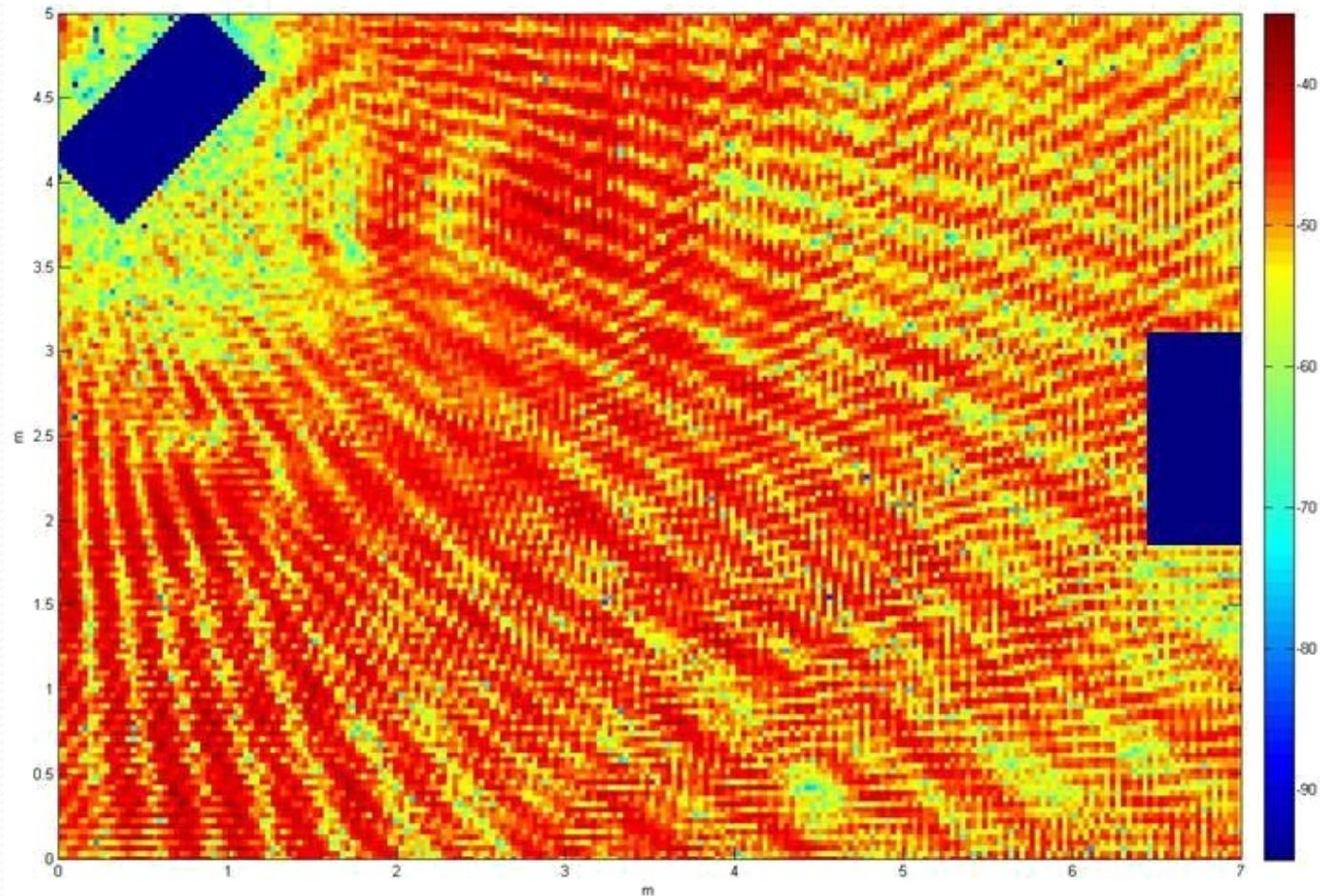
- Realistic situation
  - 3<sup>o</sup> order reflections





# Received Signal Strength (RSS)

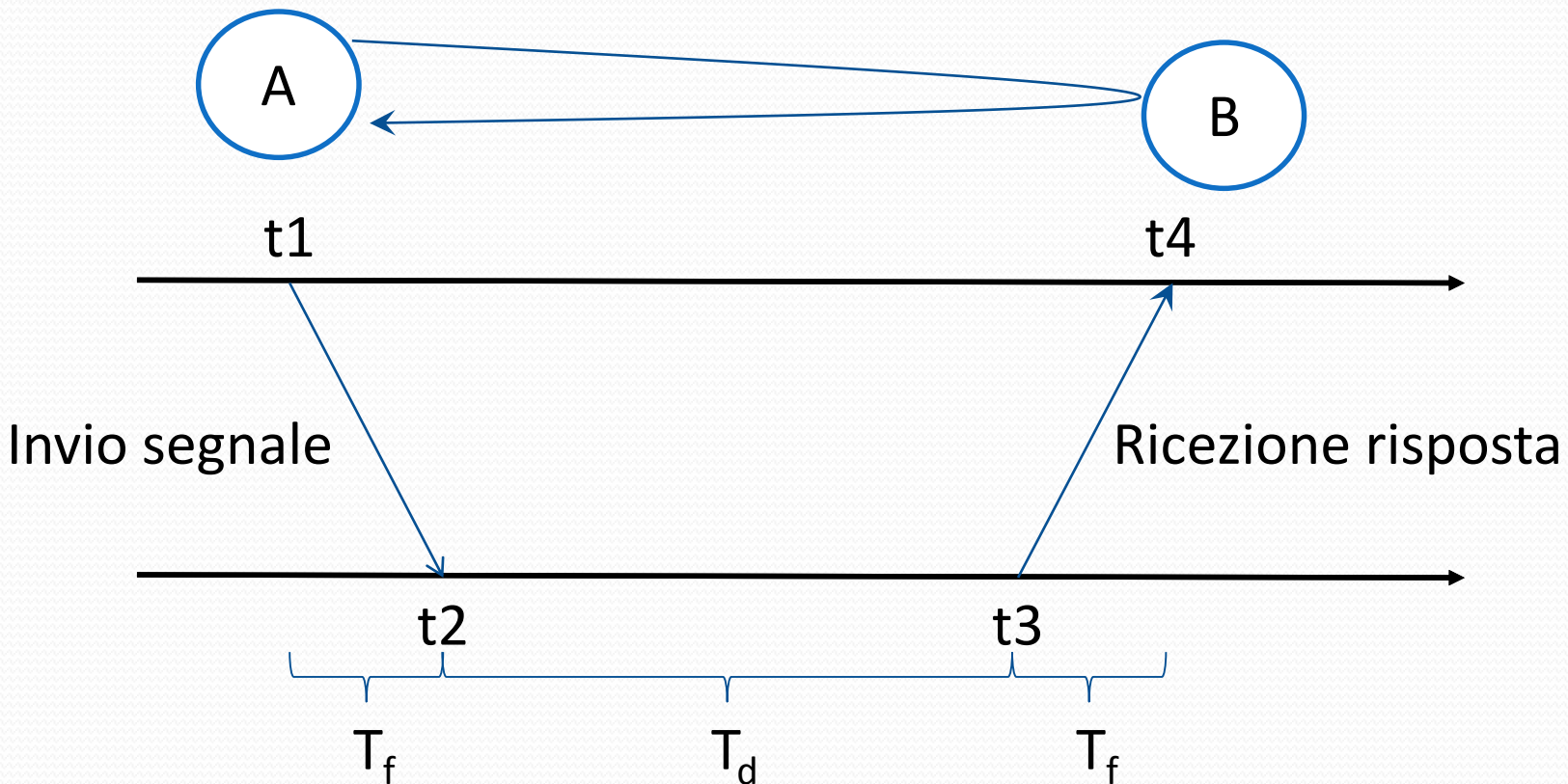
- Realistic situation
  - 3<sup>o</sup> order reflections



# Roundtrip Time of Flight (RToF)

- The transmitter and the measuring unit are the same
- The device to be localized is only a transponder
  - receives the signal and sends it back
- The measuring unit measures the difference between the time of transmission  $t_1$  and the time of reception  $t_2$ 
  - distance =  $c \cdot (t_1 - t_2) / 2$
- Reduces the need of synchronization with respect to ToA
  - At small ranges, the processing time of the transponder and measuring unit are not negligible and must be estimated accurately

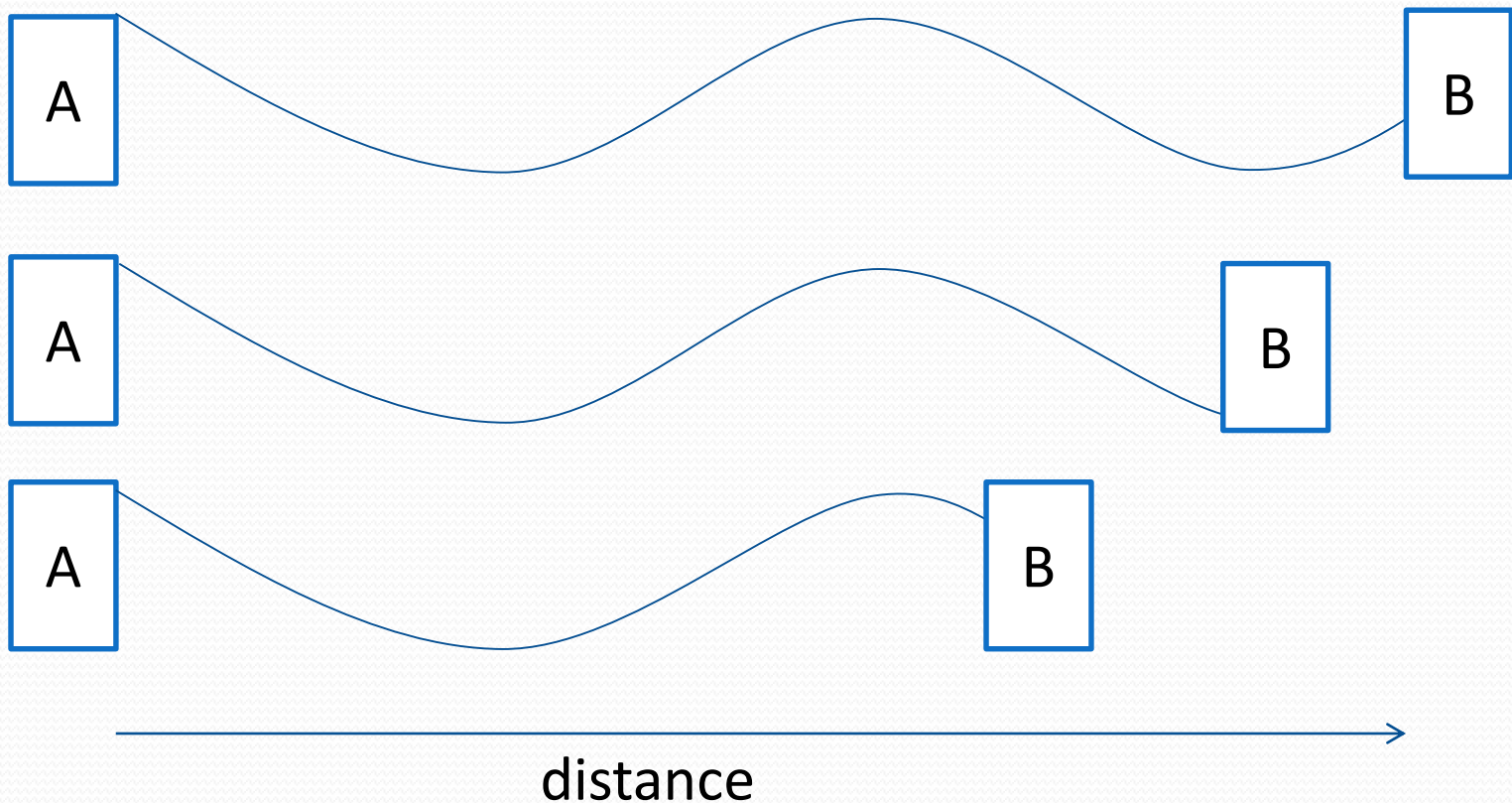
# Roundtrip Time of Flight (RToF)



$$d = c \frac{1}{2} \left( (t_2 - t_1) + (t_4 - t_3) \right)$$

# Received Signal Phase (RSP)

- Assumes the transmitter sends a pure sinusoidal signal

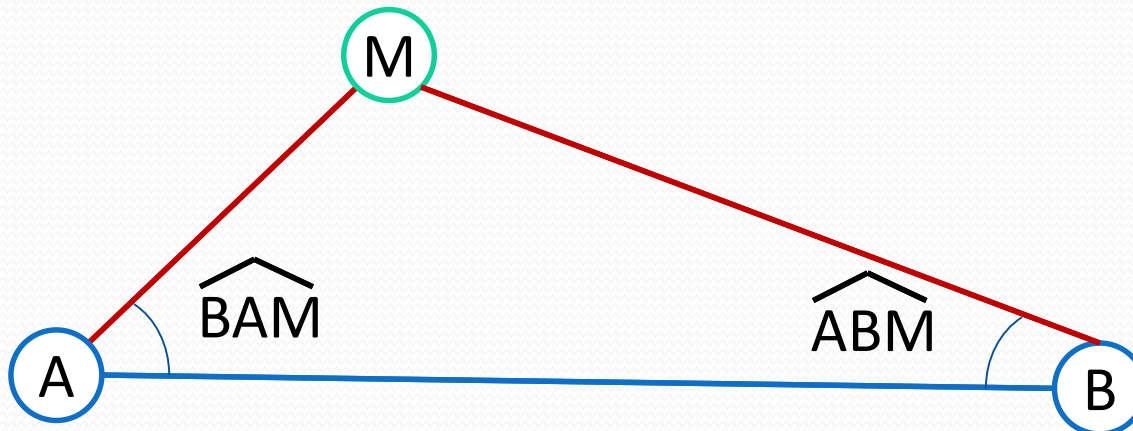


# Received Signal Phase (RSP)

- Based on the received phase of the signal, the measurement unit estimates the distance
  - This holds within a wave length
- Once distance is known it uses the same triangulation algorithm as ToA
- For distances larger than a wave-length it does not work
- Requires LOS between transmitter and receiver

# Angle of Arrival (AoA)

- Target location obtained by the intersection of several pairs of angle direction lines
- 2D: Requires at least two reference points and the respective angle measurements
- 3D: Requires at least three reference points and the respective angle measurements

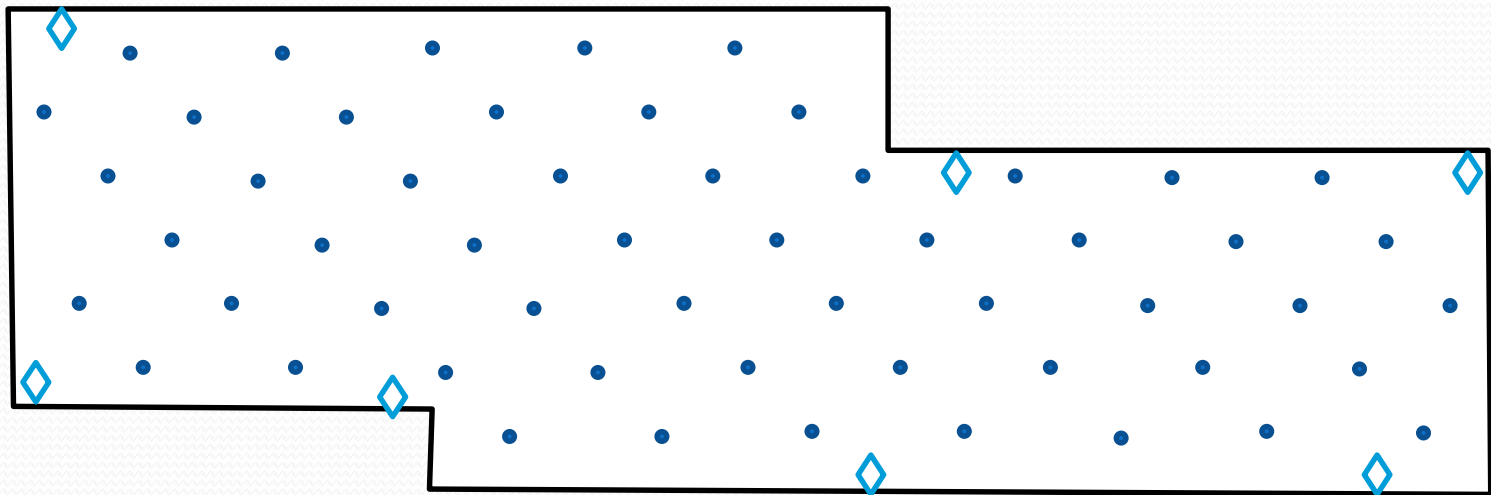


# Angle of Arrival (AoA)

- Requires directional antennas
  - Usually not available in sensors
  - More expensive and larger
  - Often implemented as arrays of antennas
- Angle measurement should be very accurate
  - Again multipath and reflection affect the measurements

# Scene analysis

- Exploits maps of RSSs measurements with respect to a set of anchors
- Measurements usually in a grid of points
  - For each point  $i$  in the map, is defined a tuple of RSS measurements  $R_i$





# Scene analysis

- At runtime, the position of a target is determined by measuring the RSS of the target with respect to the anchors
  - This produces a new tuple  $R$  of RSSs
  - $R$  is compared against all the tuples  $R_i$
  - The position of the mobile target is approximated with the position of the point (or points) whose tuple is most similar to  $R$
- To find the suitable points can be used either probabilistic methods, neural networks or KNN

# kNN

- Let  $R = \langle r_1, \dots, r_n \rangle$ ;  $R_i = \langle r_{i,1}, \dots, r_{i,n} \rangle$ ;
- Find  $k$  points for which the least mean square:

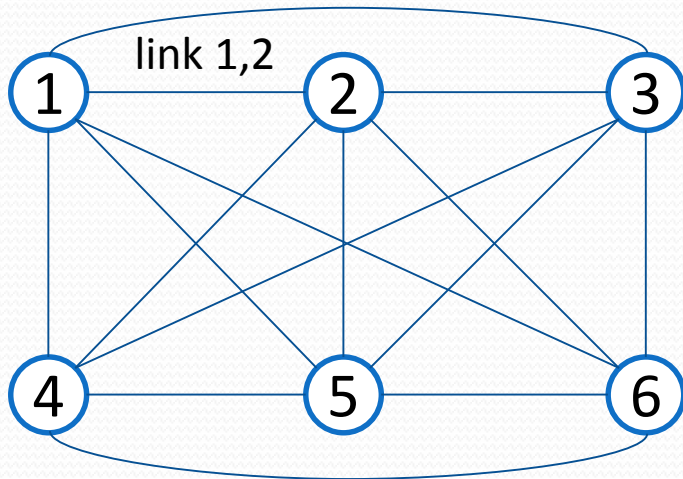
$$\sqrt{\frac{1}{n} \left( (r_1 - r_{i_1})^2 + \dots + (r_n - r_{i_n})^2 \right)}$$

- is minimum
- The position of the target can be estimated as the average position (center of mass,...) among these  $k$  points

# Radio Tomography

- A recent technique
- Exploits a grid of anchors usually deployed at the sides of a room
- The anchors exchange beacons with each other
- If a target cuts the line of sight this results in a significant change in the RSS along a link
  - ...but not so easy, a target also affects other links due to multipath

# Radio Tomography



1	RSS(1,2), ..., RSS(1,6), time
...	...
6	RSS(6,1), ..., RSS(6,5), time



RSS of each link (6·5/2 columns)

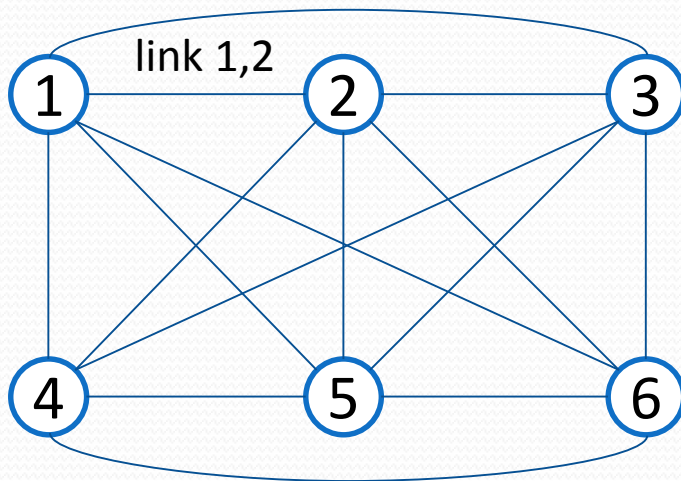

↓  
 $\sigma_{1,2}$

↓  
 $\sigma_{5,6}$

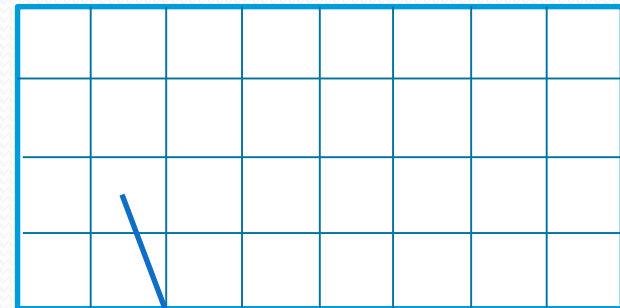
Sliding table: time

Let  $E_{RSS}$  be the average of the RSS on the links when there is no target

# Radio Tomography



Variance-based Radio Tomography Image (VRTI)



Each pixel is dependent on the crossing links (link 2,4 and link 3,4)

Uses  $\sigma_{1,2}, \dots, \sigma_{5,6}$  and  $E_{RSS}$  to compute VRTI (solves an optimization problem)

# Radio Tomography

- See the animation
  - 25 sensors
  - Acquisition rate: 0.11 seconds

# WSN multihop proximity

- Also called *Range-Free* localization: estimate position of objects based on connectivity information
- Cost-Effective: No special hardware for ranging
- Topology based (hop counting) techniques
  - Already discussed in the previous section
- Low precision

# Performance metrics

- Accuracy (location error)
  - Usually measured as mean distance error between real position and estimated position of the target
- Precision
  - Measures the self-consistency of the system
  - In different trials, how does the accuracy varies?
  - Measured with the distribution of the localization accuracy



# Performance metrics

- Complexity
  - Hardware but also communications and algorithms
- Robustness
  - To noisy signals, failure of anchors, non LOS
- Scalability
  - Coverage v.s. positioning performance
- Cost

# Summary

